Micellar Structure in Gemini Nonionic Surfactants from Small-Angle Neutron Scattering

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Received December 23, 2004. In Final Form: May 27, 2005

The size and shape of micelles formed by dimeric polyoxyethylene (nonionic gemini) surfactants having the structure \((C_{n-2}H_{2n-2}CH_{2}O_xH_{2}O_{m}H_{2}O_{2}H_{2}O_5\text{CH}_{3})_{2n}\) with alkyl and ethoxy chain lengths ranging from \(n = 12-20\) and \(m = 5-30\) have been determined using small-angle neutron scattering (SANS). The surfactants are polydisperse in the hydrophilic groups but otherwise analogous to the widely studied monomeric poly(oxyethylene) alkanols. We find that longer ethoxylated chains are needed to confer solubility on the gemini surfactants and that these chains in the hydrophilic corona around the alkyl core of the micelles are reasonably well described as a homogeneous random coil in a good solvent. Spherical micelles are formed by the surfactants with the longest ethoxylated chains. Shorter chains lead first to rods and ultimately to a vesicle dispersion. These solutions exhibit conventional cloud point behavior, and on warming, a sphere to rod transition can be observed. For the \(n = 20\) and \(m = 15\) surfactant, this shape transition is accompanied by a striking increase in viscosity at low concentration and gelation at higher concentrations.

![Figure 1: Generic structure of nonionic gemini surfactants, \(\text{Gem}_m\text{E}_n\), used in this study. \(m = 1/2(x + y)\) is the average degree of ethoxylation per alkyl chain.](image)

Introduction

In recent years there has been increasing interest in dimeric (gemini) surfactants, which consist of two conventional surfactants joined by a spacer at or near the headgroup, as they exhibit much lower critical micelle concentrations (CMCs) than can be achieved by conventional surfactants. Cationic bis(quaternary ammonium) surfactants have been most extensively studied, and the dependence of their properties on systematic variation of alkyl chain length, spacer length and type, and electrolyte concentration have been described. Small-angle neutron scattering has recently been employed to reveal micelle structure in a variety of gemini surfactant solutions, and recently, an unusual nonionic gemini has been examined. In this work, we examine a series of very hydrophobic nonionic gemini surfactants with the structure \((C_{n-2}H_{2n-2}CH_{2}O_xH_{2}O_{m}H_{2}O_5\text{CH}_{3})_{2n}\), abbreviated \(\text{Gem}_m\text{E}_n\), where \(m\) is the average number of ethylene oxide units per headgroup, shown in Figure 1. Their preparation and CMCs have been described previously. The present work is concerned with how the micelle morphology and isotropic solution structure of these gemini surfactants depend on the ethoxylation number (\(m\)) and alkyl chain length (\(n\)), concentration, and temperature and how these trends compare to conventional nonionic surfactants.

Alkyl chain lengths are varied between 12 and 20 with a fixed hexamethylen ether spacer. Ethoxylation was carried out by ring-opening polycondensation, leading to a distribution of ethoxy chain lengths about an average \(m = 5, 10, 15, 20,\) or 30. The most hydrophobic surfactants, those with the smallest headgroups, \(\text{Gem}_{12}\text{E}_5, \text{Gem}_{14}\text{E}_5,\) and \(\text{Gem}_{20}\text{E}_{10}\), are all insoluble at room temperature, forming a dispersed lamellar phase (vesicles) in water, and were not investigated in this work. The remaining surfactants all have extremely low CMCs, in the range \((1.5-7) \times 10^{-7}\) M.

Self-assembly structures, and particularly systematic trends in micelle morphology, can be rationalized using the surfactant packing parameter,\(\psi \equiv \frac{\pi dS}{\ell v}\), where \(\psi\) is the volume of a surfactant hydrocarbon tail, \(a_0\) is the effective area per headgroup, and \(\ell\) is the fully extended alkyl chain length. \(\psi\) forms an upper bound on the radius of a spherical or cylindrical micelle, or the half-thickness of a bilayer. Spherical micelles form for a packing parameter less than or equal to one-third, rodlike micelles form for a packing parameter between one-third and one-half, and bilayers form for a packing parameter between one-half and one.

