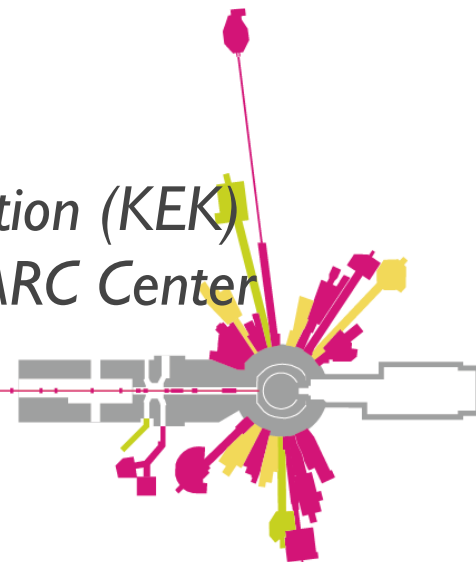


Neutrons in Soft Matter

Hideki Seto

*IMSS, High Energy Accelerator Research Organization (KEK)
Material and Life Science Experimental Facility, J-PARC Center*

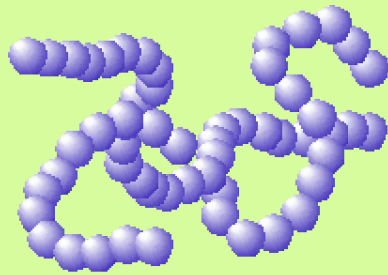


Self-introduction

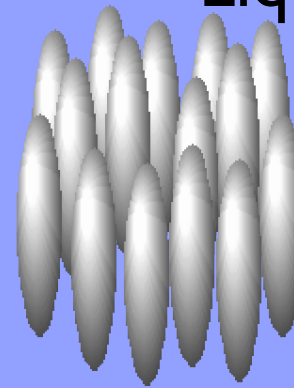
- Born in 1961 Fukushima, Japan
- 1984 Graduated from Kyoto Univ.
- 1989 Ph. D from Osaka Univ. Shape memory alloy
Single X'tal/X-ray, Neutron
- 1989-2002 Research Associate at Hiroshima Univ. Microemulsion
SANS/NSE
- 2002-2008 Associate Prof. at Kyoto Univ. Soft Matter Physics
Non-equilibrium phenomena
- 2008- Professor at KEK J-PARC

Soft Matter

Polymer



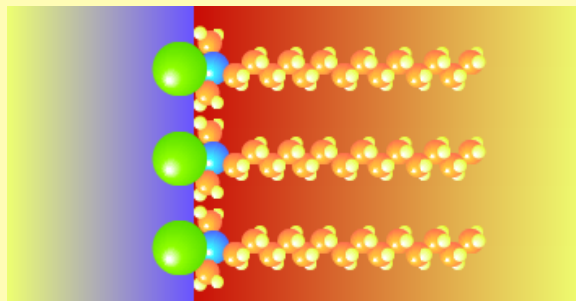
Liquid Crystal



polymeric liquid crystal

liquid crystal polymer

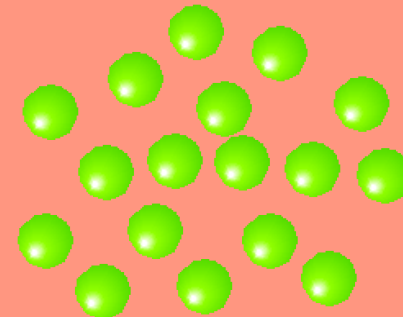
amphiphilic polymer



lyotropic liquid crystal

liquid crystal colloid

emulsion

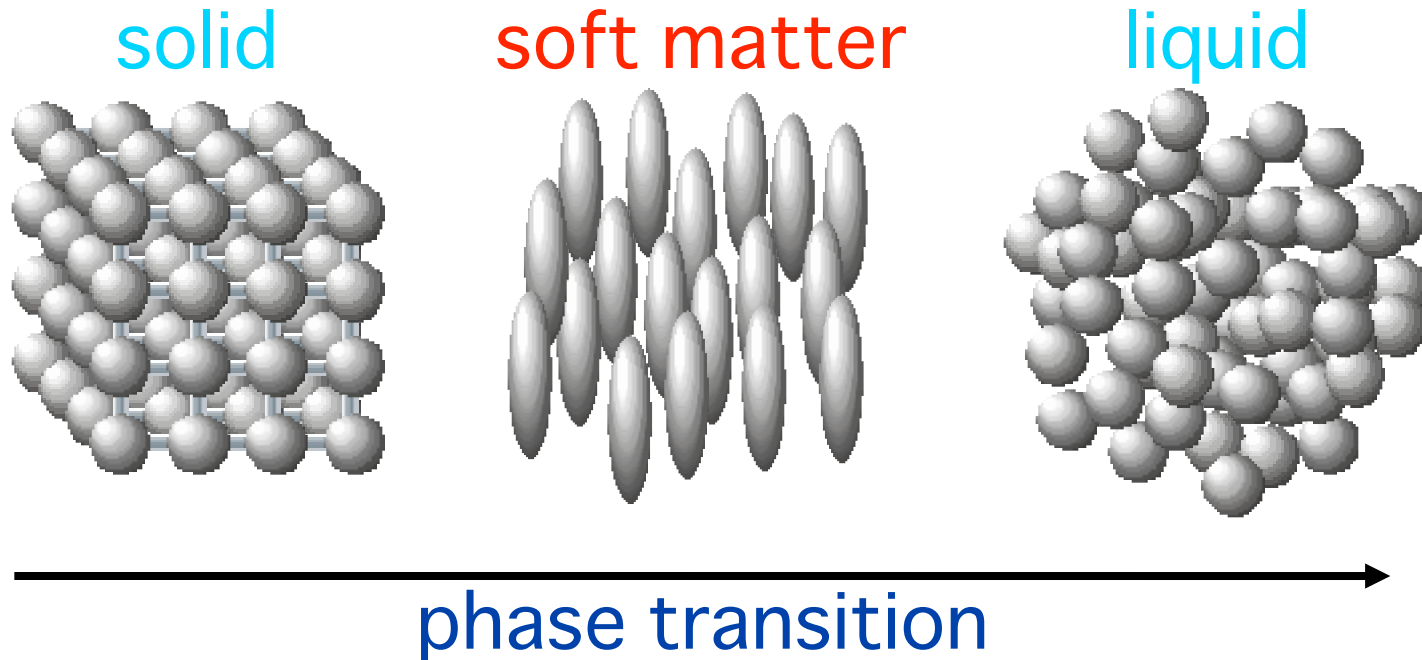


Surfactant

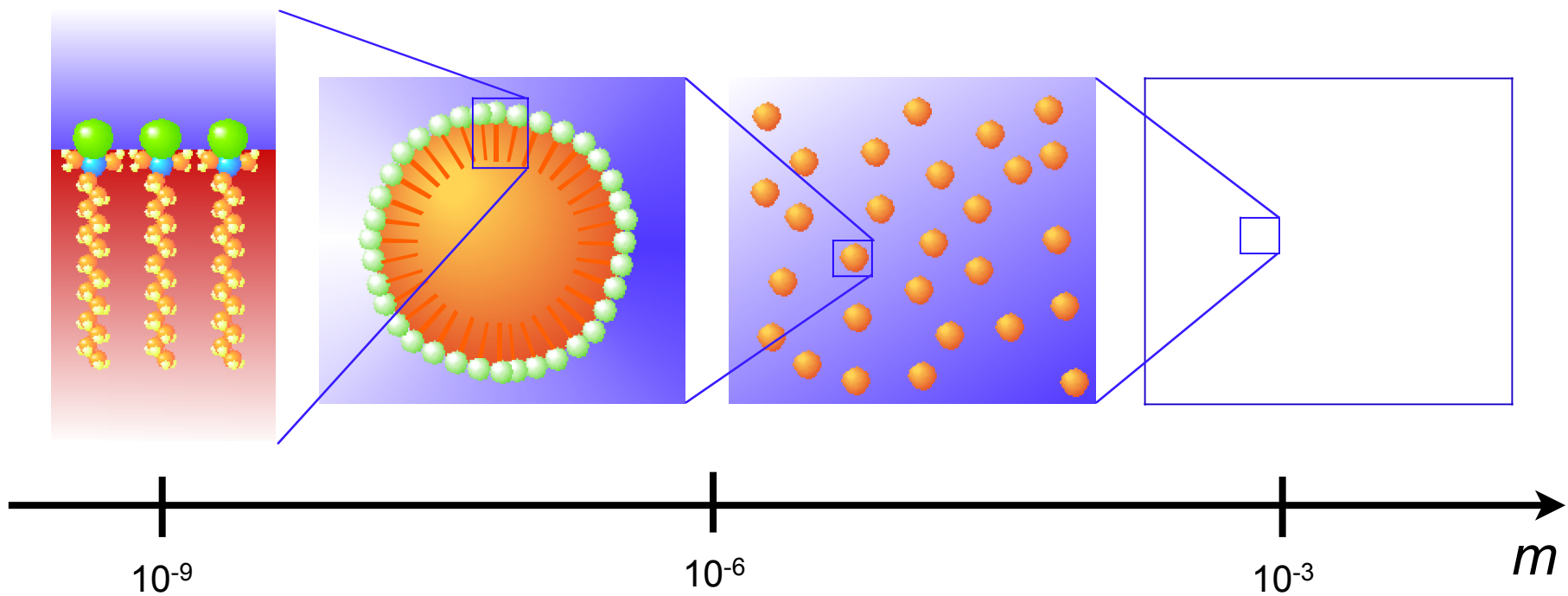
Colloid

Common properties

- large number of internal degree of freedom
- weak interaction between structure unit
- delicate balance of entropy and enthalpy

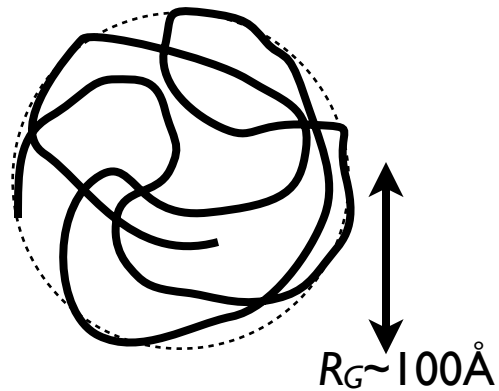


Hierarchical structure

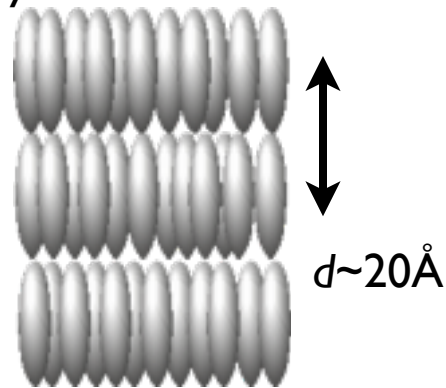


Nano-scale Structures in Soft Matter

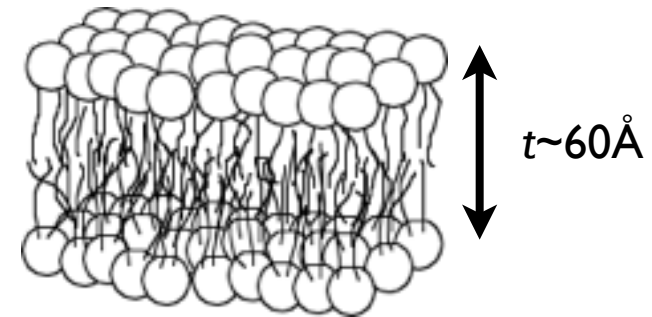
polymer



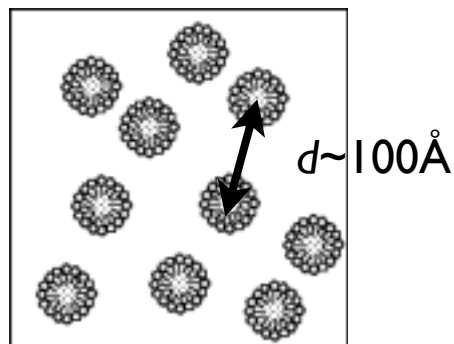
liquid crystal



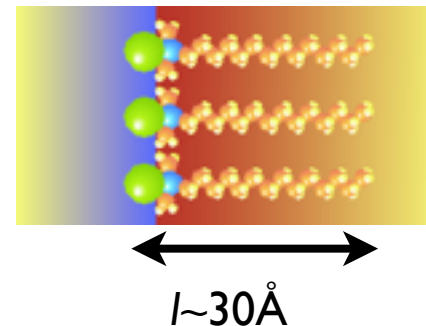
membrane



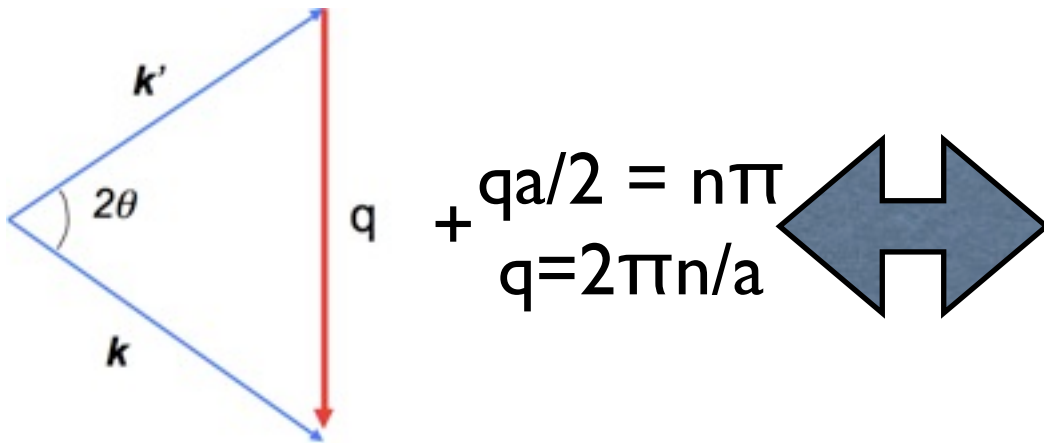
colloids



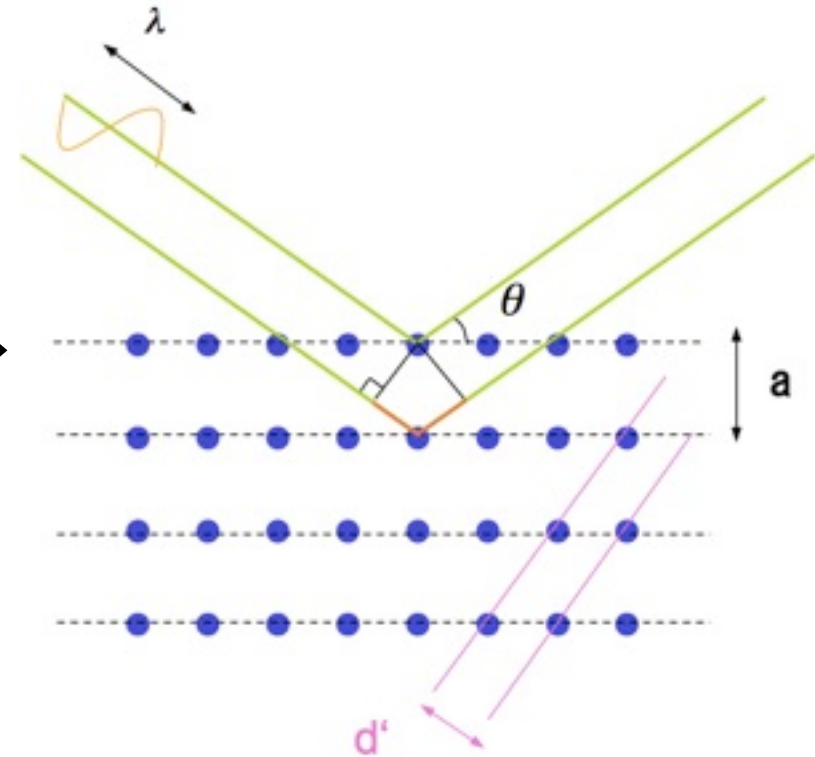
surfactant



Small-Angle Scattering



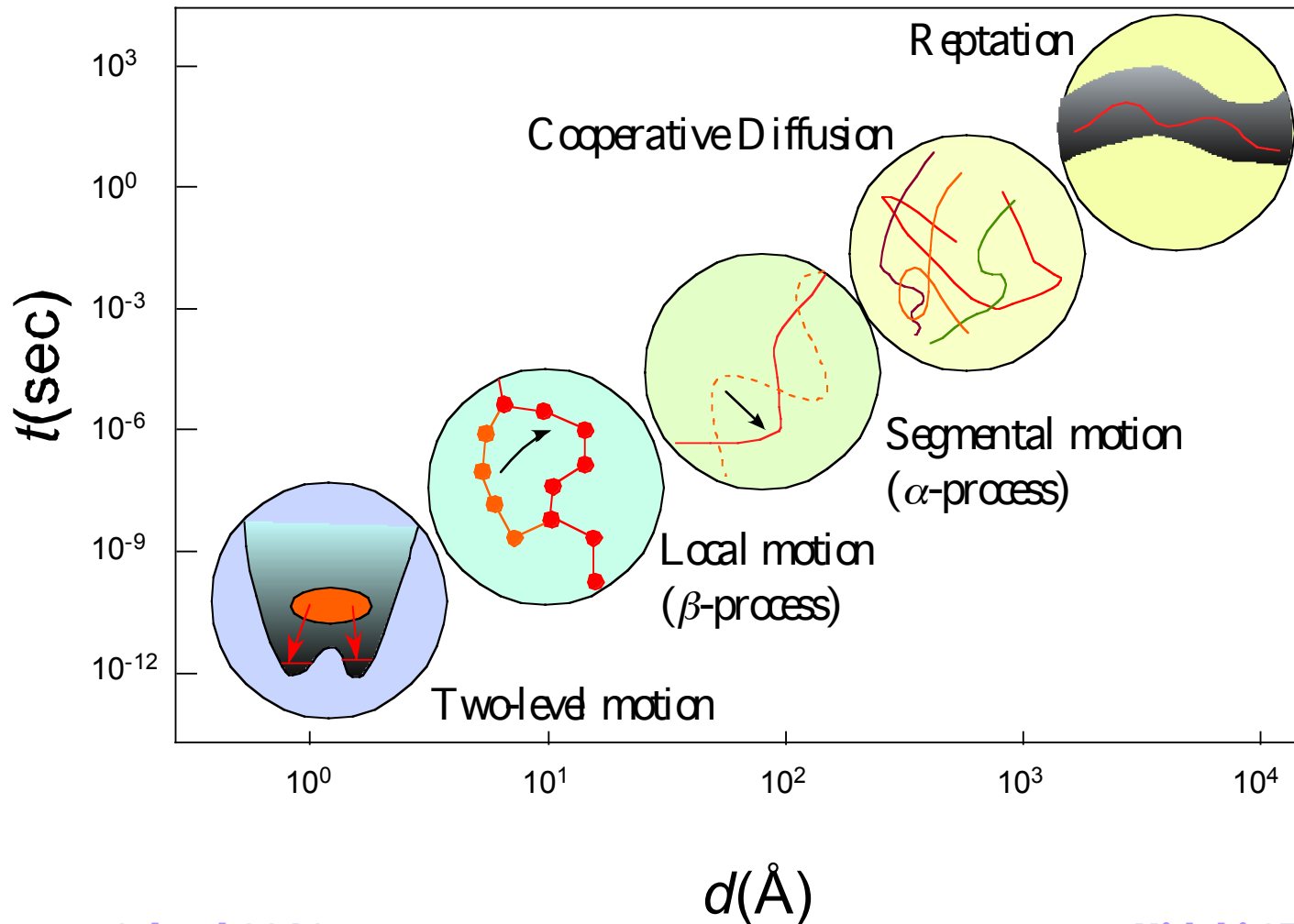
$$\begin{aligned}
 \mathbf{q} &= \mathbf{k} - \mathbf{k}' \\
 q &= 2k \sin \theta \\
 &= 2(2\pi/\lambda) \sin \theta
 \end{aligned}$$



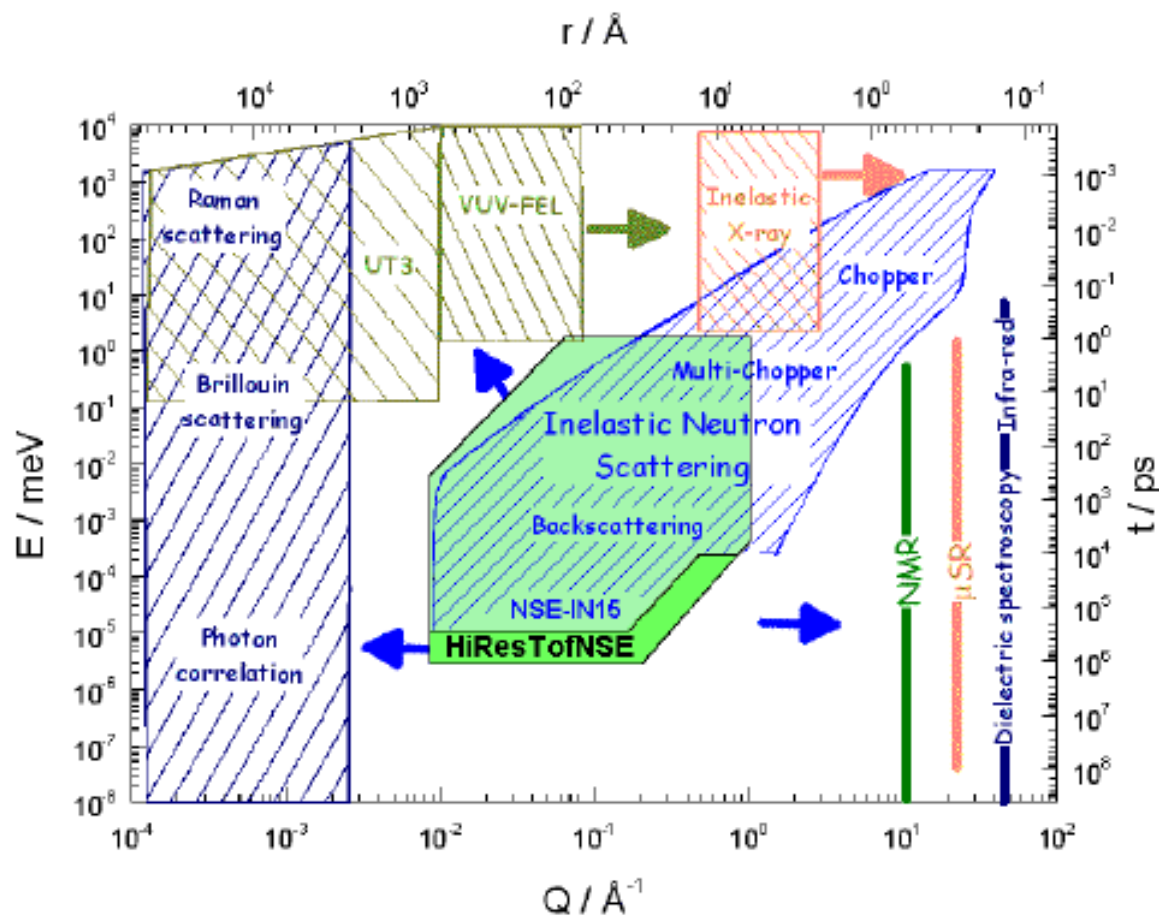
Bragg's Law: $2a \sin \theta = n\lambda$