For conventional or gemini nonionic surfactants, both \(\ell\) and \(\psi\) increase linearly with alkyl chain length,\(^4\) and changes in degree of ethoxylation alter \(a_0\). Thus, as ethoxylation number, and hence \(a_0\), is increased, the micelle morphology is expected to change toward higher curvature: from planar to rodlike to spherical. Increasing alkyl chain length causes a slight decrease in aggregate curvature.


As the temperature is increased toward the cloud temperature, many conventional nonionic surfactants exhibit micellar growth.7–9 The exact nature of micelle behavior in this region has not been fully explained but it is widely believed that as the cloud temperature is approached the polyoxyethylene headgroups begin to dehydrate,10 which decreases the area occupied, $d_0$. This leads to a sphere-to-rod transition, and some have proposed a rod to branched-rod or network transition near the cloud temperature.11,12 Because of their high hydrophobicity, these nonionic micelles display some unusual viscosity behavior accompanying the morphology change as the cloud point is approached.

**Materials and Methods**

The nonionic gemini surfactants, Gem$E_m$, were synthesized as described previously4 with the structure (Cn−2H2n−3 CHCH2(OCH2CH2)n(OH)(CH2)6). Ethoxylation is carried out as a polycondensation, leading to a distribution of hydrophilic ethoxy chain lengths about a mean, $m$, per alkyl tail (see Figure 1). The surfactants investigated here are Gem$_{12}E_{10}$, Gem$_{14}E_{10}$, Gem$_{14}E_{15}$, Gem$_{20}E_{15}$, Gem$_{20}E_{20}$, Gem$_{20}E_{30}$, and Gem$_{25}E_{25}$. Surfactants with smaller ethoxylation number in each series were found to be insoluble at room temperature.

$D_2O$ was obtained from Aldrich (>99%). Solubility and cloud temperatures of 1 wt % solutions in $D_2O$ and $H_2O$ were measured by either visually observing or spectroscopically recording (at 500 nm with a UV–Vis spectrometer) the turbidity versus increasing temperature. The cloud temperature was taken to be the temperature where the solution first becomes significantly turbid. Solutions for viscosity studies were prepared in water filtered through a Milli-Q purification system. Relative viscosities were measured using a capillary viscometer. The temperature was maintained to ±0.1 °C in a water bath.

Small angle neutron scattering (SANS) was performed on the NG3 line at the Center for Neutron Research at NIST, Gaithersburg, Maryland. Neutrons with an average wavelength of 6.0 Å and a $q$-offset by 0.2 m and scattering collected at two distances (1.4 and 6.50 mm2 2D detector with 128 elements. The detector was positioned through a Milli-Q purification system. Relative viscosities were maintained to 0.1 °C in a water bath.

**Results and Discussion**

**Dilute Solution Structure.** Table 1 summarizes the solubilities and cloud temperatures for 1 wt % Gemini nonionic surfactants in $H_2O$ and $D_2O$. Like conventional nonionic surfactants, the solubilities of these gemini surfactants in water are very sensitive to the alkyl and poly(oxyethylene) chain lengths.15 Gem$_{12}E_{10}$, Gem$_{14}E_{10}$, and Gem$_{14}E_{15}$ all exhibit accessible cloud points on warming. Gem$_{14}E_{20}$, Gem$_{14}E_{25}$, Gem$_{20}E_{20}$, and Gem$_{25}E_{25}$ all have cloud temperatures above 100 °C in both $H_2O$ and $D_2O$. The cloud point decreases with increasing alkyl chain length and increases with increasing degree of ethoxylation. The lowering of the cloud temperature in $D_2O$ relative to $H_2O$ is similar to results reported previously for conventional nonionic surfactants.16

Figure 2 shows SANS spectra for all of the soluble gemini surfactants at 1 wt % and 25 °C in $D_2O$ showing fits to monodisperse core–shell spheres or rods (see Table 3). The solid line shows the $Q^{-1}$ scattering behavior expected for long, rigid rodlike micelles.19

![Figure 2. SANS spectra of 1 wt % solutions of Gem$_{12}E_{10}$ (a), Gem$_{14}E_{10}$ (b) and Gem$_{14}E_{15}$ (c) at 25 °C in $D_2O$ showing fits to monodisperse core-shell spheres or rods (see Table 3). The solid line shows the $Q^{-1}$ scattering behavior expected for long, rigid rodlike micelles.19](https://example.com/figure2.png)

**Table 1. Cloud Temperatures (°C) for 1 wt % Gemini Nonionic Surfactants with Different Hydrophobe Lengths ($n$) and Average Degrees of Ethoxylation ($m$) in $D_2O$ and $H_2O$ (in parentheses)**

<table>
<thead>
<tr>
<th>$n$</th>
<th>10</th>
<th>15</th>
<th>20</th>
<th>30</th>
</tr>
</thead>
<tbody>
<tr>
<td>12</td>
<td>59 (67)</td>
<td>&gt;100</td>
<td></td>
<td></td>
</tr>
<tr>
<td>14</td>
<td>46 (57)</td>
<td>&gt;100</td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>81 (83)</td>
<td>&gt;100</td>
<td>&gt;100</td>
<td></td>
</tr>
</tbody>
</table>

* Gem$_{20}E_{10}$ is insoluble at room temperature, hence the cloud points could not be determined.4

$I(Q) = (N_p \Delta \rho)^2 P(Q)S(Q)$

where $N_p$ is the number density of micelles, $\Delta \rho$ is the scattering contrast, and $Q = 4\pi\lambda / \sin(\theta)$, where $2\theta$ is the scattering angle and $\lambda$ is the neutron wavelength.

Separation into form and structure factors is only exact for monodisperse spheres but is often used as an approximation for polydisperse spheres or slightly elongated particles. It is certainly not valid for highly elongated micelles where interactions depend on orientation. For nonionic surfactants, we assume as a starting point that intermicellar interactions can be neglected at a concentration of 1 wt % ($S(Q) = 1$), so that the scattering spectrum is described simply by considering $P(Q)$.

The radius of gyration, $R_G$, obtained from a series expansion of $P(Q)$ about $Q = 0$ is of all the soluble Gemini nonionics studied are listed in Table 2. In the absence of interactions, this gives a good overall measure of micelle dimensions independent of any assumptions about micelle shape. $R_G$ may be compared with the radius of a spherical or cylindrical hydrocarbon core, which is upper bounded by the fully extended alkyl chain length of the surfactant: 16.7 Å for Gem$_{32}$, 19.2 Å for Gem$_{42}$, and 26.8 Å for Gem$_{52}$. In all cases, $R_G$ is greater than expected for the core alone, and the results fall into two classes. Surfactants with longer ethylene oxide chains have radii of gyration around twice the expected core radius and are consistent with spherical micelles. These results compare well with reported radii of gyration for spherical micelles of $C_{12}E_{20}$ (Brij-35) of 30 Å$^2$ and $C_{10}E_{20}$ (Brij-55) of 30.5 ± 0.6 Å$^2$. Those with the shortest ethylene oxide chains, Gem$_{2}E_{10}$, Gem$_{3}E_{15}$, and particularly Gem$_{3}E_{20}$, have much larger $R_G$ suggesting instead eccentric or elongated micelles.

For homogeneous spheres, $R_G$ can be used to obtain the overall sphere radius using $R_S = (5/3)^{1/2}R_G$. However poly(oxyethylene) surfactants are known to form micelles with a hydrocarbon core and a corona or shell of hydrated ethylene oxide chains, which have different neutron scattering length densities. The core is usually regarded as homogeneous and hydrocarbon-like, whereas in the present systems the thickness of the surrounding ethylene oxide shell is comparable with the core radius and its scattering length density may vary radially.