$\lambda \sim 5\text{\AA}, a \sim 100\text{\AA} \Rightarrow \theta \sim 1.4^\circ$

Hierarchical dynamics

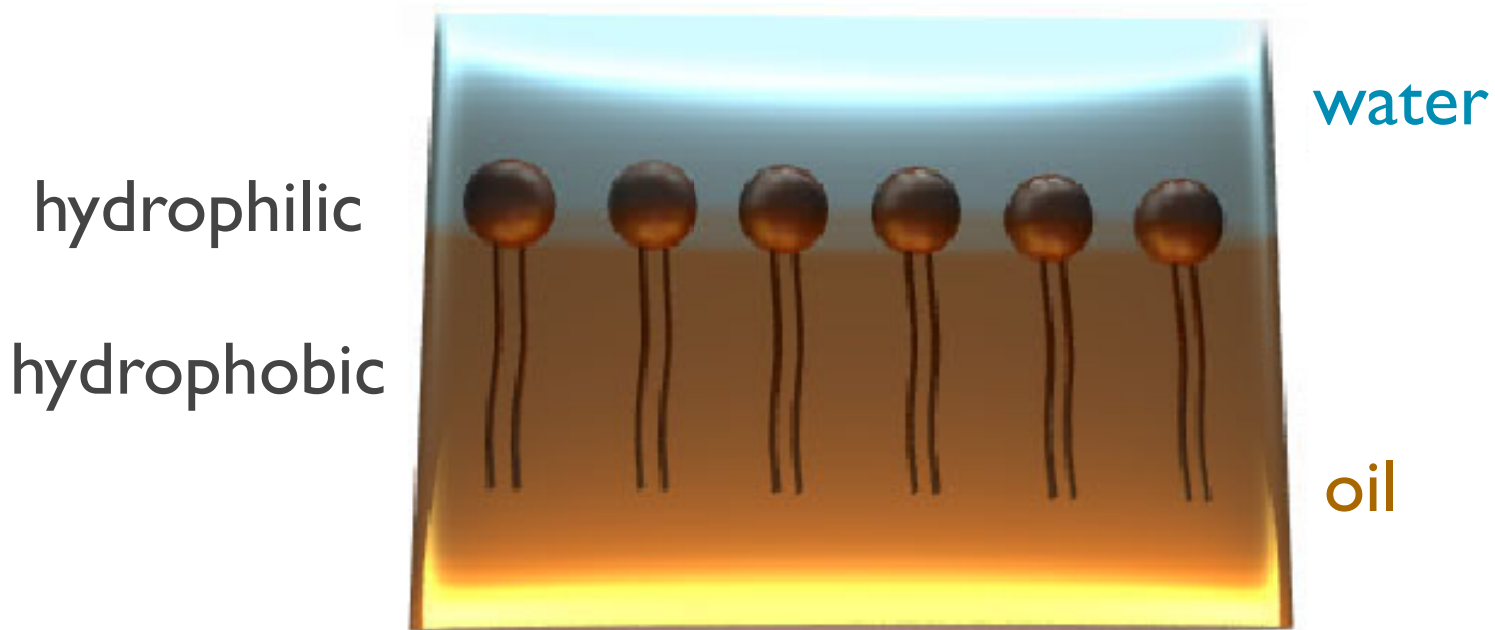


Inelastic/Quasi-elastic scattering

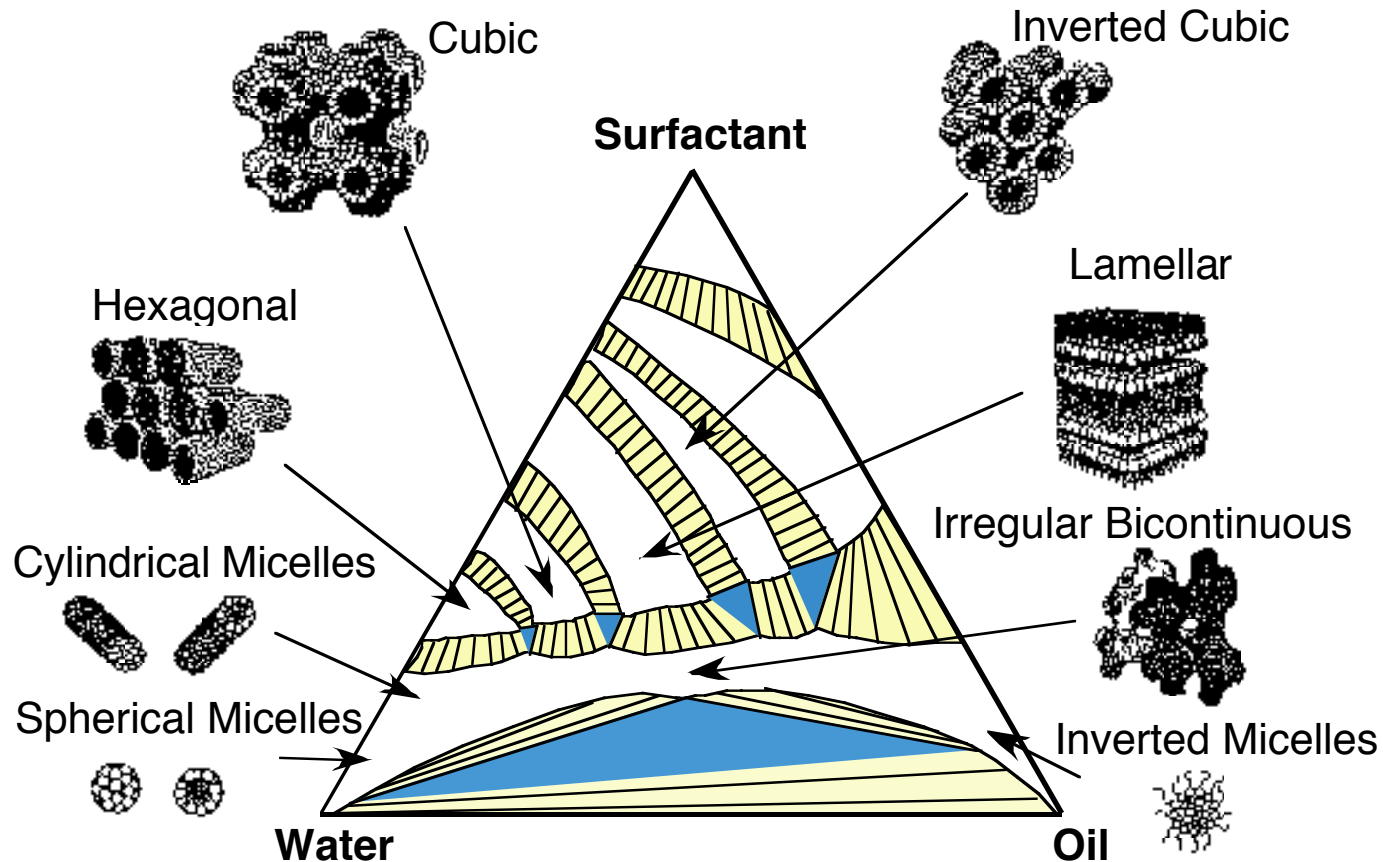


Surfactants

Amphiphilic property

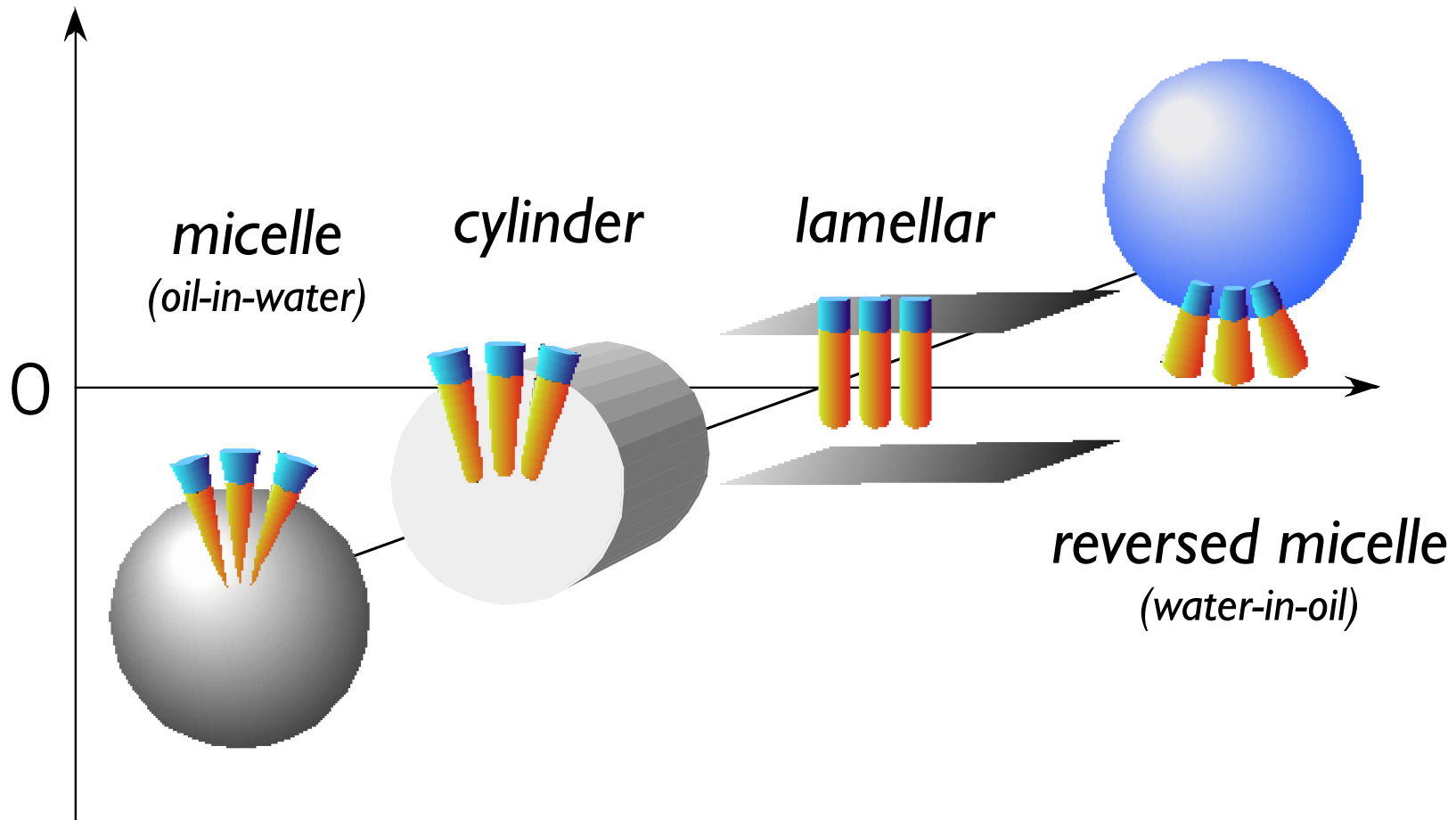


Semi-microscopic structures

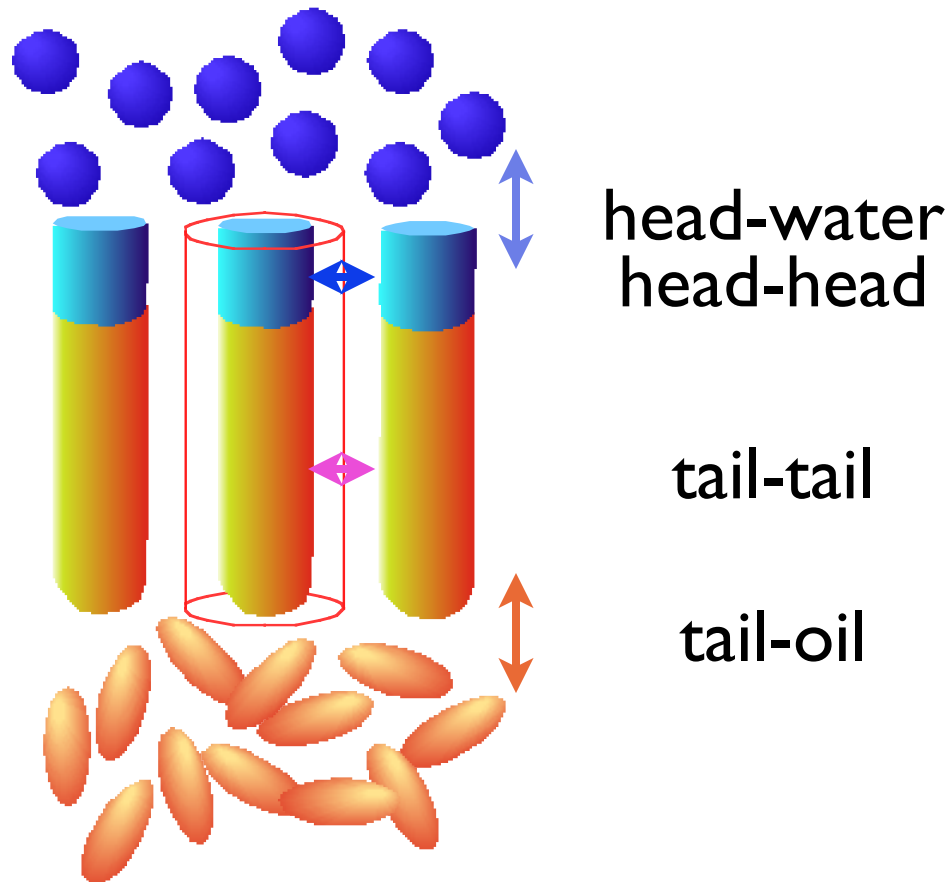


Spontaneous Curvature

depends on packing parameter

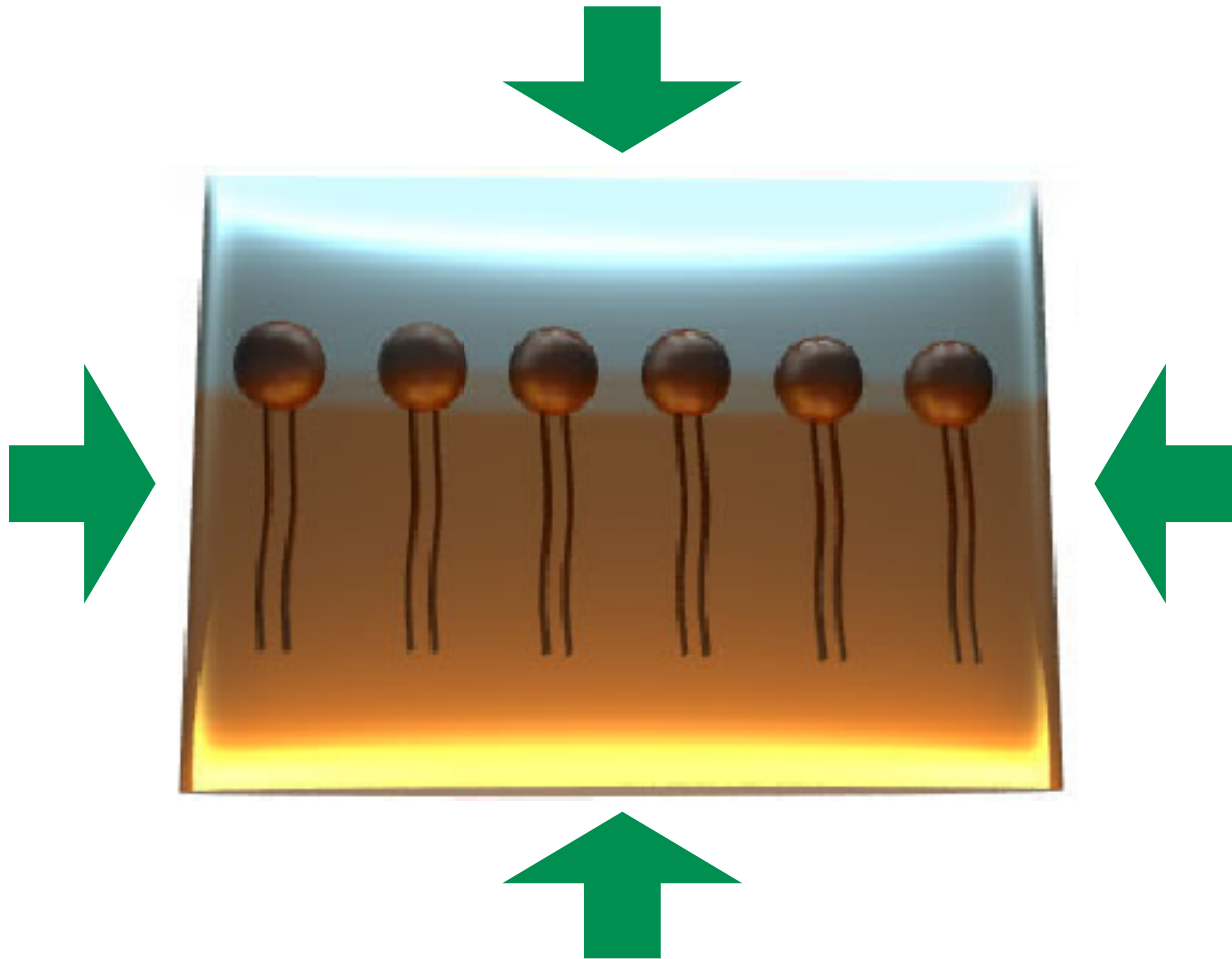


Packing parameter

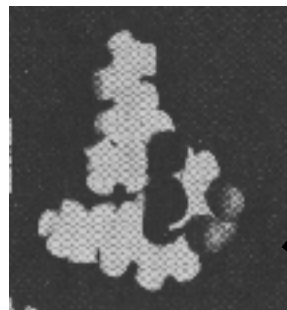


Pressure dependence

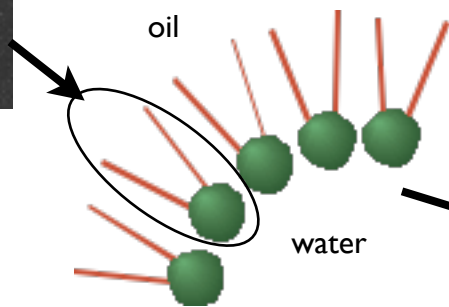
M. Nagao, HS, et al. 1999-2007



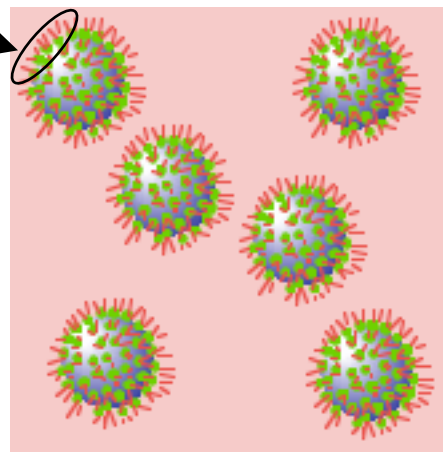
AOT + D₂O + *n*-decane



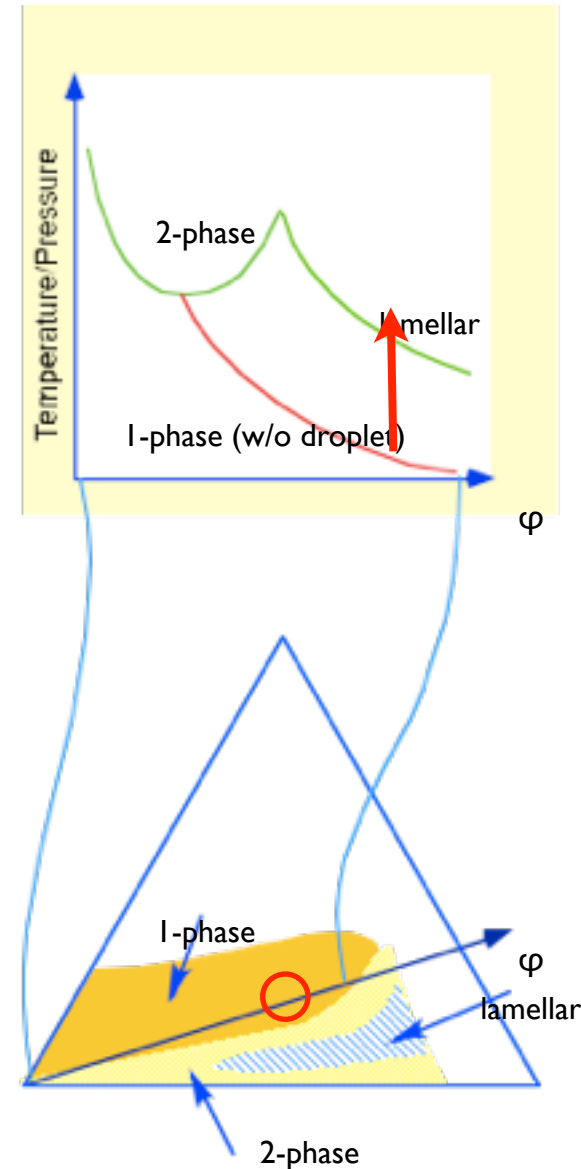
AOT molecule



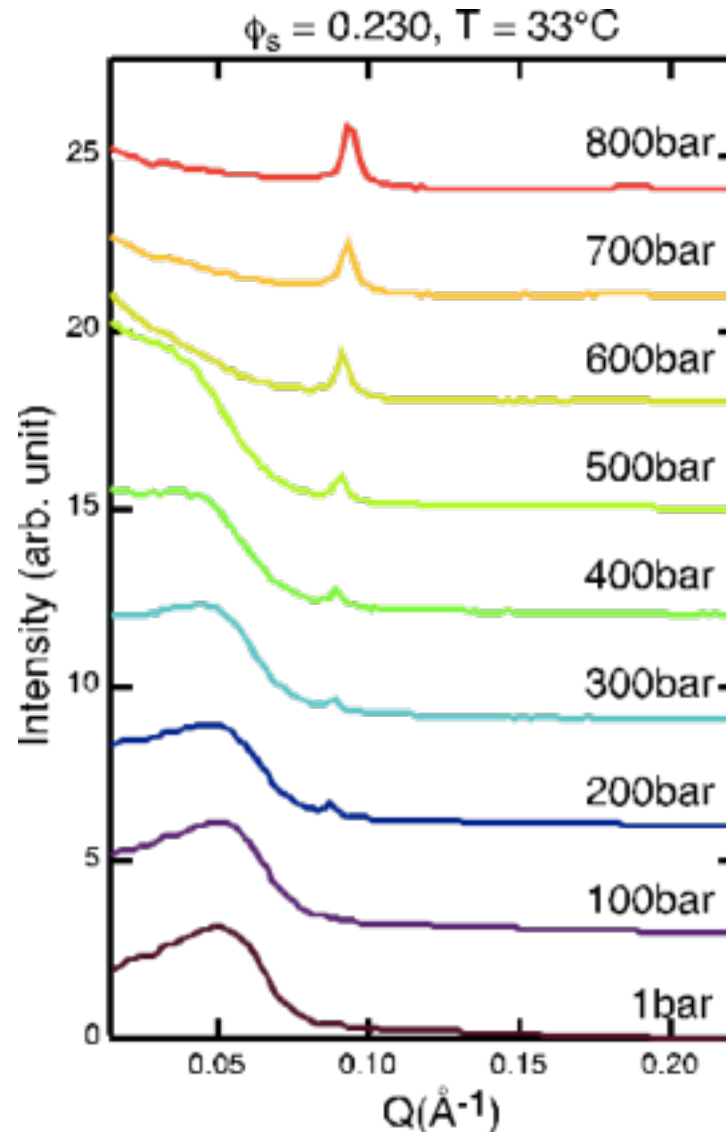
spontaneous curvature > 0



water-in-oil droplet



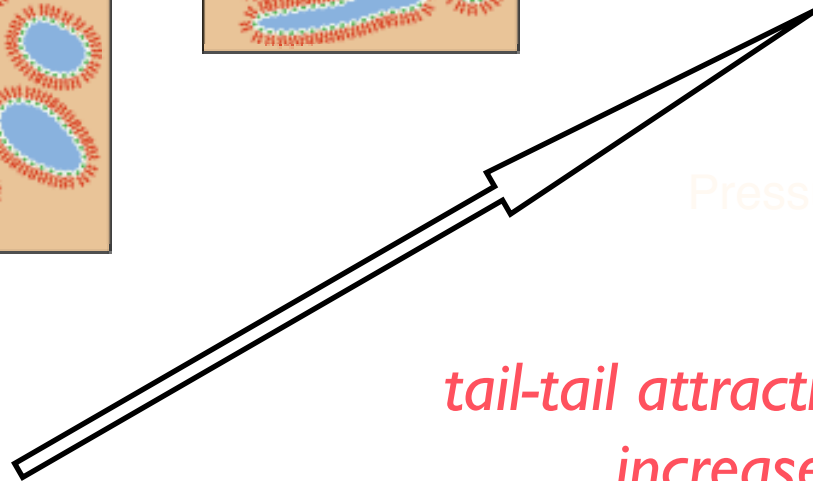
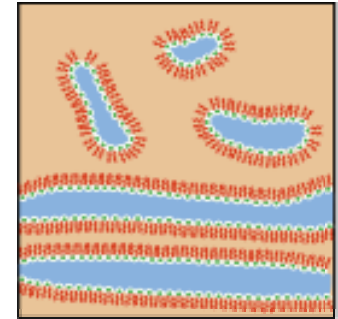
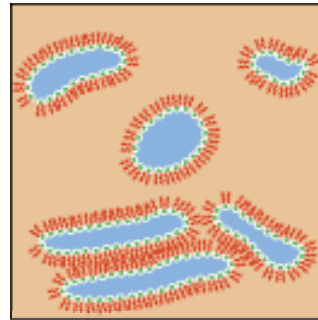
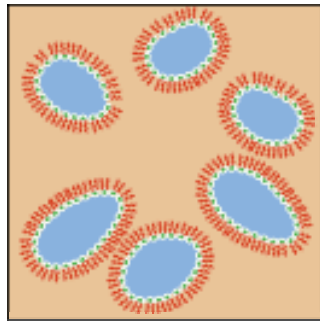
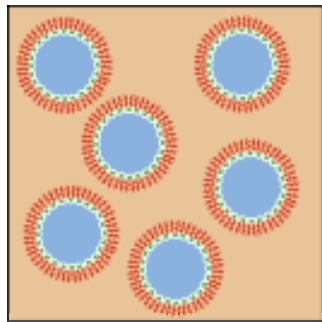