SANS spectra of 1 wt % surfactant solutions in D$_2$O were fitted to core-shell sphere and rod structural models with pure (hydrogenous) hydrocarbon cores and a (D$_2$O) hydrated polyoxyethylene shell with a uniform scattering length density. In these surfactants with high degrees of ethoxylation, it is possible that the headgroups further from the core are more hydrated, so that the scattering length density of the shell increases from the hydrophobic core to the outer size of the micelle. To evaluate this effect, we compared the calculated scattering behavior for core-shell and core + ten-shell models with linearly varying scattering length density for the shell. The two scattering curves compare very well with each other and none of the main scattering features were significantly altered by the increased number of fitting parameters. This suggests that variations in scattering length density along the polyoxyethylene chains are not significant. Similarly, fitting the data to a “flower” model as used for star polymers did not indicate any hydrophilic chains extending far into solution, so we confined our analysis to a core + single shell model to describe micelle structure.

The independent fitted variables for core-shell spheres are the core radius ($R_c$) and the shell thickness ($t_{shell}$) = $R_{micelle} - R_c$). The corresponding fitting parameters for core-shell rods are the cross-sectional radius of the core $R_c$, $t_{shell}$, and the length of the micelle core, $L_c$.

The other parameters required to describe the scattering functions are the number density of micelles, $N_p$, and the scattering length densities of the core, solvent and hydrated ethylene oxide shell, $\rho_{core}$, $\rho_{D_2O}$, $\rho_{shell}$ as well as the background coming from various sources such as incoherent scattering and ambient background. The total background, calculated using the Porod law, has been subtracted from all spectra. $\rho_{core}$ was calculated from the scattering lengths and volumes of methyl and methylene fragments, and $\rho_{D_2O}$ was taken as 1.914 × 10$^{-4}$ Å$^2$ for D$_2$O. $\rho_{shell}$ is a volume weighted average of the scattering lengths of ethylene oxide fragments and D$_2$O.

Where $b_{EO}$ and $b_{DO}$ are the scattering lengths of an ethylene oxide unit (4.139 × 10$^{-5}$ Å$^2$) and a D$_2$O molecule respectively, $v_{EO}$ and $v_{D_2O}$ are the molecular volumes (calculated from known densities) of an ethylene oxide unit (64.7 Å$^3$) and a D$_2$O molecule, respectively. $n_d/m$ is the ratio of D$_2$O molecules to ethylene oxide units in the headgroup region and was calculated from the shell volume, $V_{shell}$

$$n_{D_2O}/m = \frac{V_{D_2O}/v_{D_2O}}{m} = \left(\frac{V_{shell}}{2mN_{agg}} - v_{EO}\right)\frac{1}{v_{D_2O}}$$

where $N_{agg}$ is the micelle aggregation number calculated by simply dividing the volume of the homogeneous micelle core, $V_c$ (4/3)$\pi R_c^3$ for spheres; $\pi R_c^2 L_c$ for rods) by the volume of the hydrophobic moiety of a single molecule, $V_{shell}$, which here includes two alkyl chains and a hexamethylene spacer (864 Å$^3$ for Gem$_{12}$; 972 Å$^3$ for Gem$_{14}$; 1300 Å$^3$ for Gem$_{20}$).

### Table 2. Radii of Gyration of Gemini Nonionic Surfactant Micelles in 1 wt % Solution at 25 °C

<table>
<thead>
<tr>
<th>surfactant</th>
<th>$R_G$ (Å)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gem$<em>{12}E</em>{10}$</td>
<td>69 ± 5</td>
</tr>
<tr>
<td>Gem$<em>{12}E</em>{15}$</td>
<td>27 ± 3</td>
</tr>
<tr>
<td>Gem$<em>{14}E</em>{10}$</td>
<td>208 ± 20</td>
</tr>
<tr>
<td>Gem$<em>{14}E</em>{15}$</td>
<td>26 ± 6</td>
</tr>
<tr>
<td>Gem$<em>{20}E</em>{10}$</td>
<td>80 ± 50</td>
</tr>
<tr>
<td>Gem$<em>{20}E</em>{20}$</td>
<td>38 ± 3</td>
</tr>
<tr>
<td>Gem$<em>{20}E</em>{30}$</td>
<td>54 ± 5</td>
</tr>
</tbody>
</table>


(25) Richetti P. Personal communication.


The number density of micelles (micelles divided by volume) was calculated from

$$N_p = \frac{\phi_{HC}}{V_c}$$

where $\phi_{HC}$ is the volume fraction of hydrocarbon from $^{24}$

$$\phi_{HC} = \frac{\phi_{m,HC}}{d_{HC}} + \frac{\phi_{m,EO}}{d_{EO}} + \frac{\phi_{m,solv}}{d_{solv}}$$

where $\phi_{m,HC}$, $\phi_{m,EO}$, and $\phi_{m,solv}$ are the mass fractions of hydrocarbon tails, ethylene oxide and D$_2$O respectively, and $d_{HC}$, $d_{EO}$, and $d_{solv}$ are the corresponding densities (assumed to be the same as the bulk densities). The mass fractions were calculated from

$$\phi_{m,HC} = \frac{Mw_{tail}}{Mw_{surf}}$$

$$\phi_{m,EO} = \frac{Mw_{head groups}}{Mw_{surf}}$$

$$\phi_{m,solv} = 1 - (\phi_{m,HC} + \phi_{m,EO})$$

where $\phi_{m,surfactant}$ is the mass fraction of surfactant in solution and $Mw_{tail}$, $Mw_{head groups}$, and $Mw_{surf}$ are the molecular weights of the tail, the combined headgroups and the total surfactant.

Figure 2 shows the best fits of monodisperse core–shell models to the SANS spectra of 1 wt % gemini nonionic surfactants at 25 °C, with corresponding values of the molecular weights of the tail, the combined headgroups and Mw,surf are the mass fraction of surfactant in solution and Mw,tail, Mw,head groups, and Mw, surf are the molecular weights of the tail, the combined headgroups and the total surfactant.

<table>
<thead>
<tr>
<th>surfactant</th>
<th>model</th>
<th>$R_c (\AA)$</th>
<th>$t_{shell} (\AA)$</th>
<th>$R_{tot} (\AA)$</th>
<th>$L_c (\AA)$</th>
<th>$\rho_{shell} \times 10^{-6} \AA^{-2}$</th>
<th>$n_{D,of,m}$</th>
<th>$N_{agg}$</th>
<th>$t_{calc} (\AA)$</th>
<th>$R_f (\AA)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gem12E10</td>
<td>rod</td>
<td>13</td>
<td>20</td>
<td>33</td>
<td>130</td>
<td>4.6</td>
<td>4.8</td>
<td>79.9</td>
<td>12.3</td>
<td>14.9</td>
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<tr>
<td>Gem12E15</td>
<td>sphere</td>
<td>17.8</td>
<td>21.2</td>
<td>39.0</td>
<td>650</td>
<td>5.0</td>
<td>6.8</td>
<td>27.3</td>
<td>16.2</td>
<td>18.9</td>
</tr>
<tr>
<td>Gem14E10</td>
<td>rod</td>
<td>14.8</td>
<td>18.2</td>
<td>33.0</td>
<td>650</td>
<td>3.7</td>
<td>2.5</td>
<td>46.0</td>
<td>12.5</td>
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<td>sphere</td>
<td>19.2</td>
<td>20.5</td>
<td>39.7</td>
<td>650</td>
<td>4.9</td>
<td>6.2</td>
<td>30.5</td>
<td>15.8</td>
<td>18.9</td>
</tr>
<tr>
<td>Gem20E15</td>
<td>rod</td>
<td>19</td>
<td>18</td>
<td>37</td>
<td>b</td>
<td>4.1</td>
<td>3.4</td>
<td>b</td>
<td>18.2</td>
<td>18.9</td>
</tr>
<tr>
<td>Gem20E20</td>
<td>sphere</td>
<td>26.0</td>
<td>26.1</td>
<td>52.1</td>
<td>b</td>
<td>5.2</td>
<td>8.3</td>
<td>56.8</td>
<td>20.9</td>
<td>22.4</td>
</tr>
<tr>
<td>Gem20E30</td>
<td>sphere</td>
<td>22.8</td>
<td>29.9</td>
<td>52.7</td>
<td>5.6</td>
<td>13.7</td>
<td>39.3</td>
<td>27.8</td>
<td>25.3</td>
<td>28.3</td>
</tr>
</tbody>
</table>