Pressure dependence of SAXS



Structure change with P



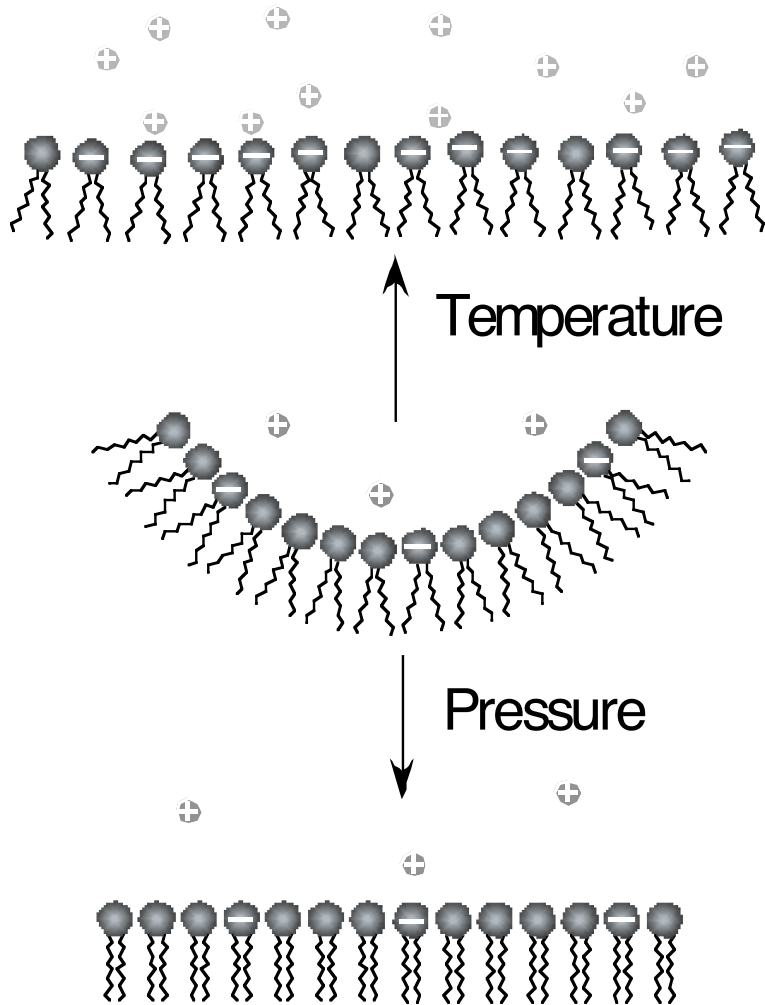
The same as increasing T



Pressure

tail-tail attractive force increases

Why T-effect and P-effect seems to be the same?



counter-ion dissociation

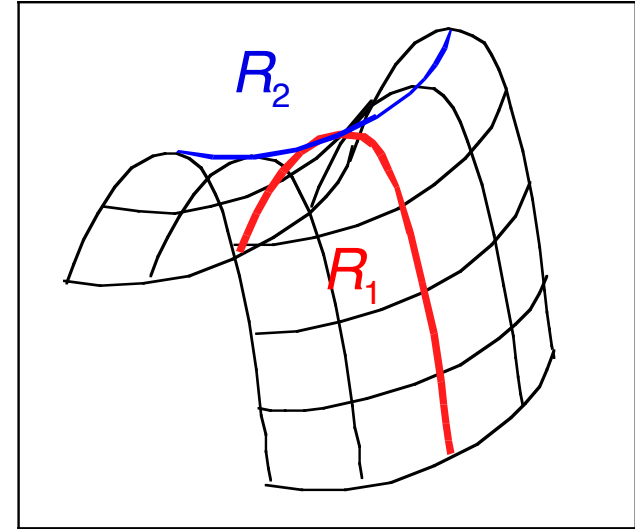
tail-tail interaction

Bending energy of surfactant layers

W. Helfrich, Z. Naturforsch. C28 (1973) 693

mean curvature $H = \frac{1}{2} \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$

Gaussian curvature $K = \frac{1}{R_1} \frac{1}{R_2}$



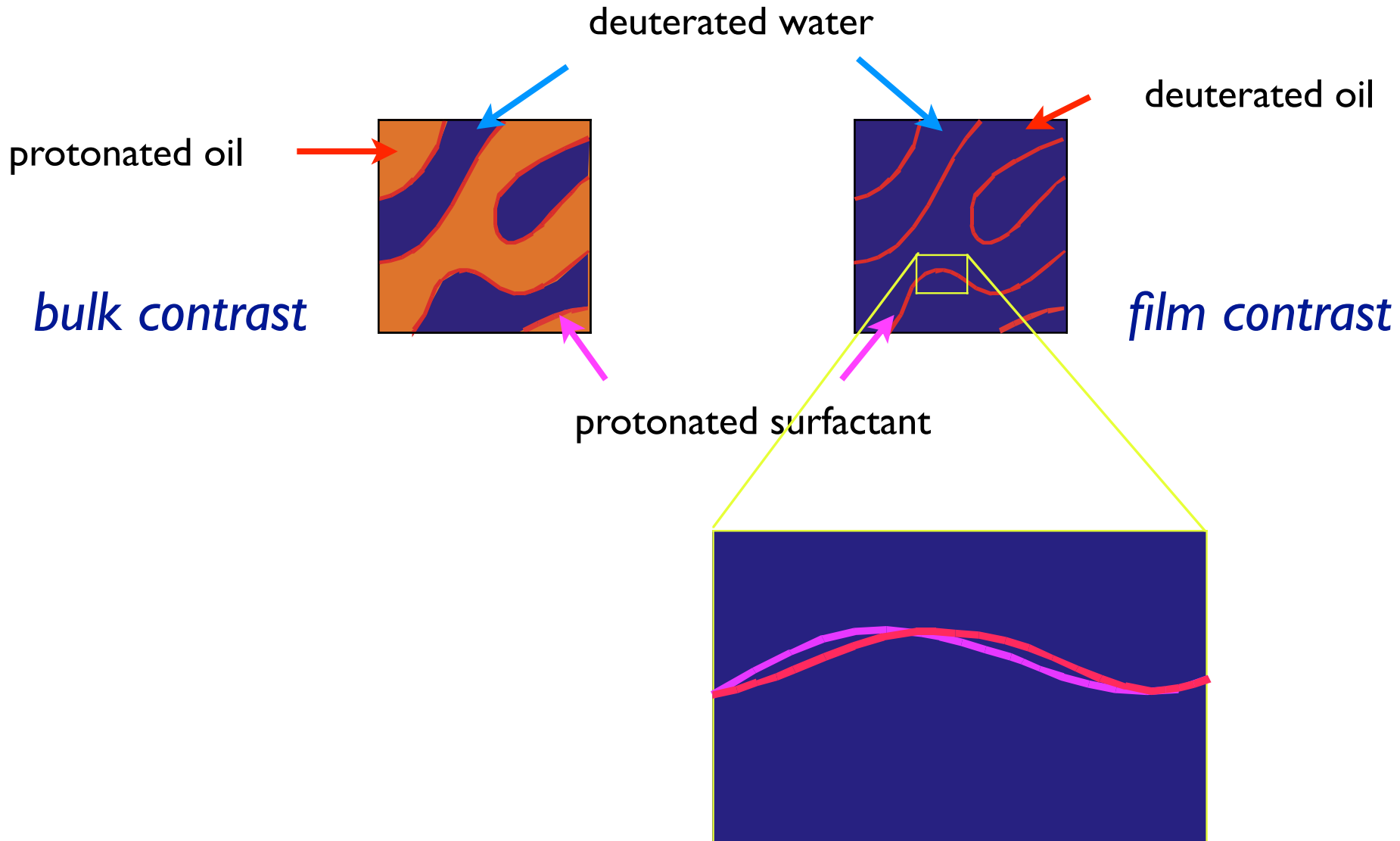
bending modulus

saddle-splay modulus

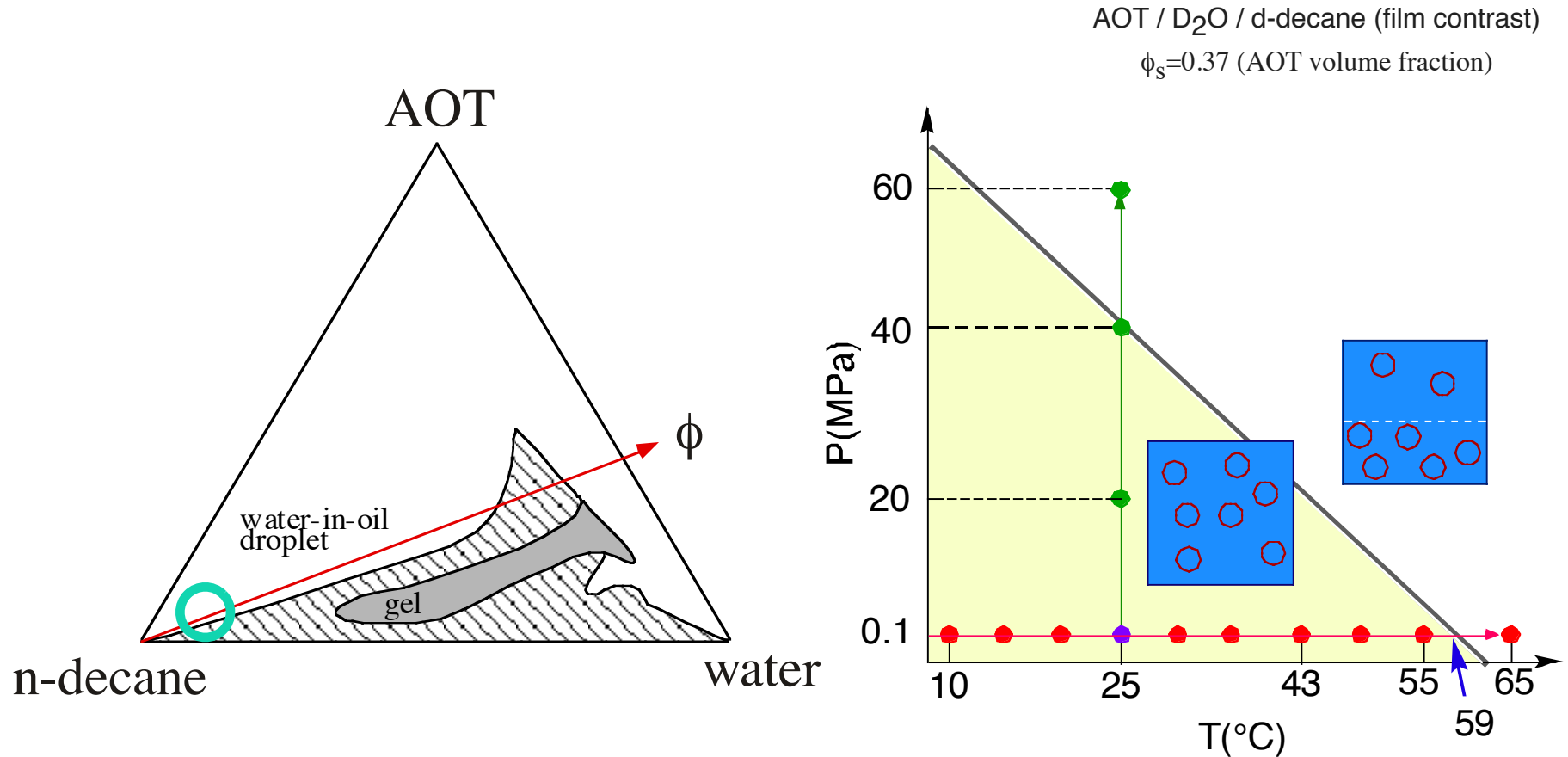
$$E_{bend} = \int \left[\kappa \left(H - \frac{1}{R_s} \right)^2 + \bar{\kappa} K \right] dS$$

spontaneous curvature

Neutrons see...

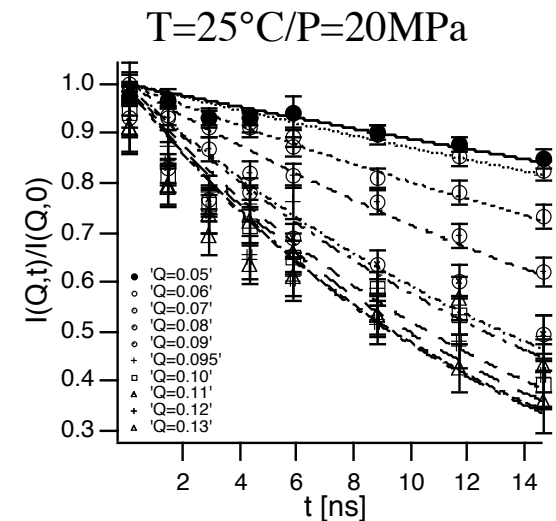
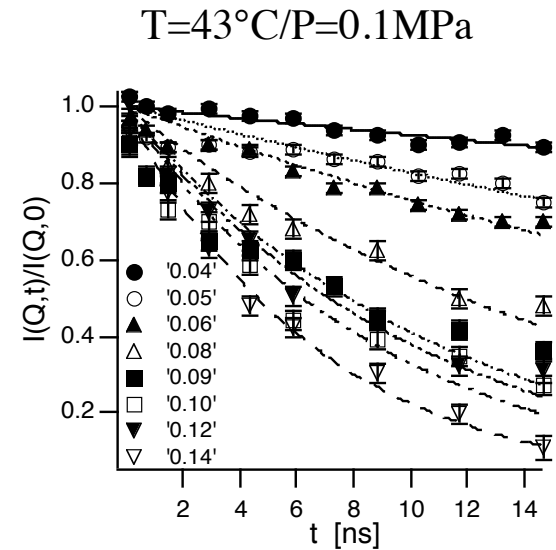
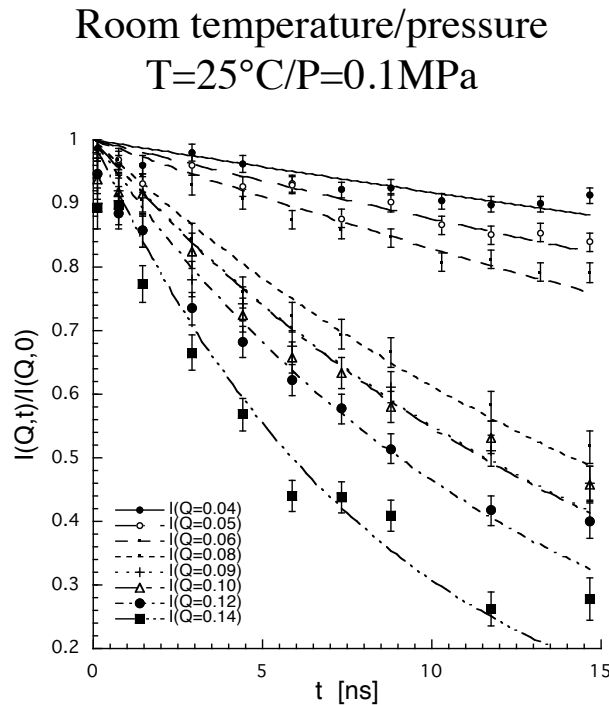


Phase separation of a water-in droplet



Kawabata et al., Phys. Rev. Lett. **92** (2004) 056103.