*$R_c$ is the radius of the hydrocarbon core of the micelle, $t_{shell}$ is the thickness of the polyoxyethylene shell, $R_{tot}$ is the total radius ($R_c + t_{shell}$), $L_c$ is the core length of a core–shell rod (the total length is $L_c + 2t_{shell}$), $\rho_{shell}$ is the scattering length density of the shell obtained from $n_{D,of,m}$, $t_{calc}$ is the thickness of the polyoxyethylene layer calculated from scaling arguments, and $R_f$ is the Flory radius (see text).

Table 3. Best Fit Parameters for 1 wt % Gemini Surfactants at 25 °C (Figure 2) Showing the Model that Yielded the Best Fit

The fitted length of the core was 131 Å and aggregation number 115; however, due to the poor quality of the fit at low Q, this should only be taken to indicate an anisotropic micelle.

Additional structural features such as spherical end caps on the micelles, flexibility in the rods, or micelle polydispersity. Intermicellar attractions could also be responsible for the discrepancy; however, these are probably not significant as an adequate fit was obtained for the much longer rods of Gem12E10 and for Gem20E15 at higher temperatures, as discussed below.

Considering first the spherical micelles formed by Gem20E15, Gem14E15, and Gem20E20, the fitted hydrocarbon core radii of 17.8, 19.2, and 26 Å are in good agreement with the expected fully extended alkyl chain lengths, $l_c$, of 16.7, 19.2, and 26.8 Å. The micelle core is consistent with the standard picture for conventional surfactants, although the radius may be slightly greater than expected for Gem12E15 because of the hexamethylene spacer.

The core radius of the rodlike micelles is in every case notably smaller than the corresponding spheres, with 13 Å versus 17.8 Å for Gem12E10, 14.8 Å versus 19.2 Å for Gem14E15, and 19 Å versus 23–26 Å for Gem20E15. This has also been observed previously for conventional surfactants$^{31}$ and can be understood qualitatively by considering the thermodynamics of rodlike micelles. Israelachivi et al.$^5$ have argued that rodlike micelles form spherical end caps in order to reduce the free energy cost of hydrocarbon ends in contact with water. Using a combination of thermodynamic and geometric arguments, they show that the ratio of the area of the rod ($a_o$) to the area of the end caps ($a_e$) lies between 2/3 and 1. From this expression, it can be shown that the cross-sectional radius of the rod must lie between 2$l_c/3$ and $l_c$, which forms an upper bound on the radius of a spherical section end-cap. That is, the radius of a rodlike micelle will be up to 2/3 less than that of a sphere, which is close to the radius ratio observed here.

Among the rod-forming micelles, the fitted length of the cores increases significantly as alkyl tail length is increased from Gem12E10 to Gem14E15. The micelle sphere–to–rod transition is very sensitive to alkyl chain length in both ionic and nonionic conventional surfactants.$^{32}$ Here too a small change in chain length produces a large effect. It has been conjectured previously that longer alkyl chains may not be fully extended in the micelle core.$^{30}$ In the language of the surfactant packing parameter, this means that alkyl chain volume, $v$, increases faster than the micelle radius, which is less than $l_c$, leading to a lower curvature. Our results showing the smaller radii of the hydrocarbon core of rodlike micelles also support this proposition.