Results of NSE experiments



Scattering from a shell

Expansion of the shape fluctuation into spherical harmonics

Huang et al. PRL 59 (1987) 2600.
Farago et al. PRL **65** (1990) 3348.

$$R(\theta, \phi, t) = R_0 \left\{ 1 + \sum_{nm} a_{nm}(t) Y_{nm}(\theta, \phi) \right\}$$

up to n=2 mode gives

$$I(Q, t) / I(Q, 0) = \exp[-D_{eff} Q^2 t]$$

$$D_{eff} = D_{tr} + \frac{5 f_2 j_2(QR_0) \langle |a_2|^2 \rangle}{Q^2 [4 \pi f_0(QR_0) + 5 f_2(QR_0) \langle |a_2|^2 \rangle]}$$

damping frequency of the 2nd mode deformation

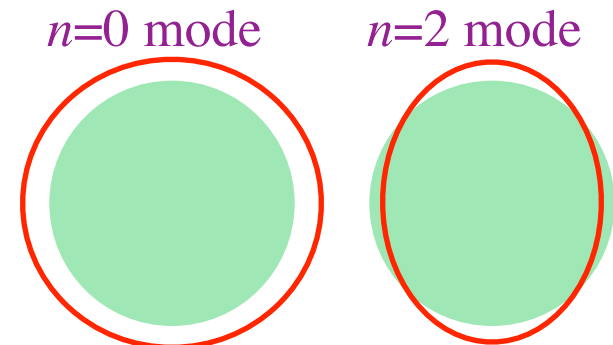
mean-square displacement of the 2nd mode deformation

translational diffusion shape deformation

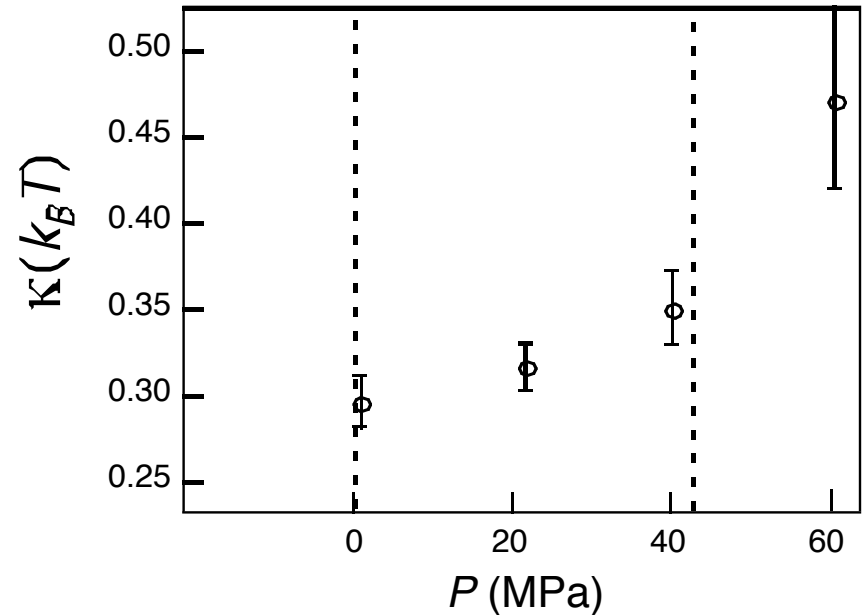
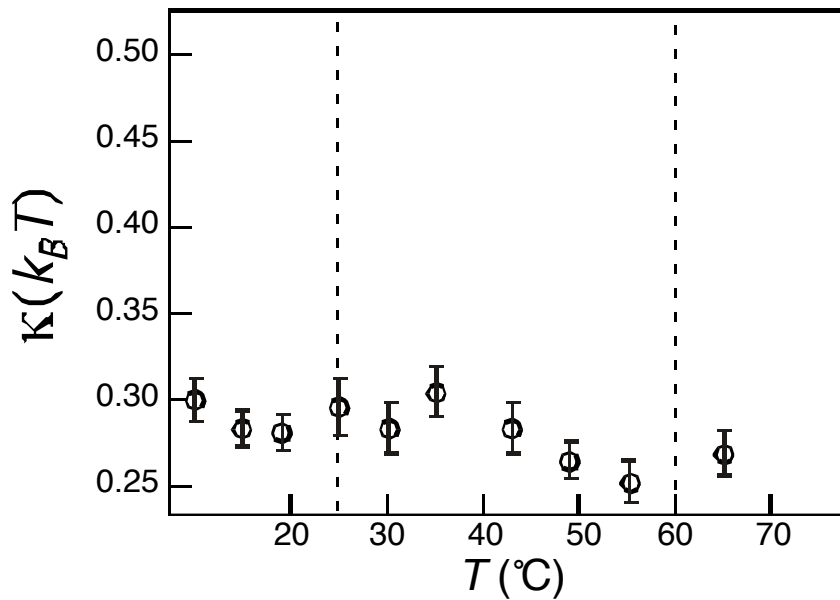
where

$$f_0(QR_0) = [j_0(QR_0)]^2$$

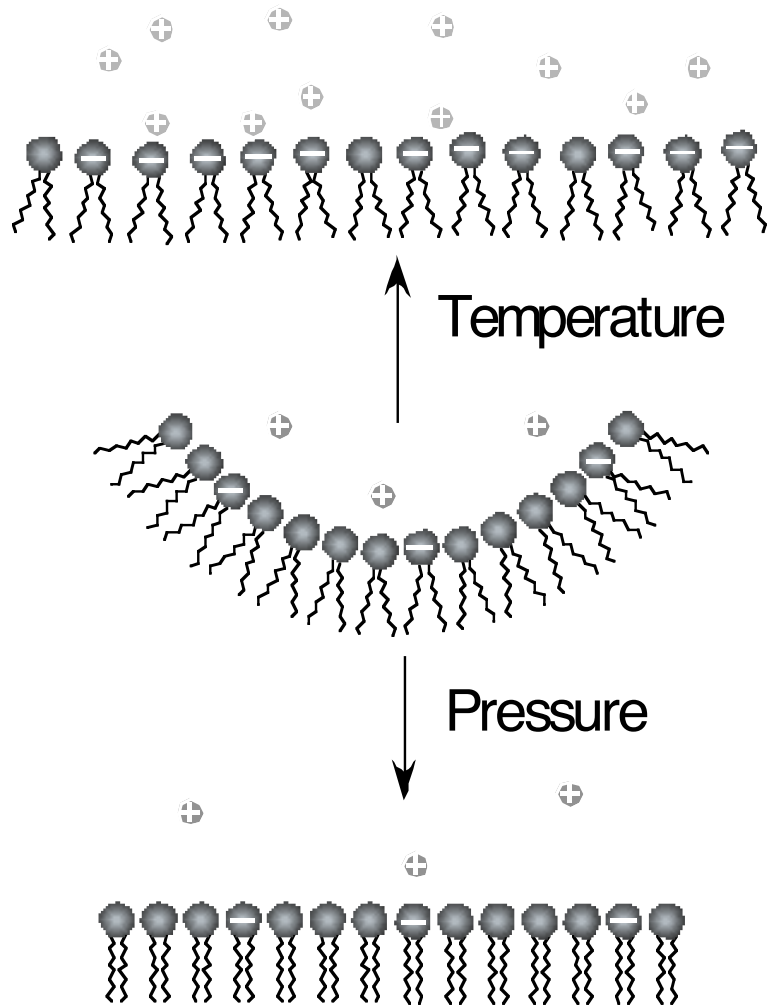
$$f_2(QR_0) = 5[4 j_2(QR_0) - (QR_0) j_3(QR_0)]^2$$



T- and P- dependence of the bending modulus



T- and P-effects on an ionic surfactant monolayer



spontaneous
curvature

bending
modulus

decrease

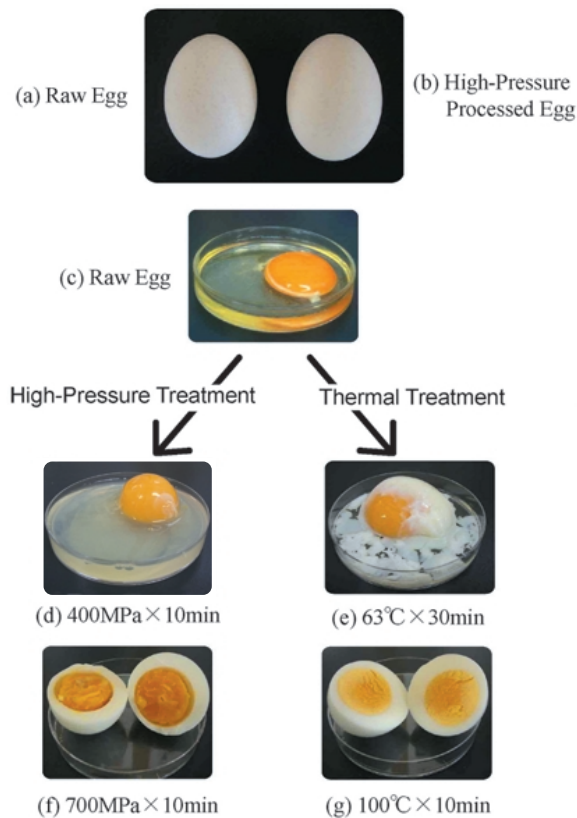
decrease

decrease

increase

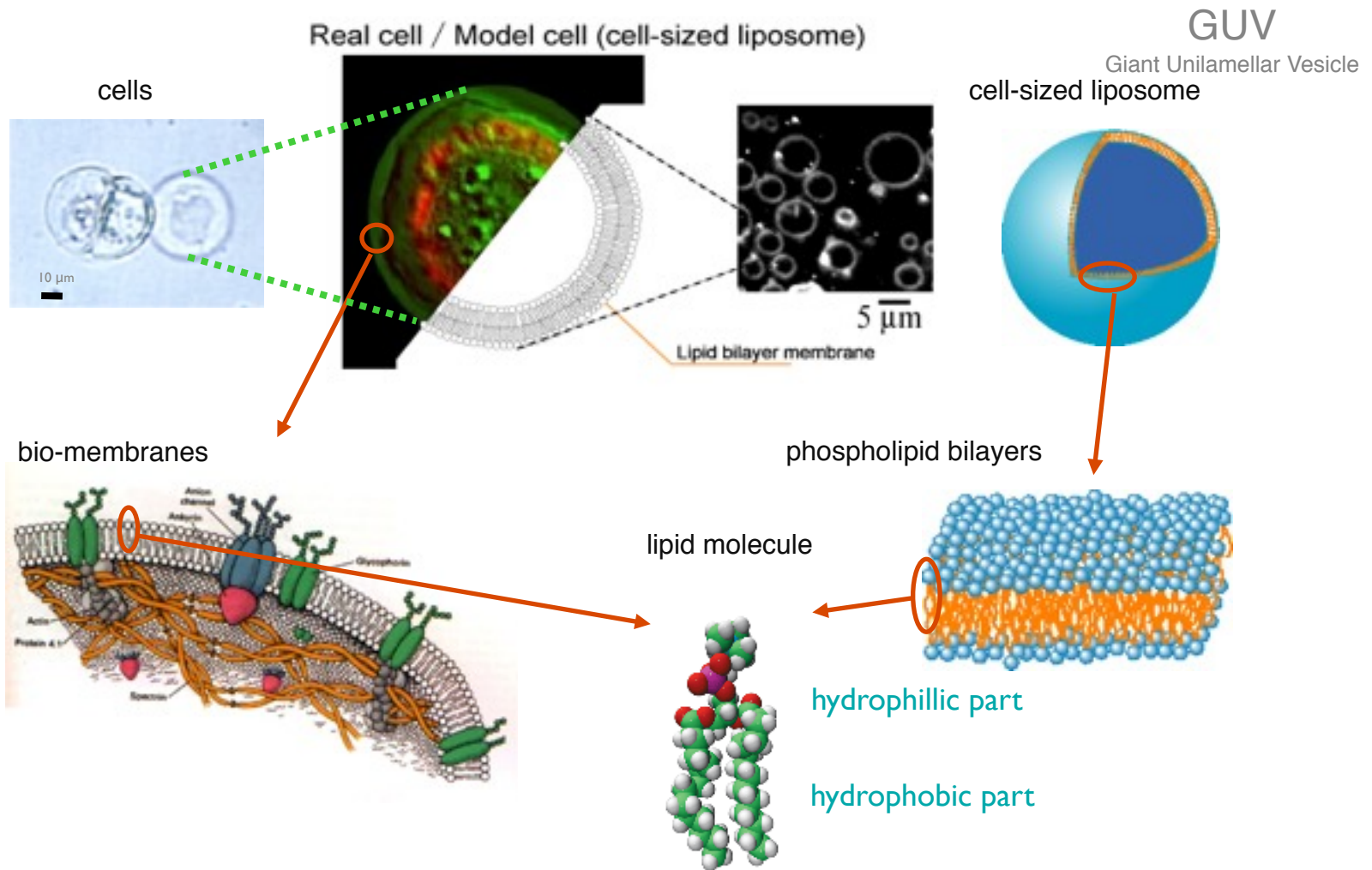
Possible application

- pressure antagonism of anesthesia
- deep sea organisms
- food processing



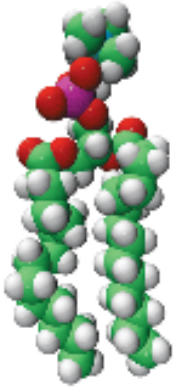
Lípids

Cells and Vesicles

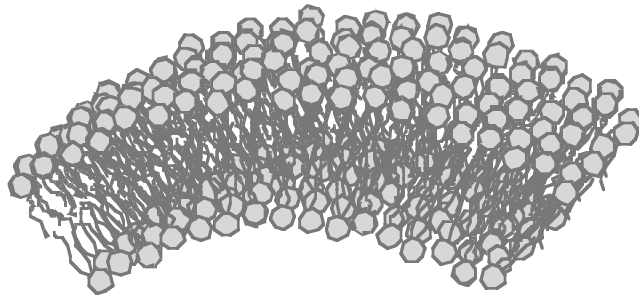
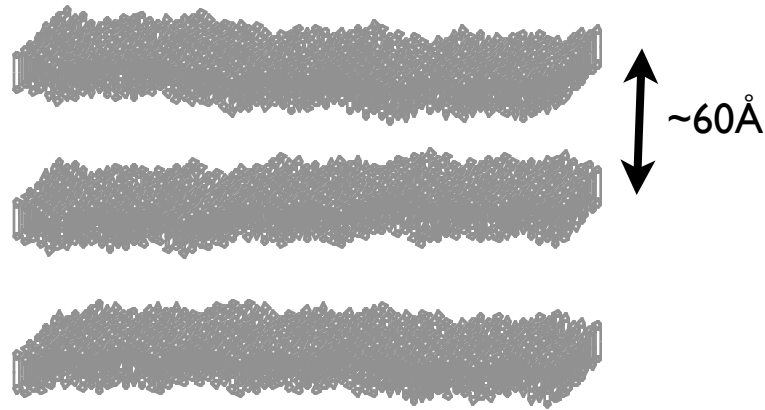


Lamellar structure of lipid bilayers

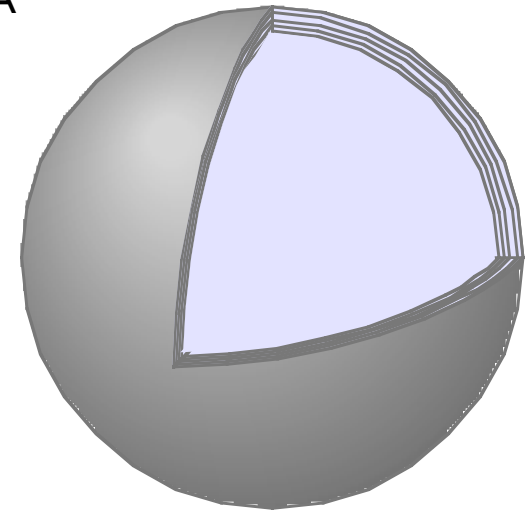
phospholipid



lamellar structure



bilayer



multilamellar vesicles

10^{-10}

10^{-9}

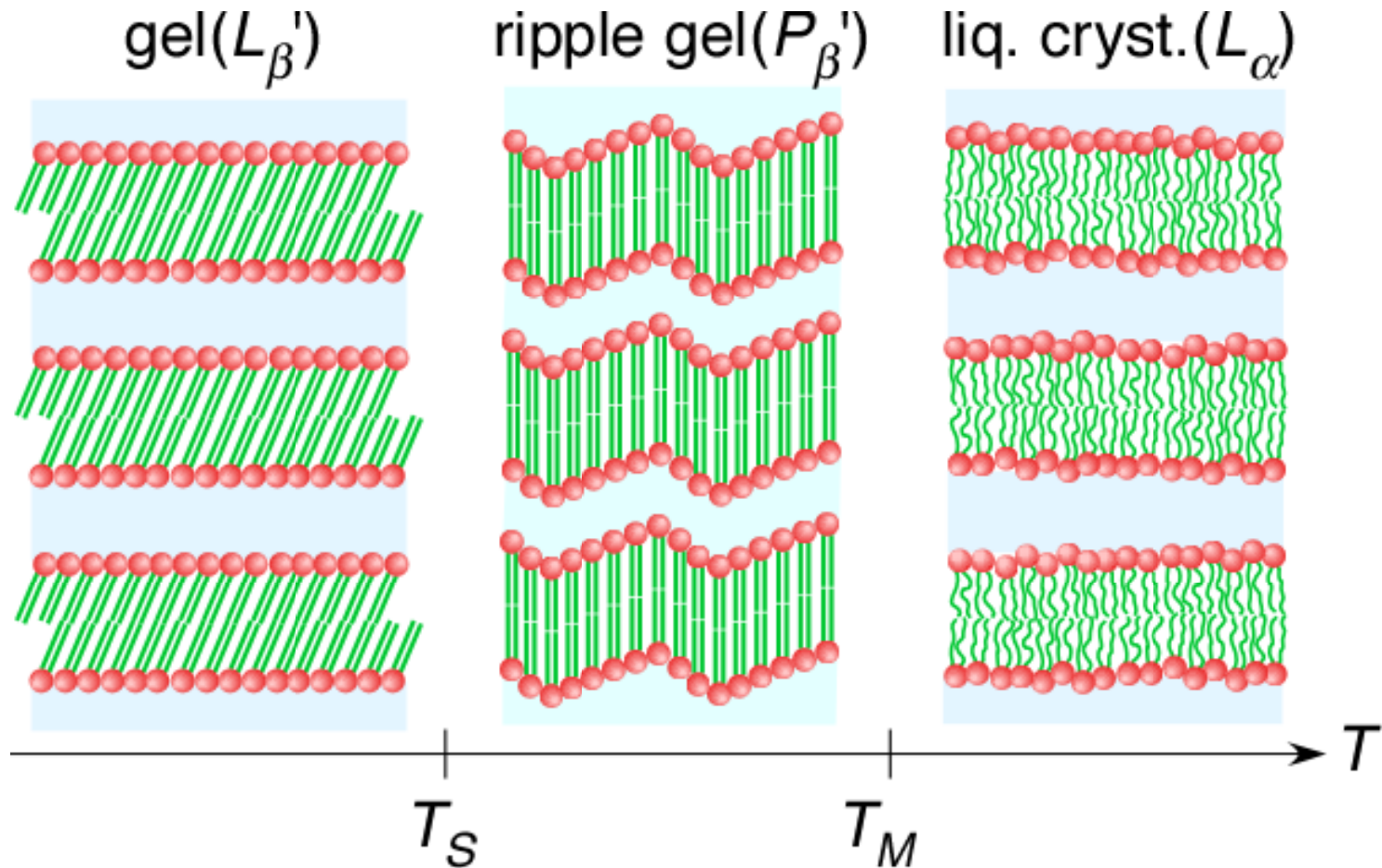
10^{-8}

10^{-7}

10^{-6}

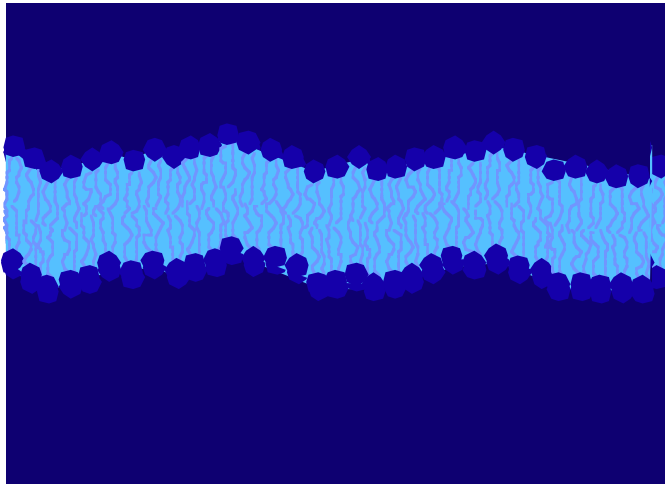
scale [m]

Phase transitions of lipid bilayers



Neutron vs X-ray

neutron

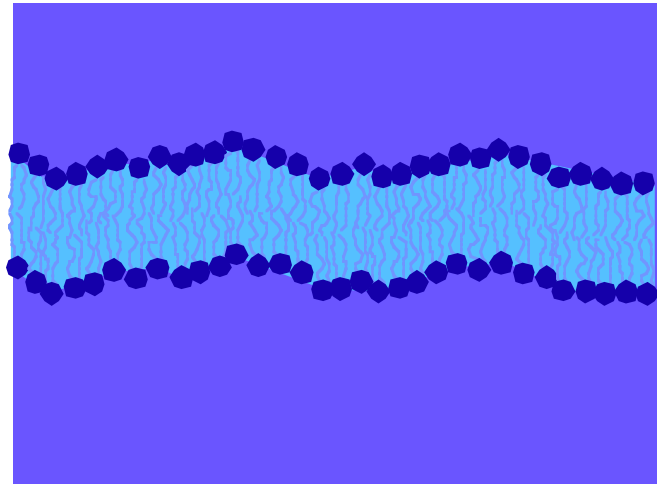


dynamical behavior



bending modulus

x-ray



static structure

NSE measurements on lipid bilayers

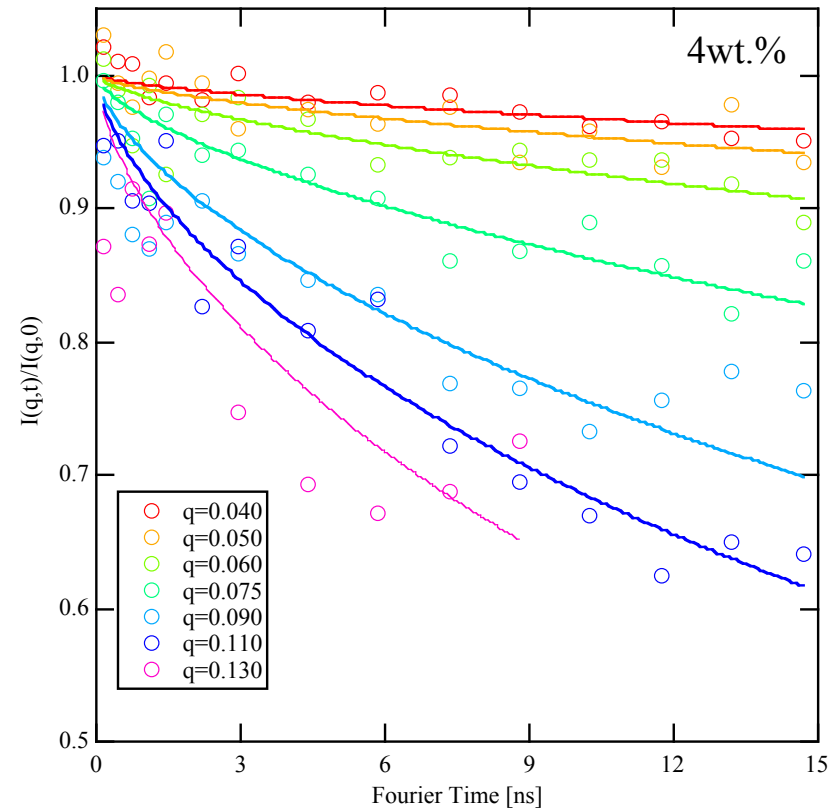
N. L. Yamada, HS, et al. 2005-2008

DPPC/CaCl₂/D₂O
(DPPC: 4wt%, CaCl₂: 7mM)

$d \sim 1000 \text{ \AA}$



Considered as a single
membrane fluctuation.



Single membrane fluctuation

Zilman and Granek

A lateral length L along the membrane flat surface is perturbed in some way, because they are 2D connected object.

$$h \simeq (k_B T / \kappa)^{1/2} L^\zeta \quad \text{roughness exponent: } \zeta = 1 \quad (2\text{D object}) \\ = 3/2 \quad (1\text{D object})$$

$$L \simeq (\kappa / k_B T)^{1/2\zeta} Q^{-1/\zeta}$$

The Stokes-Einstein diffusion coefficient is,

$$D(Q) \simeq (k_B T / \eta L) \simeq (k_B T / \eta) (k_B T / \kappa)^{1/2\zeta} Q^{1/\zeta}$$

The relaxation rate is,

$$\Gamma(Q) \simeq D(Q) Q^2 \simeq (k_B T / \eta) (k_B T / \kappa)^{1/2\zeta} Q^{2+(1/\zeta)}$$

Thus they obtained the stretched exponential form of the relaxation function as,

$$I(Q, t) = \exp[-(\Gamma(Q)t)^\beta]$$

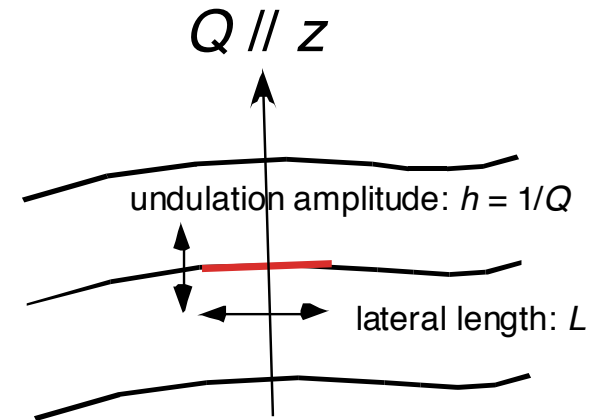
where

$$\Gamma(Q) = \gamma_\alpha \gamma_\kappa (k_B T)^{1/\beta} \kappa^{1-(1/\beta)} \eta^{-1} Q^{2/\beta}$$

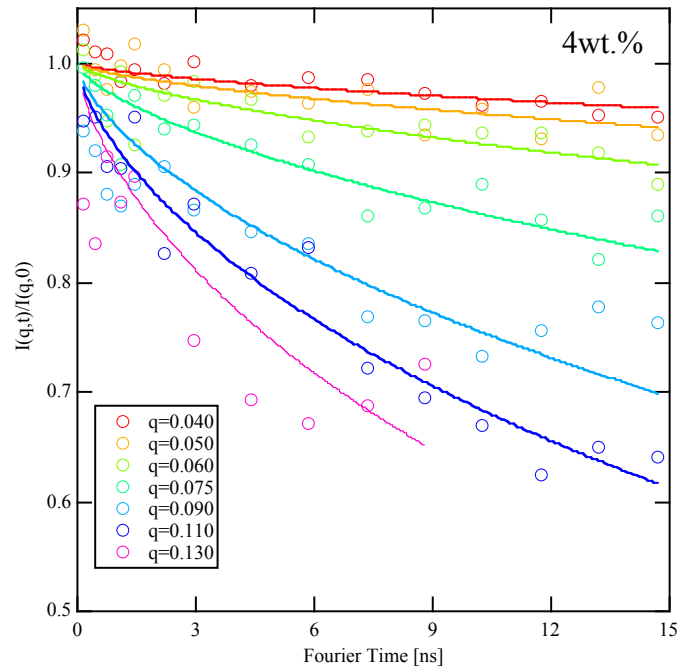
with

$$\beta = 2 / (2 + 1/\zeta) = 2/3 \quad (2\text{D object}) \quad \gamma_\alpha = 0.024 \quad (2\text{D object}) \\ = 3/4 \quad (1\text{D object}) \quad = 0.0056 \quad (1\text{D object})$$

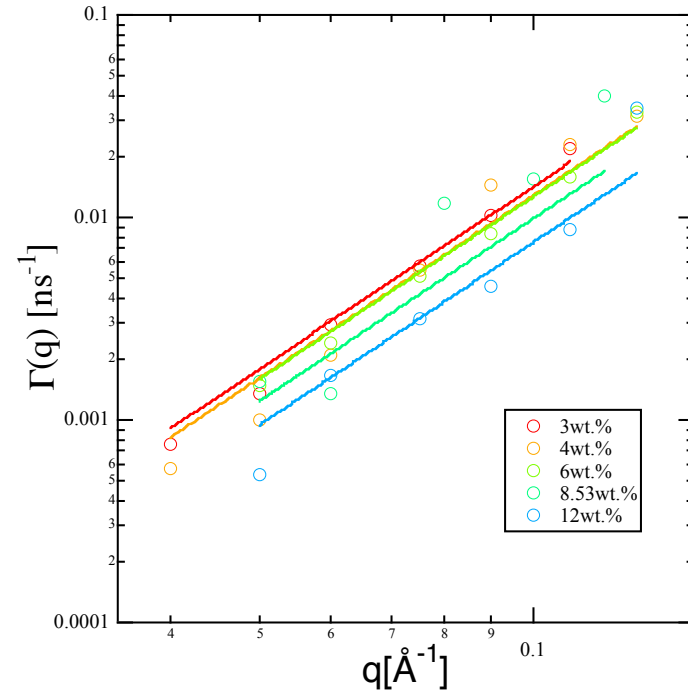
$$\gamma_\kappa = 1 - 3 \ln(\xi / l(t)) k_B T / (4\pi\kappa)$$



NSE results



$$I(q,t) = I(q,0) \exp(-(\Gamma t)^{2/3})$$



$$\Gamma = Aq^3$$

$$K_C = (\gamma_\alpha \gamma_\kappa (k_B T)^{3/2} / A \eta)^2$$

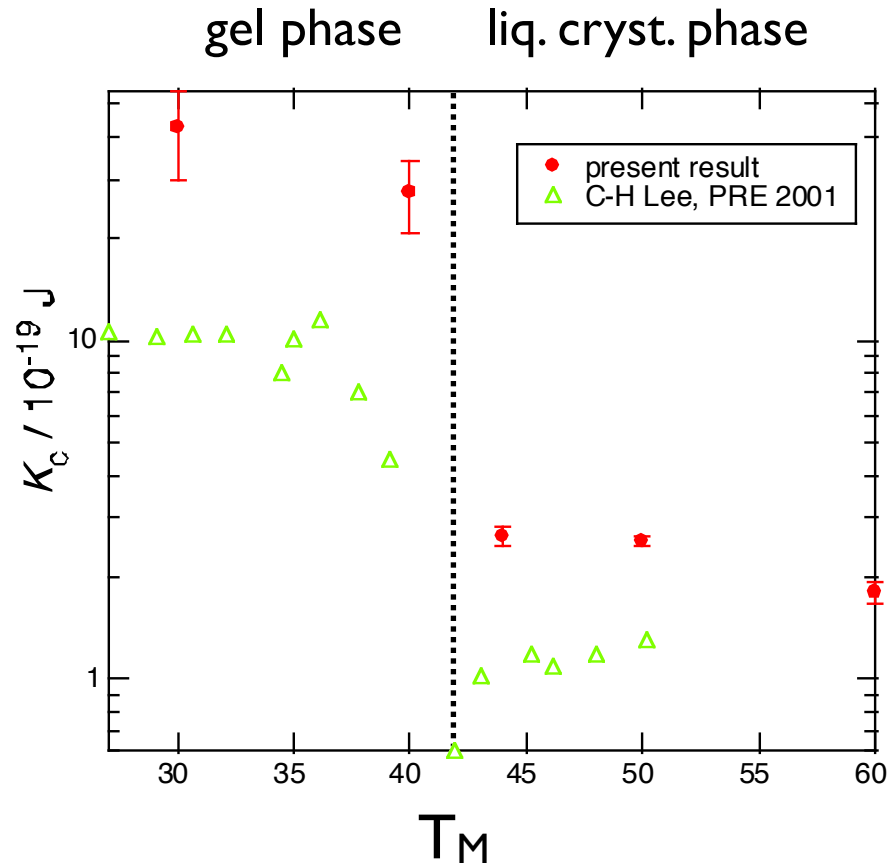
K_C : bending modulus

η : viscosity of D₂O

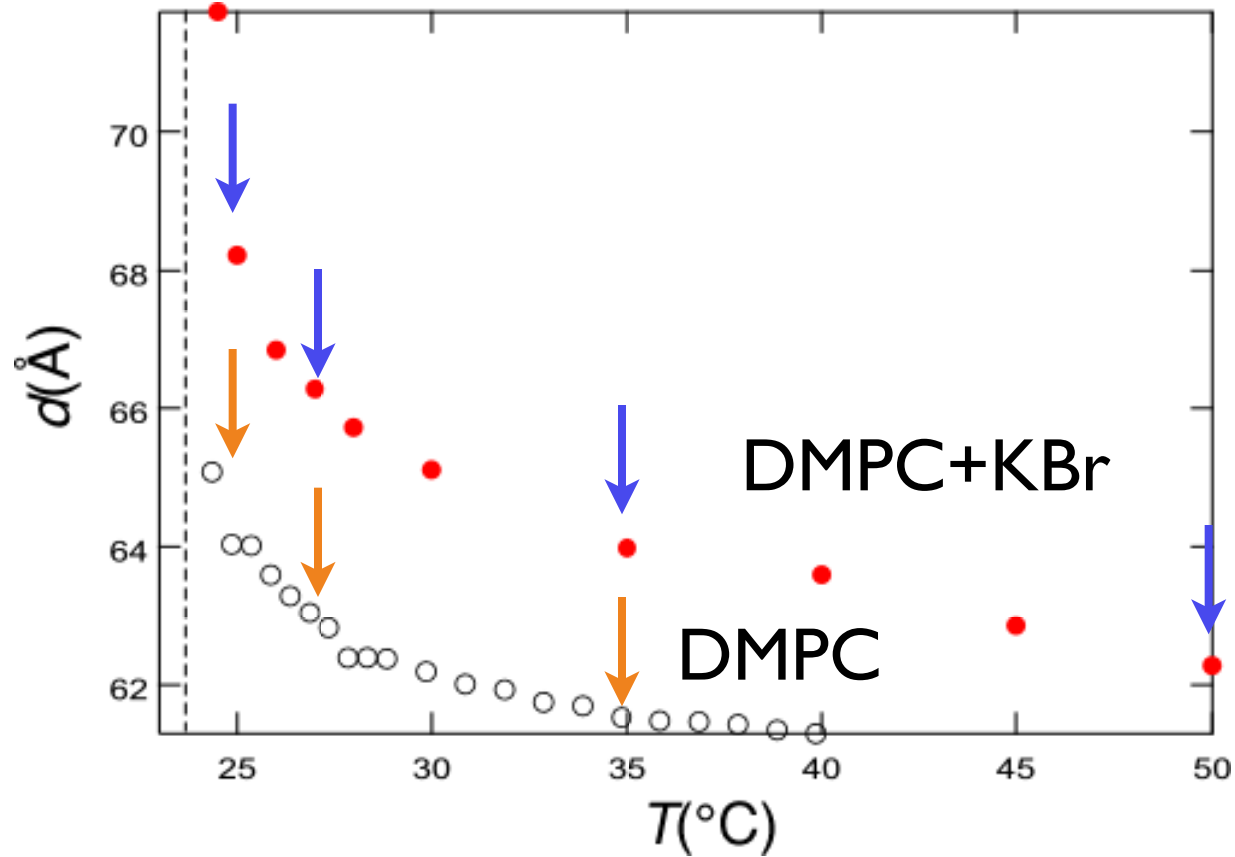
$\gamma_\alpha = 0.025$: 2D membrane

$\gamma_\kappa = 1$: $K_C \gg k_B T$

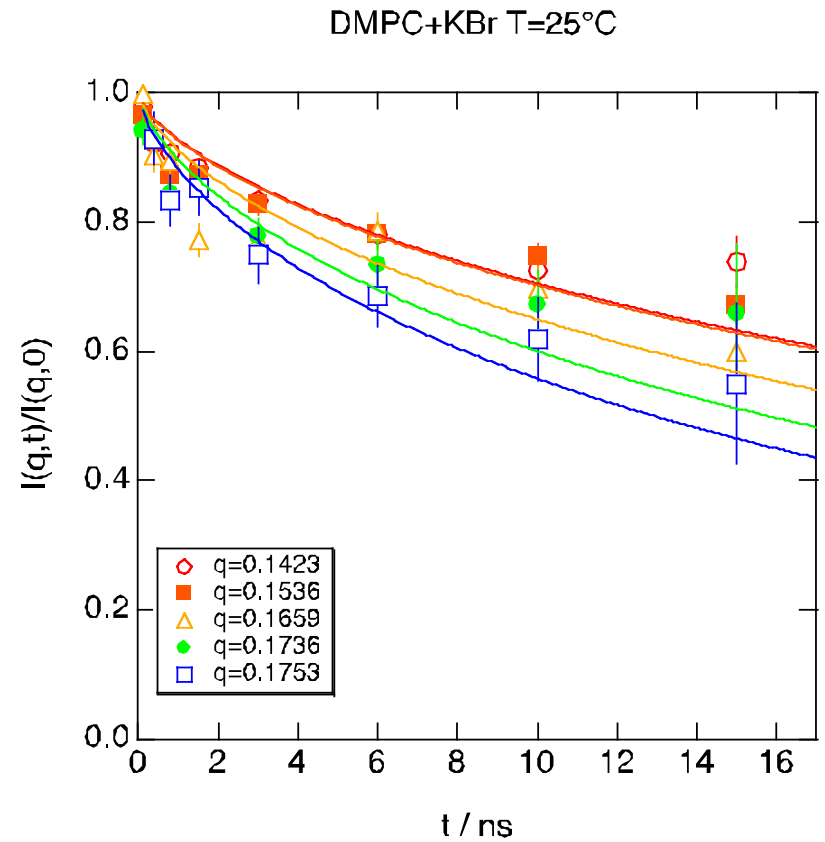
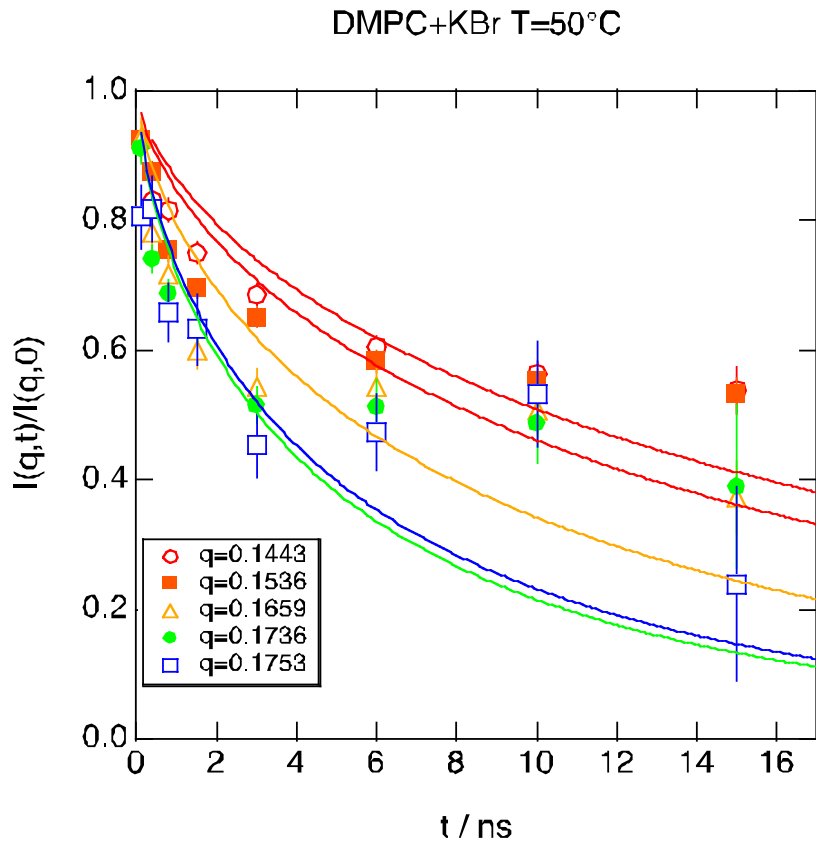
T-dependence of bending modulus



Anomalous swelling above T_M



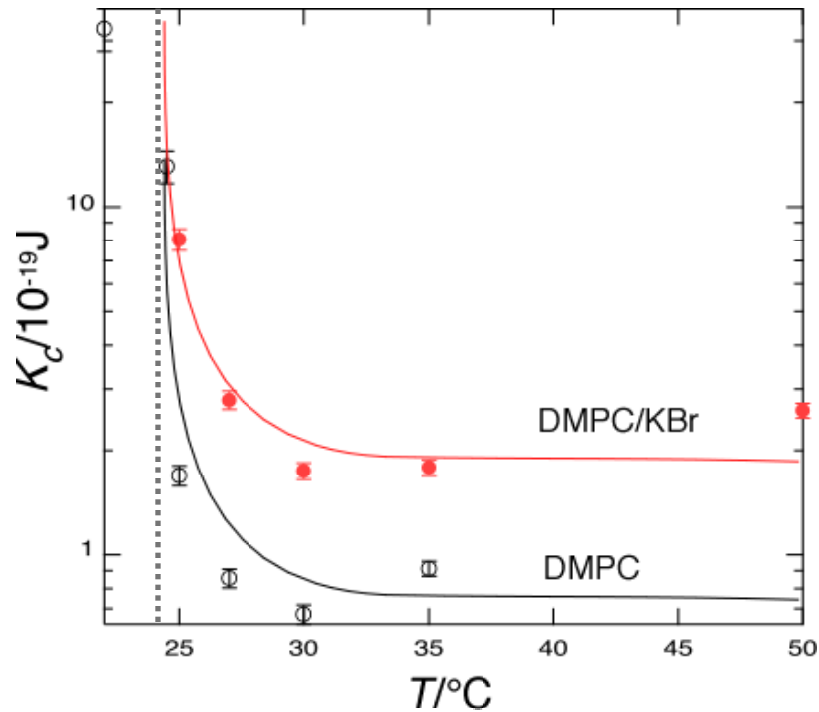
NSE results



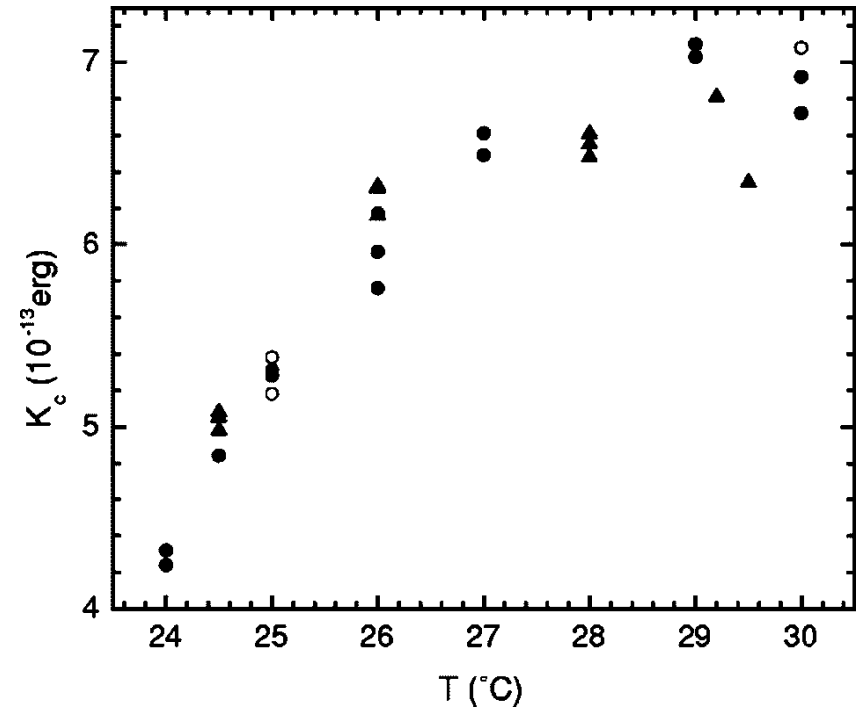
$$I(q,t)/I(q,0) = C \exp[-(\Gamma t)^{2/3}]$$

Bending modulus

NSE, 2007



SAXS, 2005

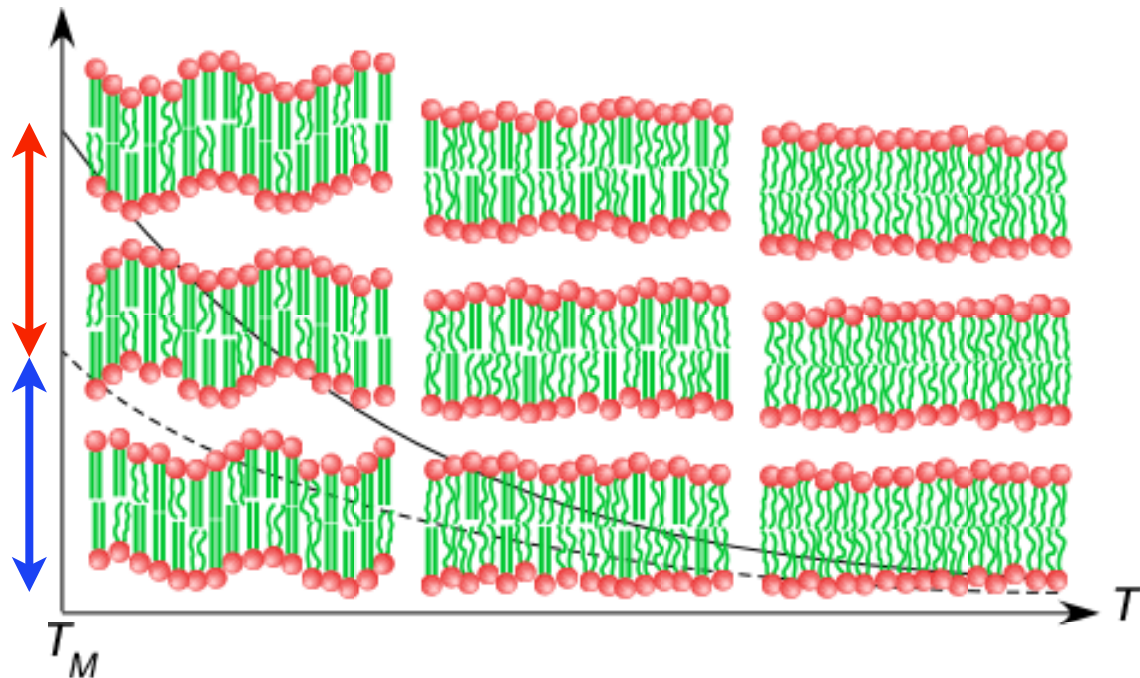


Softening \Rightarrow Thermal fluctuation increases
 \Rightarrow Repeat distance increases

Our interpretation

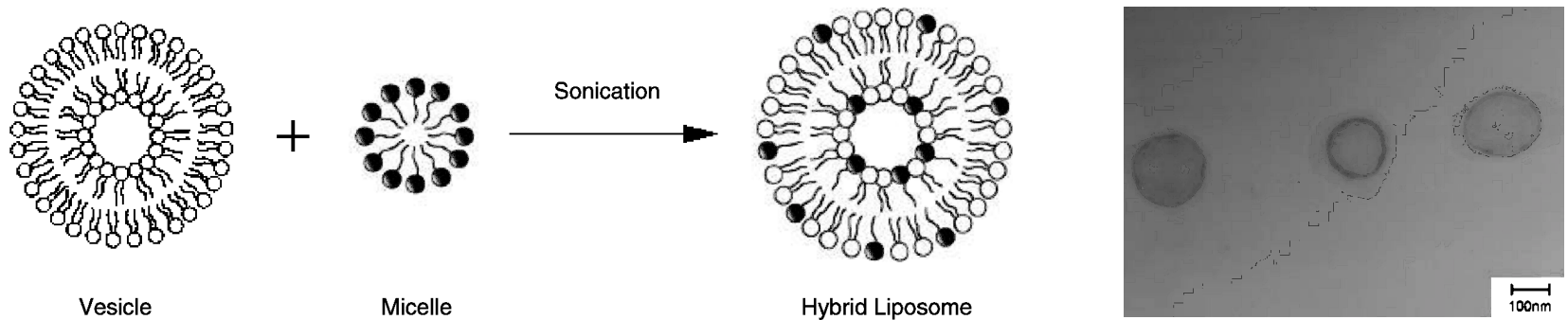
irregular stacking of
bumpy layers

thickening & hardening

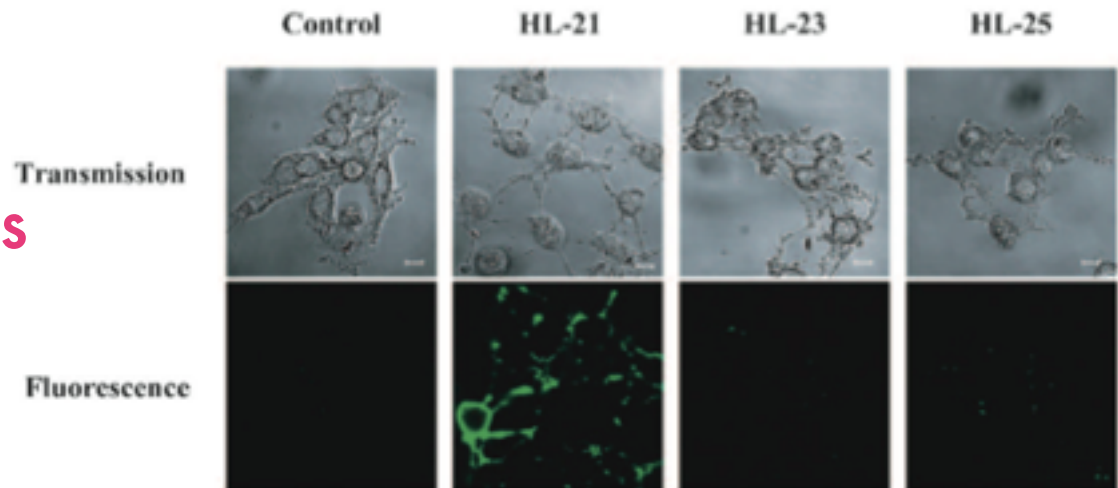


Possible application

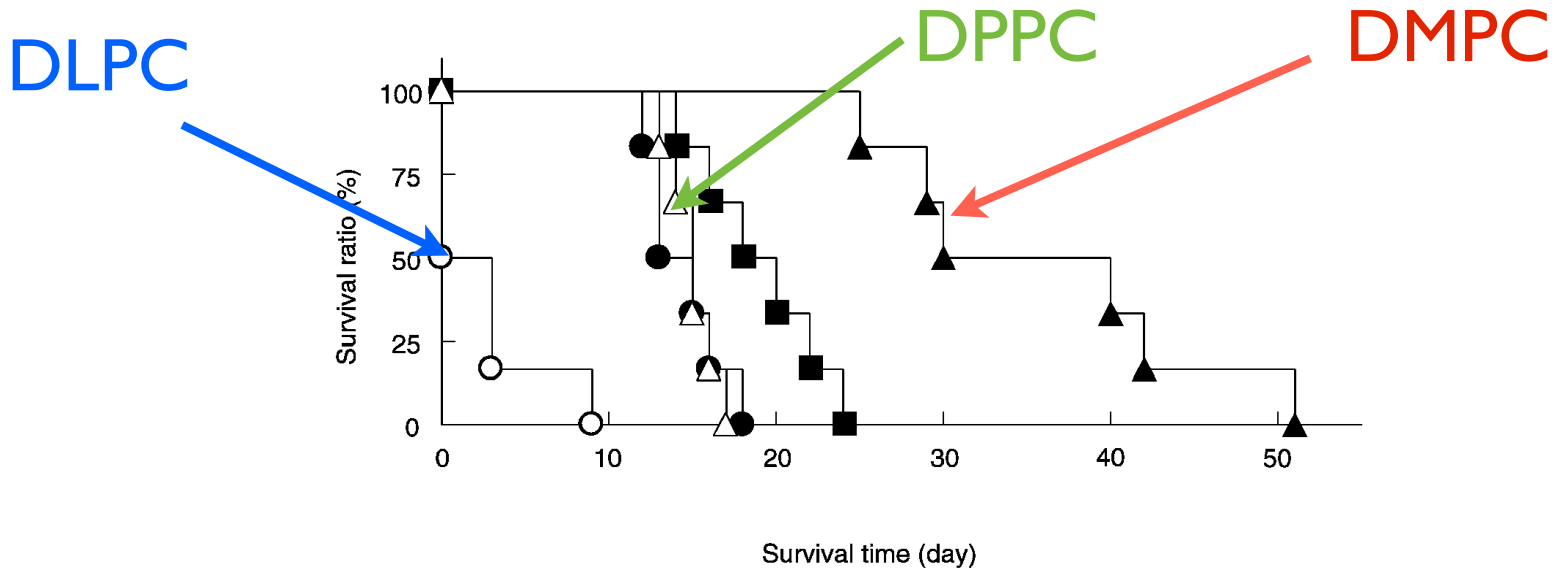
Inhibitory Effects of Hybrid Liposomes on the Growth of Tumor Cells



HL induces apoptosis
of tumor cells



Survival ratio depends on lipids



DMPC(LC phase at RT)
Soft

➤ compatible with tumor cells

DPPC(Gel phase at RT)
Hard

➤ no effect

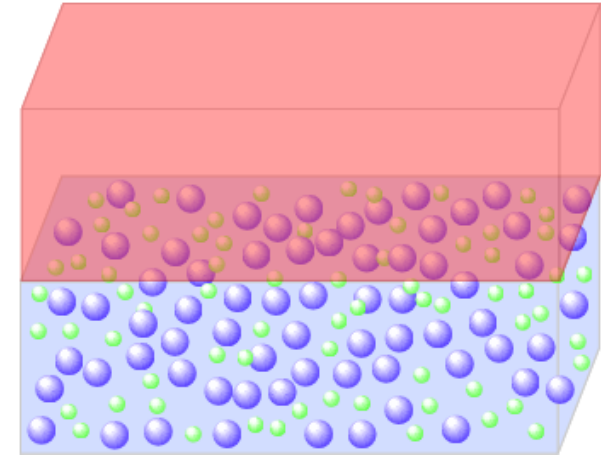
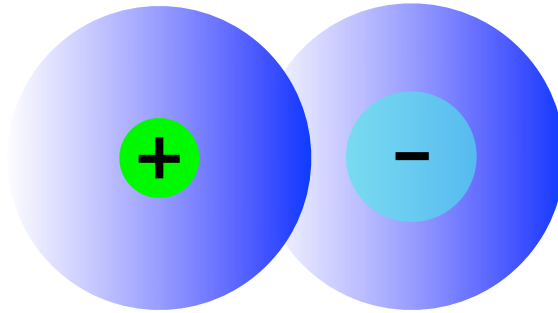
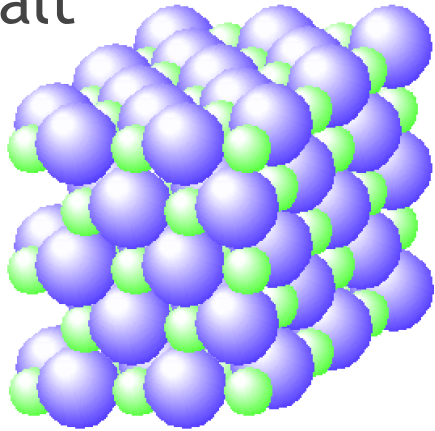
DLPC(LC phase at RT)
Foreigner

➤ kills normal cells

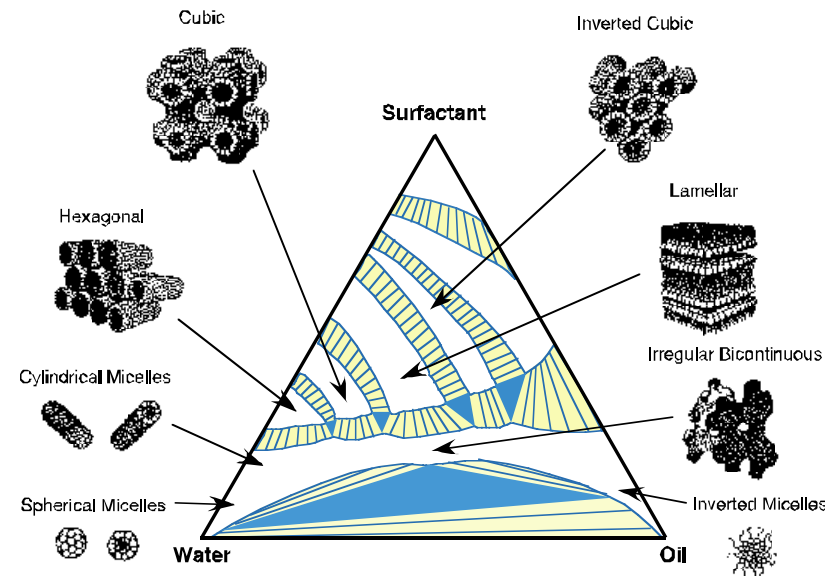
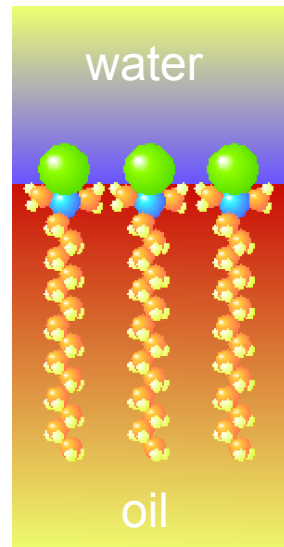
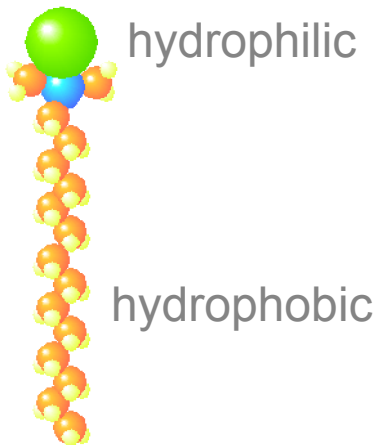
Salts

Salt vs Surfactant

Salt

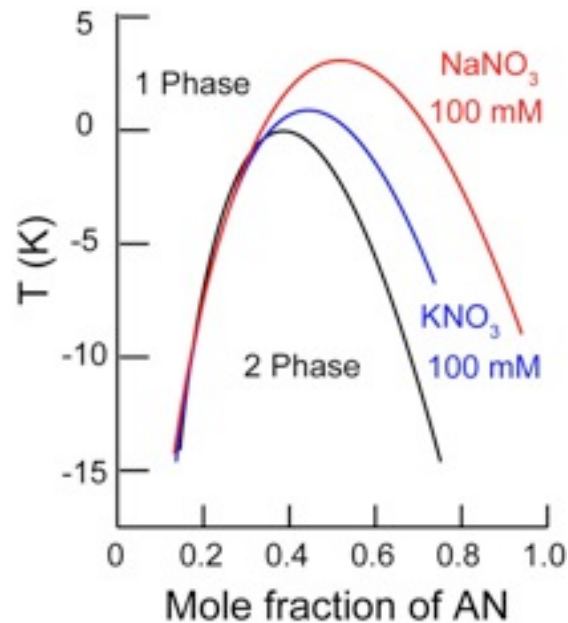


Surfactant

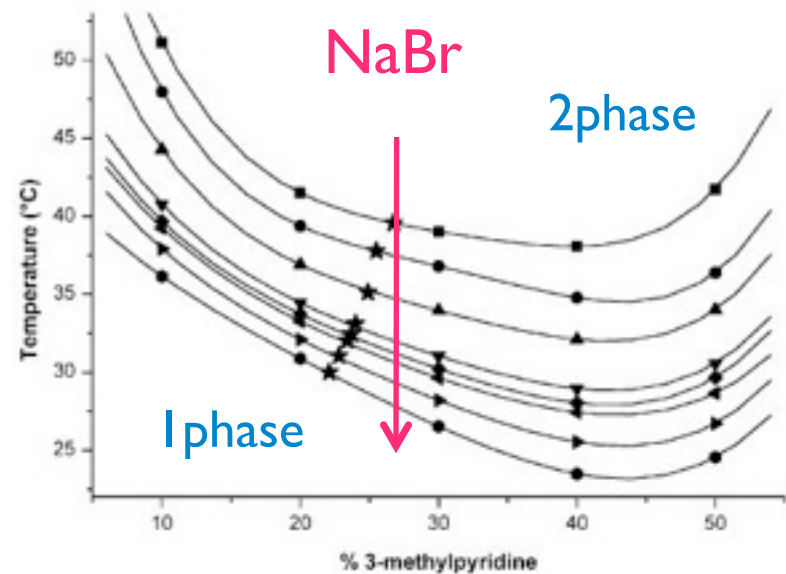


Water + Organic Solvent + Salt

water + acetonitrile (UCST)



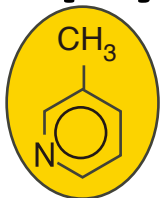
water + 3-methylpyridine (LCST)



V. Gutmann, "The Donor-Acceptor Approach to Molecular Interactions", Plenum Press (1978).

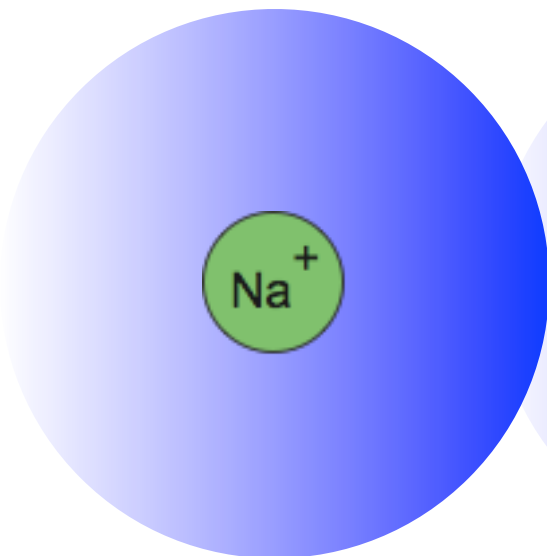
M. Wagner, et al., PCCP, **4**, 5330 (2002).

D₂O + 3-methylpyridine (3MP) + salt

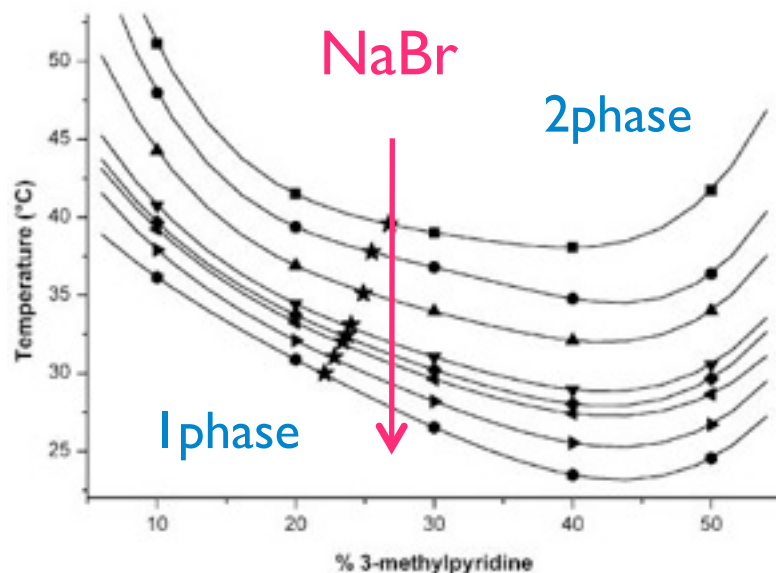
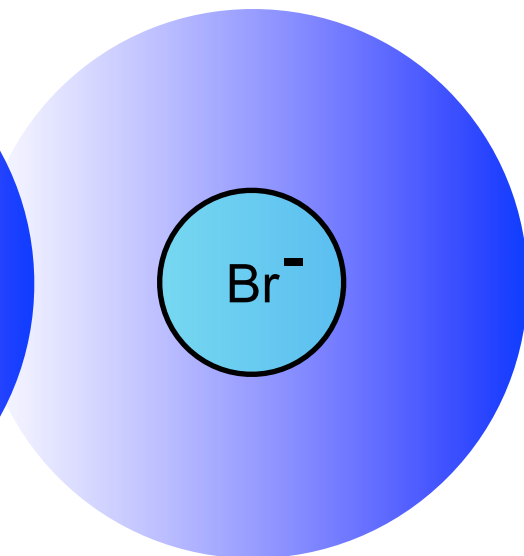


normal salt

hydrophilic



hydrophilic

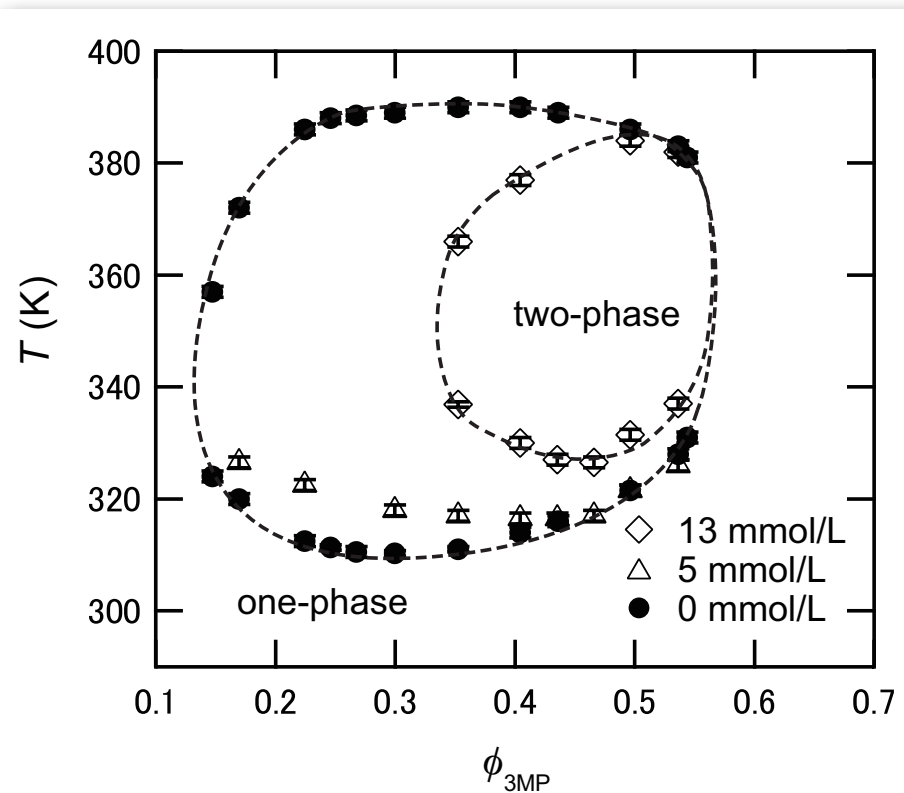
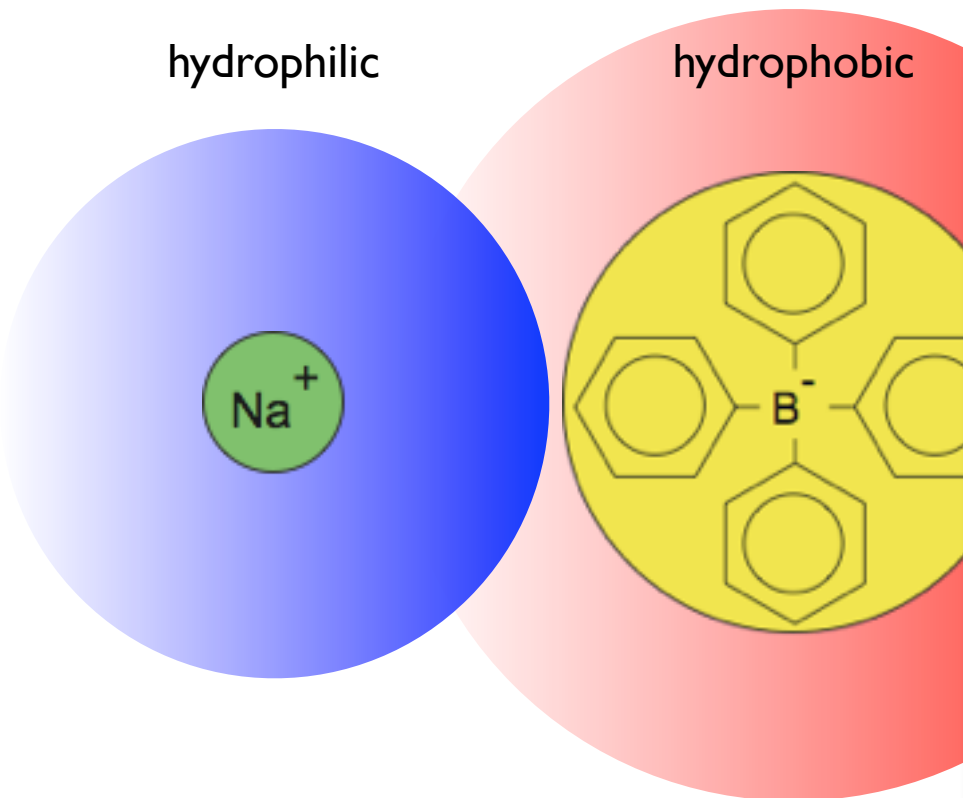


M.Wagner, et al., PCCP, 4, 5330 (2002).

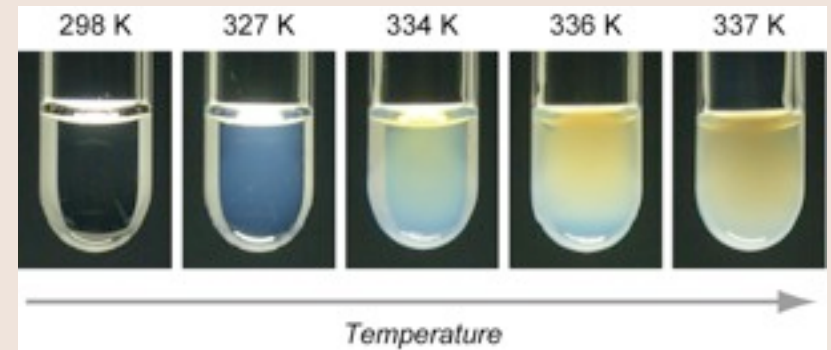
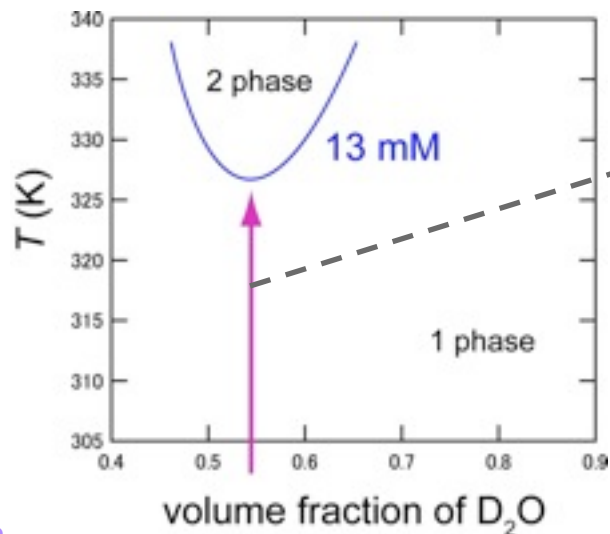
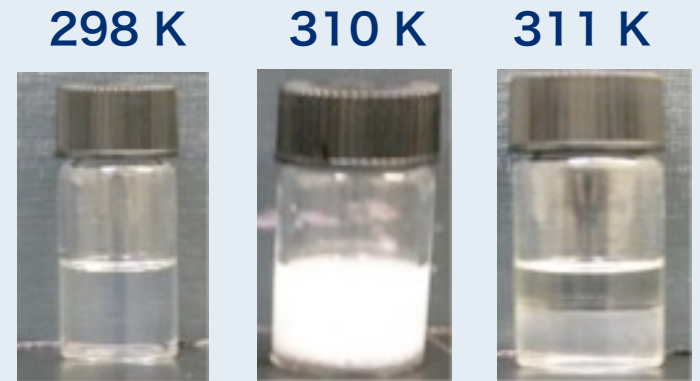
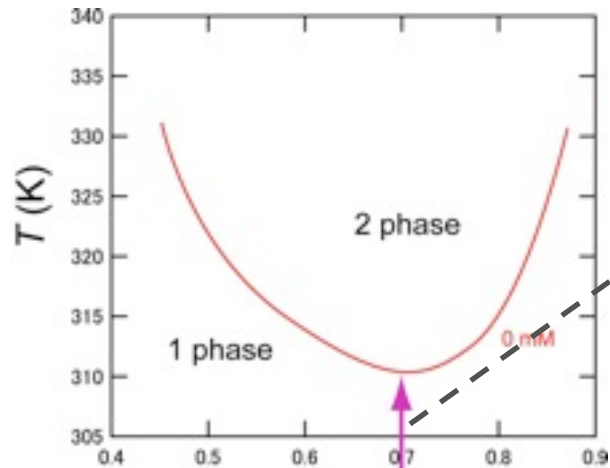
Antagonistic Salt

K. Sadakane, HS, et al. 2006-

sodium tetraphenylborate (NaBPh_4)

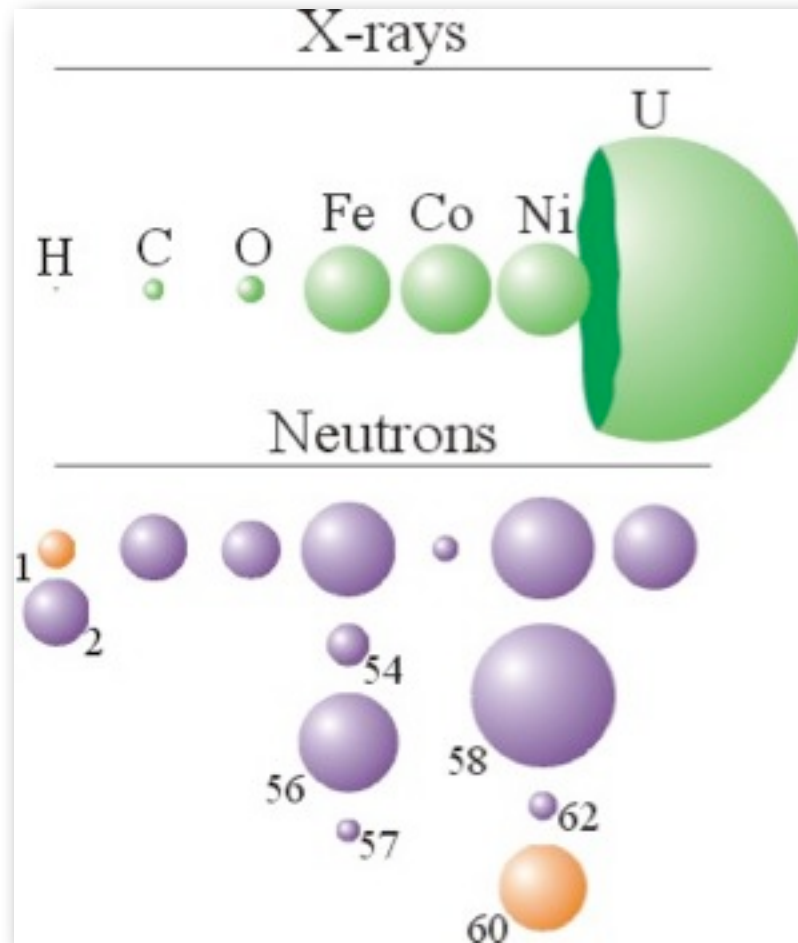


Visual inspection



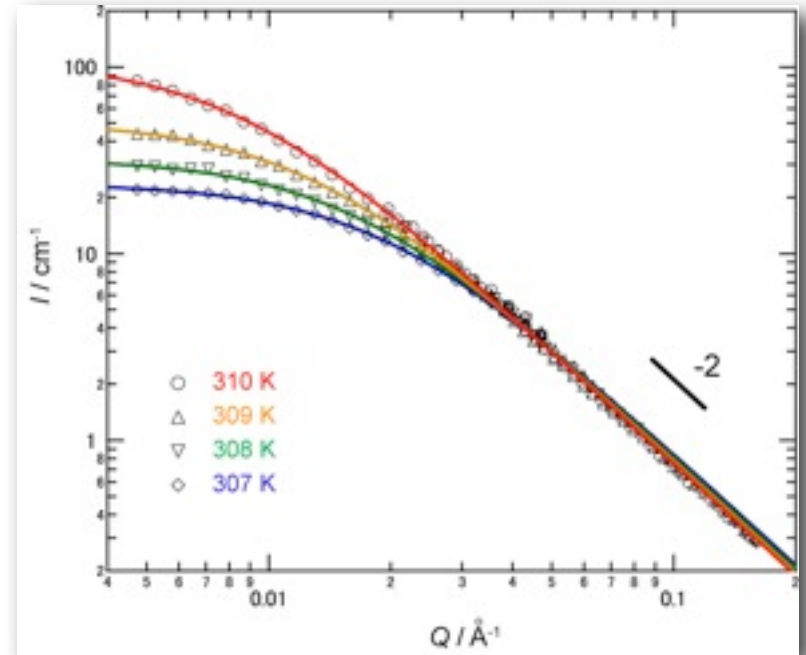
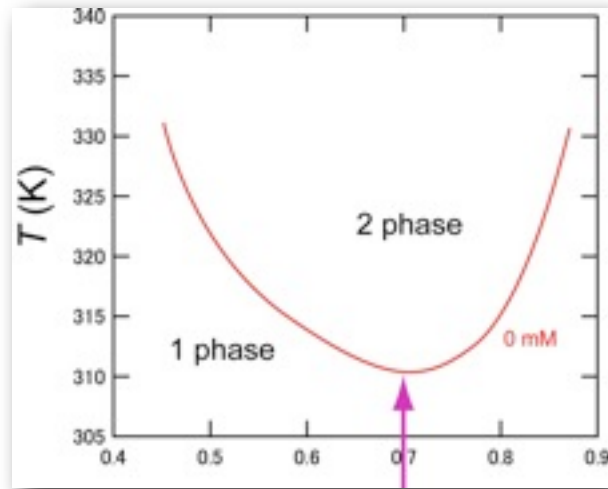
No phase separation is observed
when $NaBPh_4 > 15 \text{ mM}$

Scattering Length Densities



Small-Angle Neutron Scattering

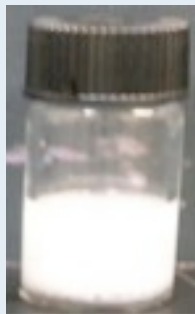
① $\text{NaBPh}_4 = 0 \text{ mM}$



298 K

310 K

311 K

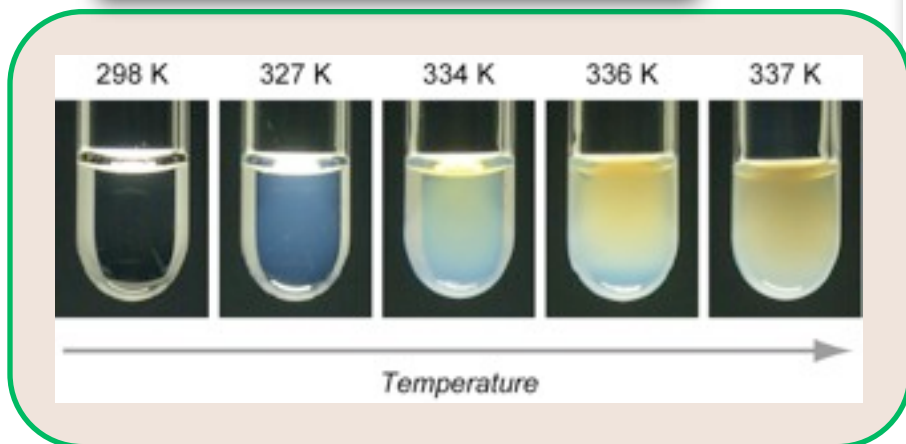
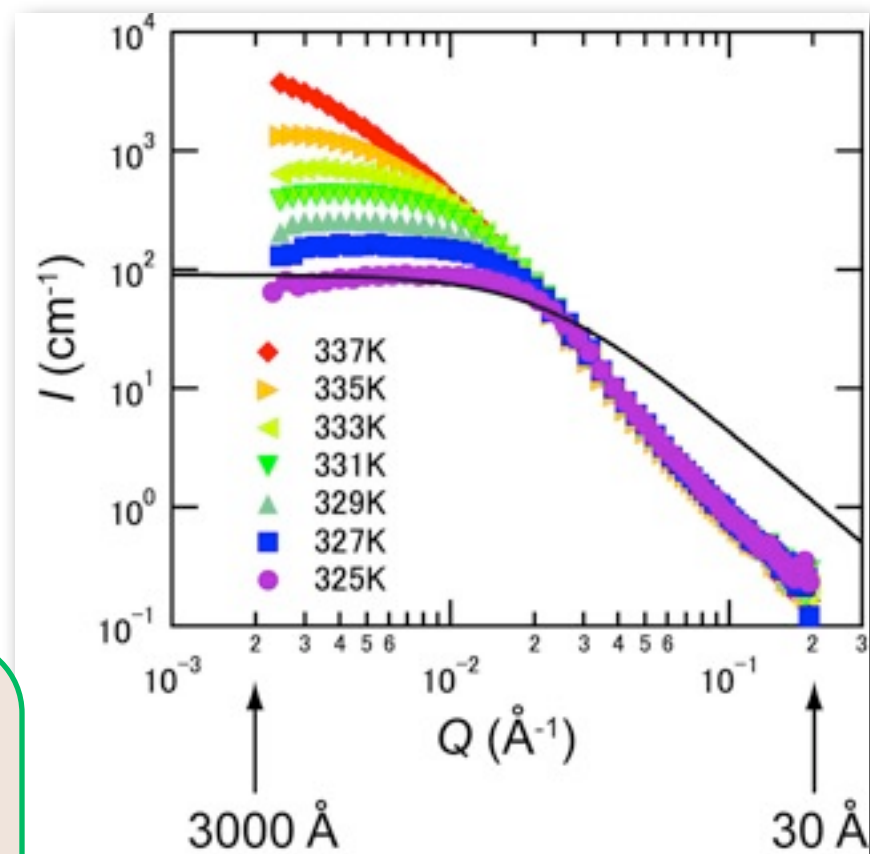
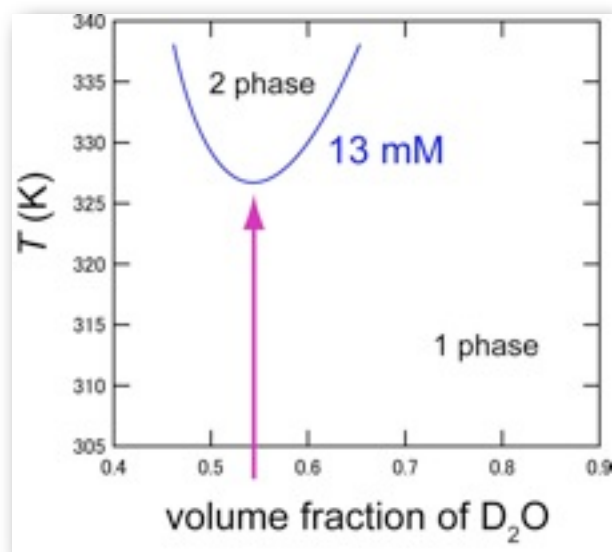


Ornstein-Zernike equation

$$I(Q) = \frac{I_0}{1 + \xi^2 Q^2}$$

Deviation from O-Z

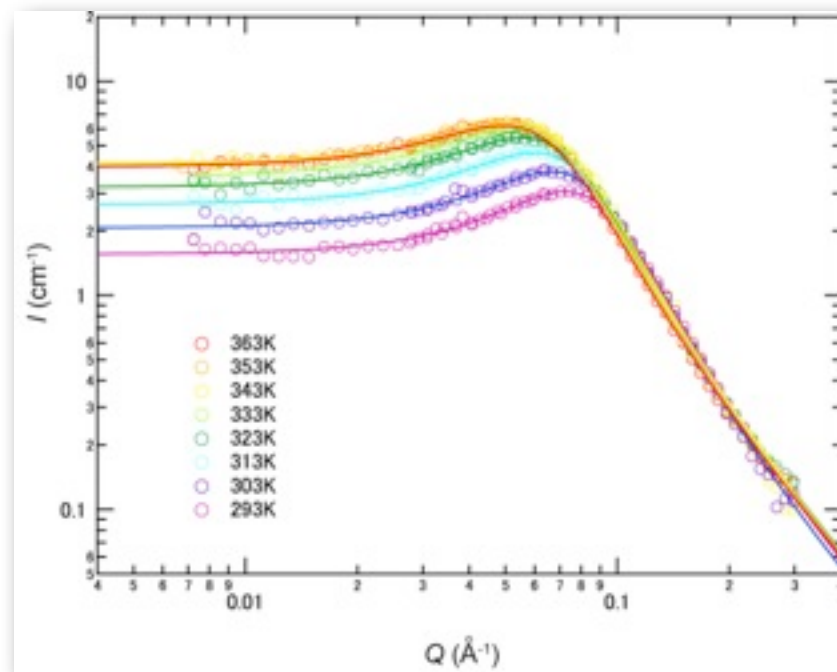
② $\text{NaBPh}_4 = 13 \text{ mM}$



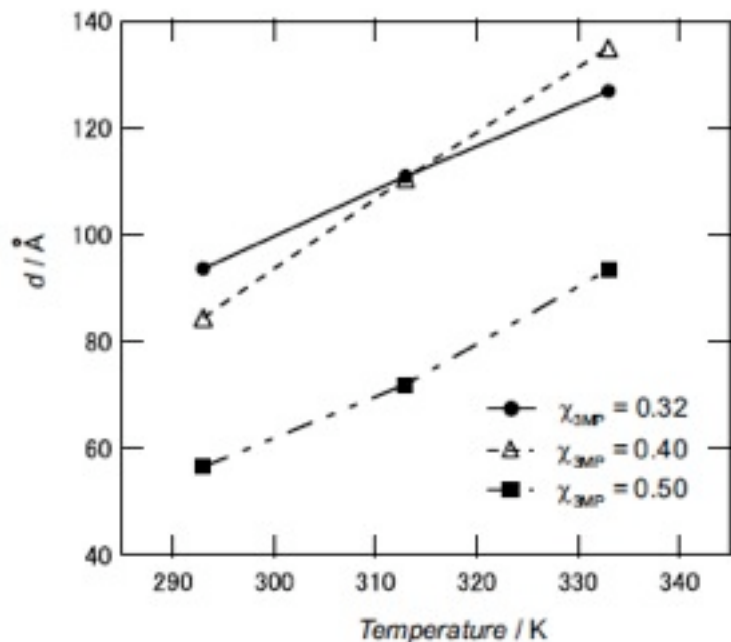
~~$$I(Q) = \frac{I_0}{1 + \xi^2 Q^2}$$~~

Charge density wave model

③ NaBPh₄ = 85 mM



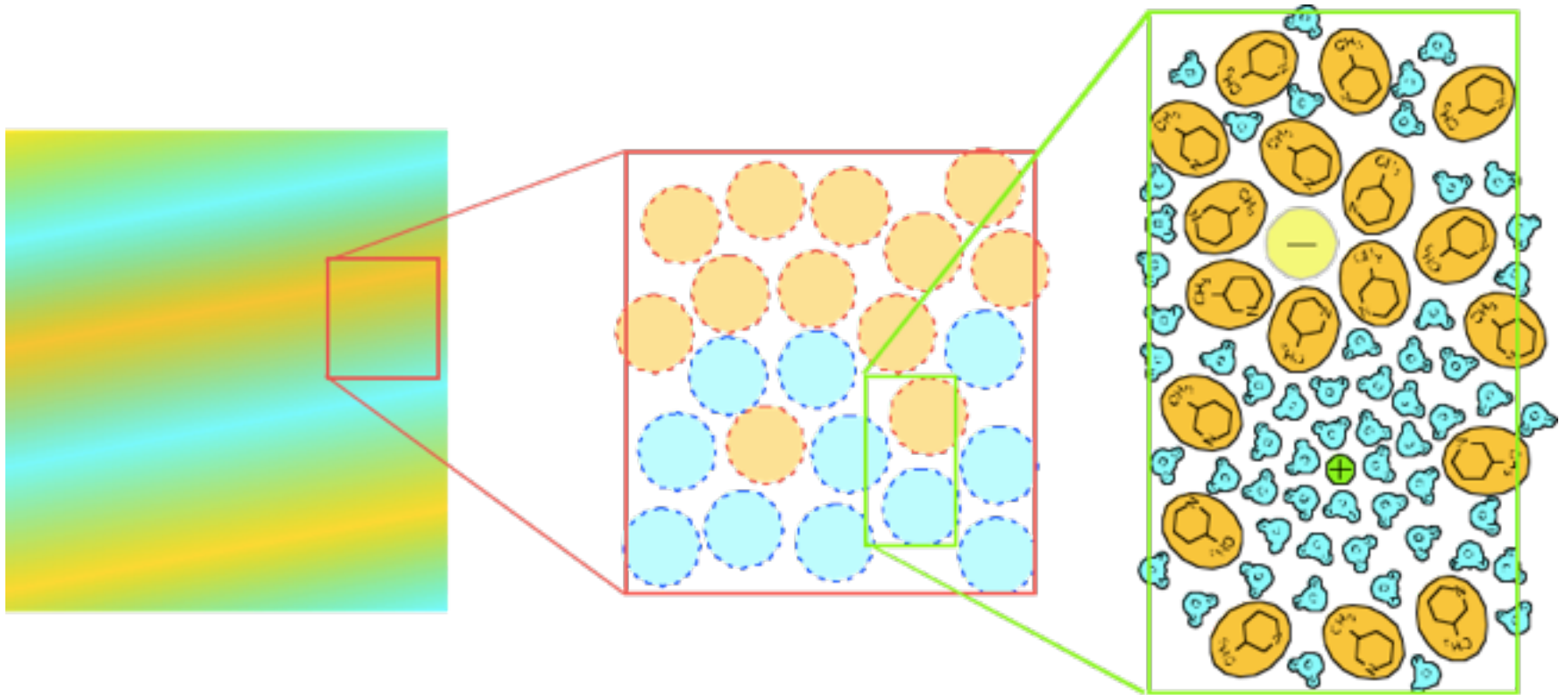
$$I_{\text{OK}}(Q) = \frac{I_0}{1 + (1 - \gamma_p^2 / (1 + \lambda^2 Q^2)) \xi^2 Q^2}$$



Onuki and Kitamura, JCP 2004

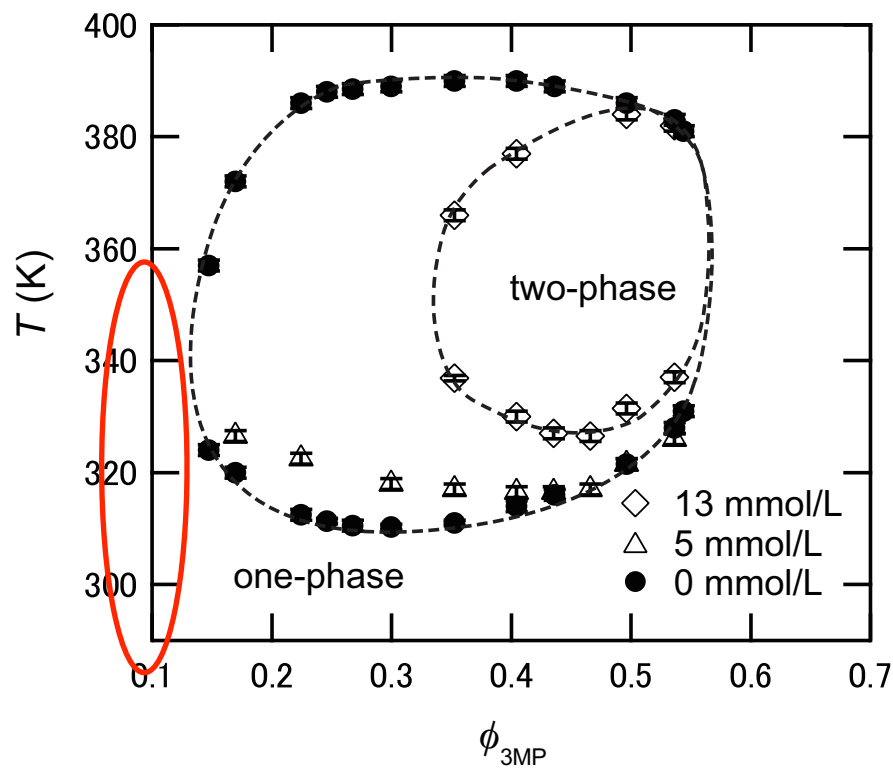
Hideki SETO (KEK, Japan)

Schematic picture

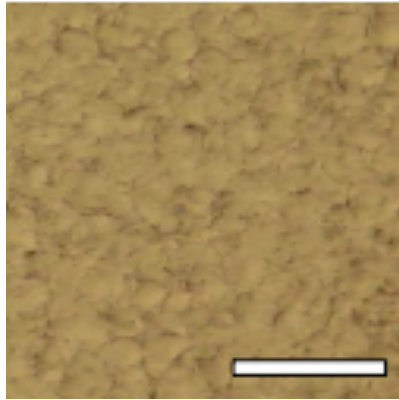


$\text{NaBPh}_4 = 85 \text{ mM}$, water rich

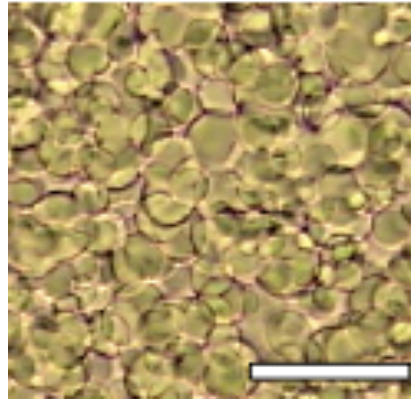
K. Sadakane, HS, et al., Phys. Rev. Lett. **103**, 167803 (2009).



Optical Microscope

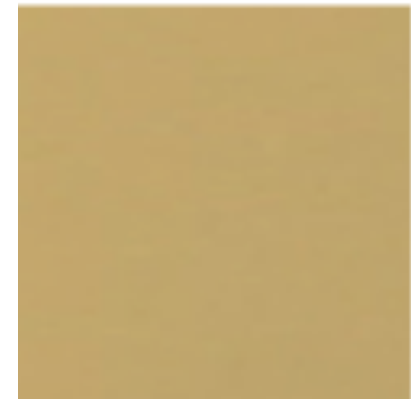


293



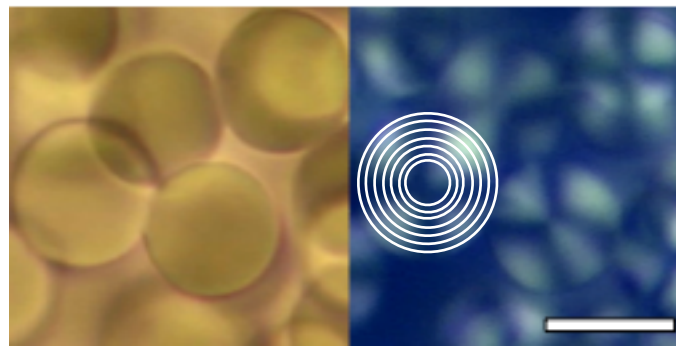
100 μm

313



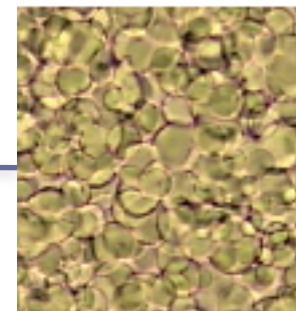
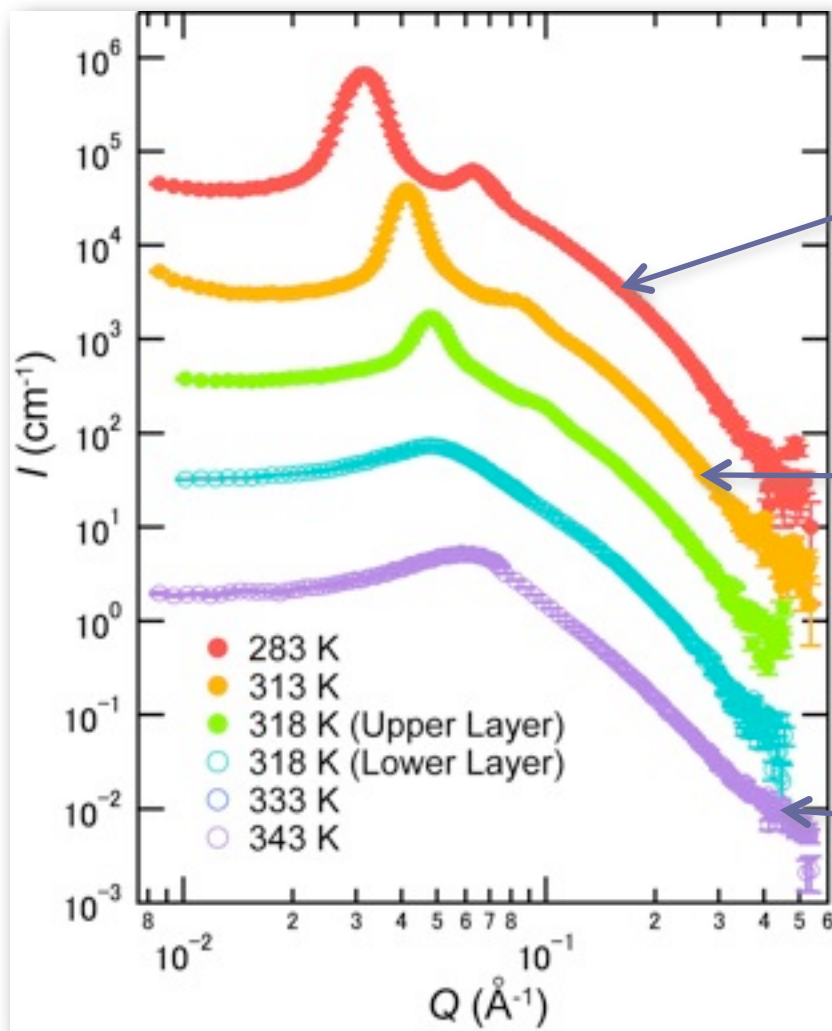
323

Temperature →



20 μm

SANS results



Model analysis

Scattering Intensity: $I(Q) = P(Q) \times S(Q)$

$$I(Q) = \frac{2\pi P(Q)S(Q)}{dQ^2}$$

$P(Q)$: Form factor of membrane

$$P(Q) = \frac{2(\Delta\rho)^2}{Q^2} \left[1 - \cos(\delta Q) e^{-\sigma^2 Q^2/2} \right]$$

$S(Q)$: Structure factor of lamellar

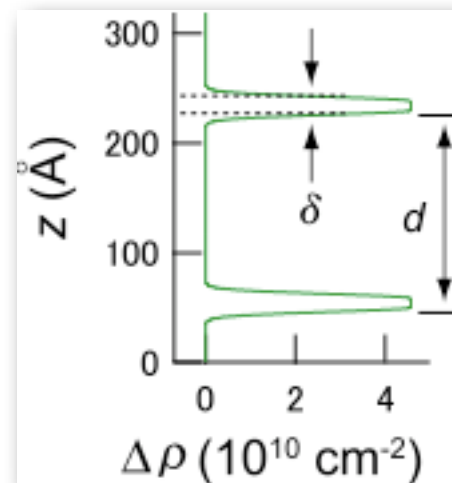
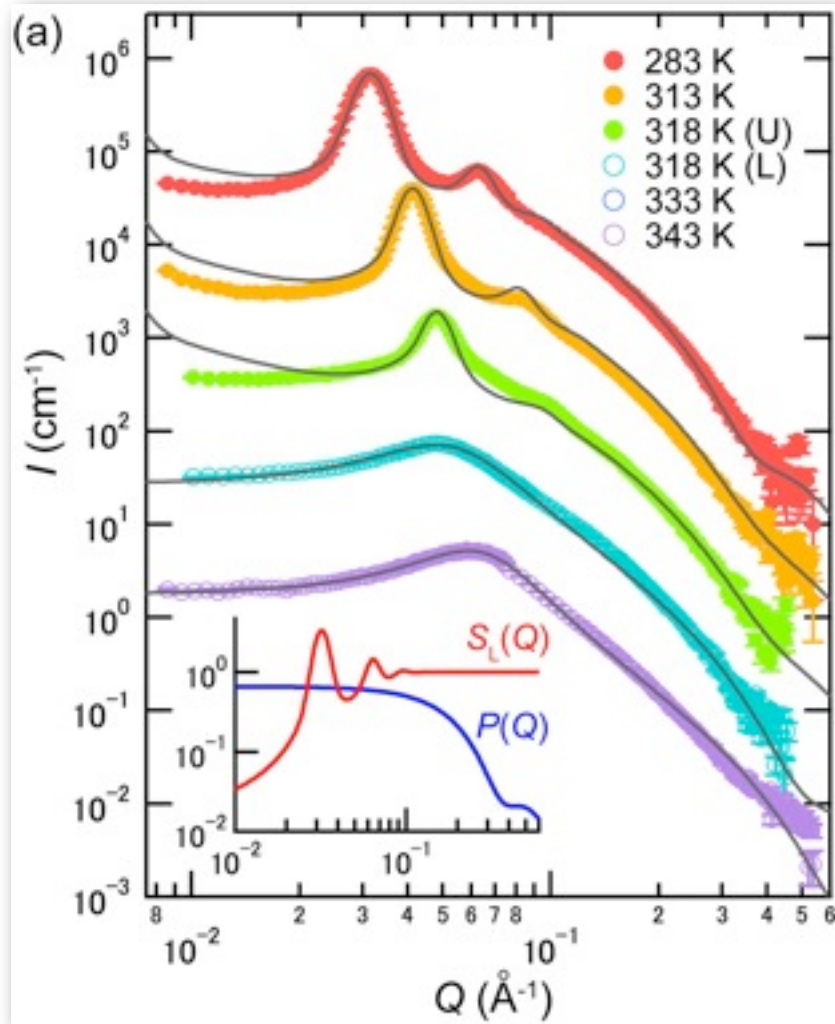
$$S(Q) = 1 + 2 \sum_{n=1}^{N-1} \left(1 - \frac{n}{N} \right) \cos\left(\frac{dnQ}{1 + 2\Delta Q^2 d^2 \alpha(n)} \right) \times \exp\left[-\frac{\Delta Q^2 d^2 n + 2d^2 \alpha(n) Q^2}{2(1 + 2\Delta Q^2 d^2 \alpha(n))} \right] \frac{1}{\sqrt{1 + 2\Delta Q^2 d^2 \alpha(n)}}$$

δ : thickness of membrane

d : repeat distance between each membrane

$\Delta\rho$: scattering contrast between membrane and bulk solution

Result of the fitting



Fit parameters

$$\delta = 13.9 \pm 0.1 \text{ (\AA)}$$

$$d = 149.7 \pm 0.6 \text{ (\AA)}$$

$$\Delta\rho = 4.90 \pm 0.01 \text{ (} 10^{10}\text{cm}^{-2}\text{)}$$

Scattering length densities

$$\text{D}_2\text{O} : \rho = 6.39 \text{ (} 10^{10}\text{cm}^{-2}\text{)}$$

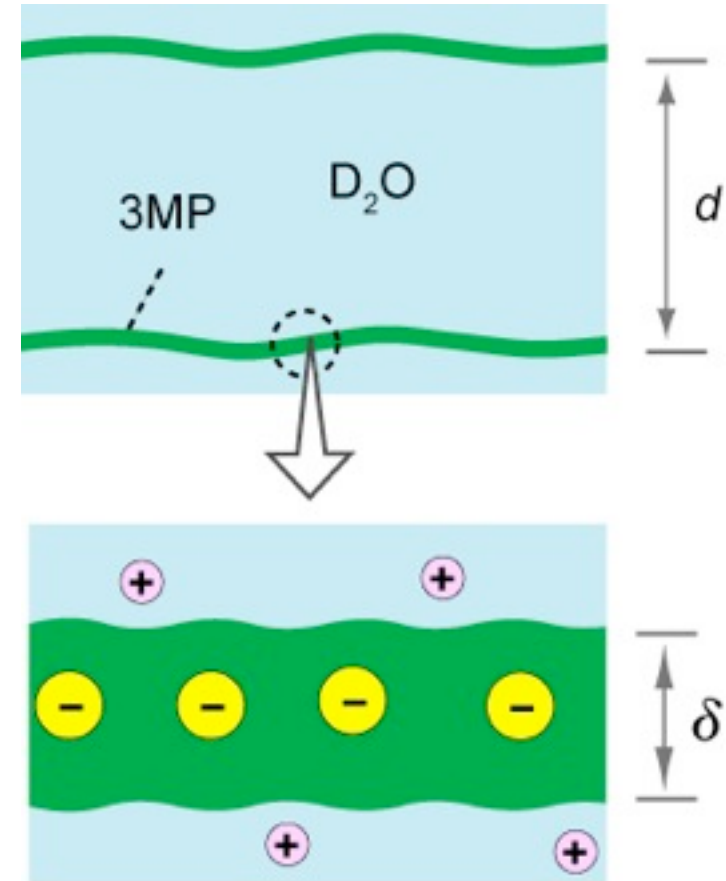
$$\text{3MP} : \rho = 1.42 \text{ (} 10^{10}\text{cm}^{-2}\text{)}$$

$$\longrightarrow \Delta\rho = 4.97 \text{ (} 10^{10}\text{cm}^{-2}\text{)}$$

Estimation of the membrane thickness

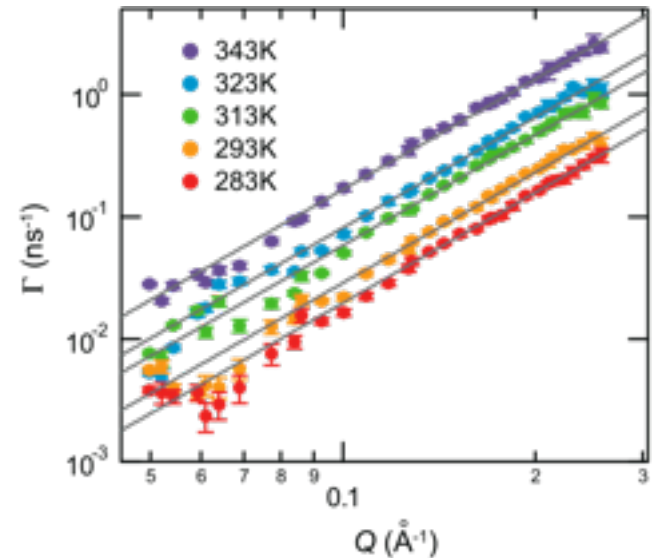
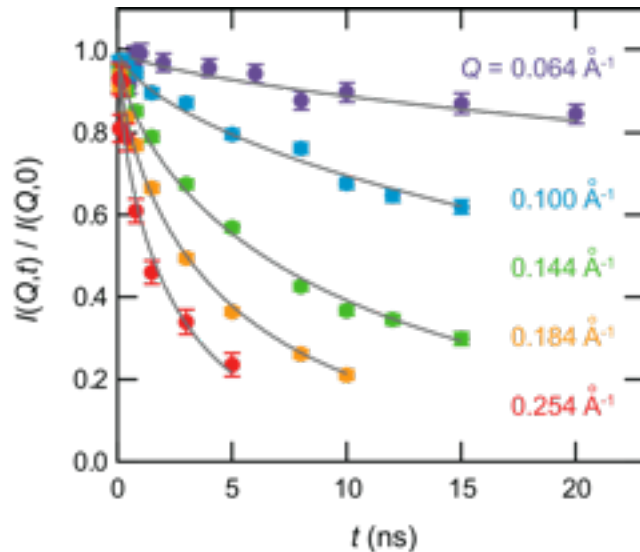
$$\delta = \varphi_{\text{3MP}} d = 149.7 \times 0.09 = 13.5 \text{ \AA}$$

\longrightarrow This value is consistent with the fitting value, 13.9 \AA.



NSE confirmed the membrane picture

$\phi_{3MP} = 0.09$, $C_{salt} = 85$ mM
 $T = 293.2$ K



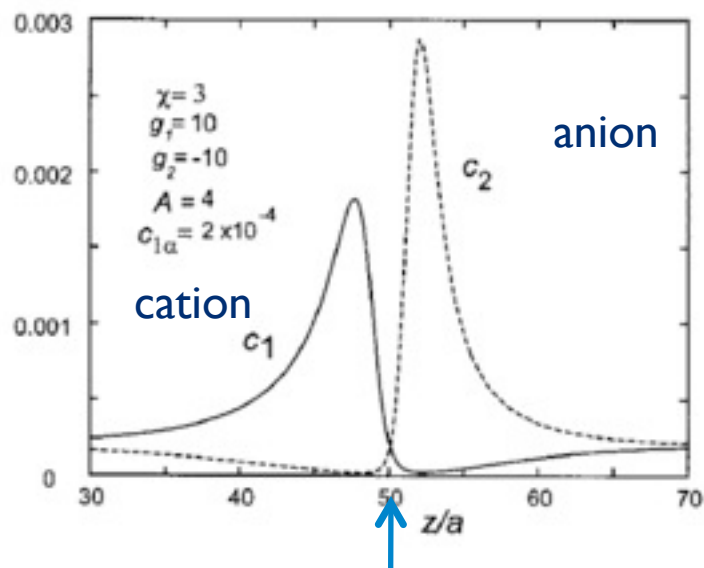
$$I(Q,t)/I(Q,0) = \exp(-(\Gamma t)^{2/3})$$

$$\Gamma = 0.025(k_B T/\kappa)^{1/2}(k_B T/\eta)Q^3$$

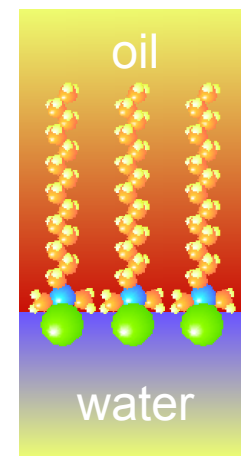
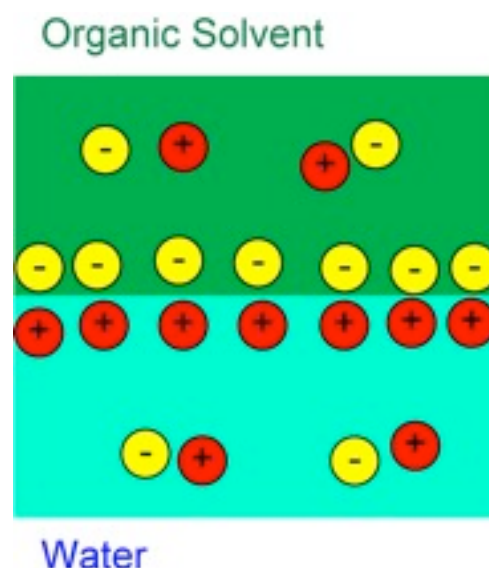
The single membrane fluctuation model (Zilman and Granek) explains well.

Behave as amphiphilic molecules

A. Onuki, J. Chem. Phys, 128, 224704 (2008).



Liquid-liquid interface



Decreasing the interfacial energy in the presence of ions

$$\Delta\gamma = -AT\sqrt{n_{\text{ion}}/\ell_B}$$

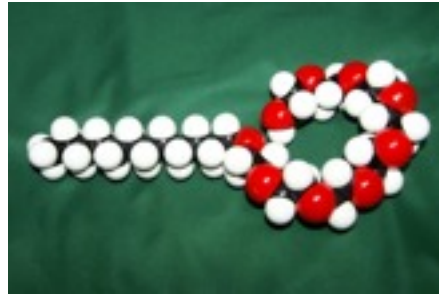
(n_{ion} : concentration of ion)

Possible application

detergent



surfactant



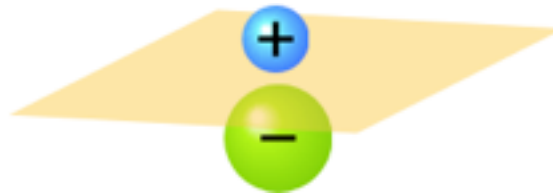
difficult to dissociate



salt



cation+anion



easy to dissociate



Neutrons in Soft Matter



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MICHIHIRO FURUSAKA

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 WILEY

\$158.00