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Micelle aggregation numbers, \( N_{agg} \), are shown in Table 3. Like the hydrocarbon core radii, the aggregation numbers for Gem\(_{20}\)E\(_{20}\), Gem\(_{20}\)E\(_{15}\), and Gem\(_{30}\)E\(_{30}\) agree well with expectations for spherical micelles with fully extended alkyl chains (i.e., a surfactant packing parameter of exactly one-third). However, both the radius and aggregation numbers of Gem\(_{20}\)E\(_{20}\) are smaller than expected, and this is considered below.

The corona of polyoxyethylene chains behaves as a fairly homogeneous layer with an approximately constant scattering length density. The fitted shell thickness of 20–30 Å is comparable with or greater than the corresponding hydrophobic core radii, making these micelles somewhat similar to those formed by block copolymers. Considering first only spherical micelles, the shell thickness increases with increasing polyoxyethylene chain length. These results are also consistent with recent results for C\(_{12}\)E\(_{23}\) micelles, which yielded a core radius of 15–17 Å and a homogeneous shell thickness of approximately 25 Å, close to the value we obtain for Gem\(_{20}\)E\(_{20}\).

The measured shell thickness is much smaller than the fully extended (all trans) lengths of approximately 40 Å for E\(_{10}\) or 120 Å for E\(_{30}\) and is consistent with the polyoxyethylene chains adopting a coiled conformation in aqueous solution. The conformation of polyoxyethylene chains and the structure of the hydrophilic shell in nonionic surfactant micelles has long been a subject of investigation. The characteristic dimension of a polyoxyethylene coil of \( m \) units in water can be described by its end-to-end distance or Flory radius, \( R_F \), where the statistical segment length of CH\(_2\)CH\(_2\)O is \( l = 3.9 \) Å and the exponent \( \alpha = 0.583 \). However, polymer chains tethered on a surface may be extended into a brush-like conformation by excluded volume interactions with their neighbors. Johnsson et al. have recently used such a model, developed for much longer starlike block copolymer micelles, to describe polyoxyethylene chains as short as 17 units in the corona of spherical lipid micelles. The shell thickness around a sphere in this model is given by

\[
\nu_{\text{calc}}(\text{sphere}) = \left[ \frac{m l^{1/2} R_c}{3 \alpha^{1/2}} - R_c^{1/2} \right] - R_c \tag{2}
\]

where \( N_{\text{chain}} \) is the number of chains attached to the micelle surface, here twice the micelle aggregation number.

The same scaling arguments can be applied to describe the conformation of chains tethered to a rodlike micelle, yielding

\[
\nu_{\text{calc}}(\text{rod}) = \left[ \frac{1 + \alpha l^{1/2} \left( \frac{\pi R_c}{4 \nu} \right)^{1/2} + R_c^{1/2} \left( \frac{\nu}{\alpha} \right)^{1/2}}{\frac{1 + \alpha l^{1/2} \left( \frac{\pi R_c}{4 \nu} \right)^{1/2} + R_c^{1/2} \left( \frac{\nu}{\alpha} \right)^{1/2}}{2}} \right] - R_c \tag{3}
\]

Here \( \nu \) is the volume occupied by one gemini surfactant in the hydrophobic core. Thus, \( 2 \nu R_c^{3/2} \) is equal to the number of tethered polyoxyethylene chains (2 per molecule) per unit of length along the core, \( N_{\text{chain}} \). Shell thicknesses for spheres and rods, \( \nu_{\text{calc}} \), calculated in this way using best-fit core radii are listed in Table 3.

In every case except Gem\(_{20}\)E\(_{15}\), the calculated thickness is less than the experimentally fitted shell thickness. More remarkably, it is in every case less than the unperturbed Flory radius of the polyoxyethylene chain, \( R_F \). (The same is true for the results of Johnsson et al., for which the layer thickness only exceeds \( R_F \) for chains containing more than 80 ethoxy units.) This suggests that tethering to a hydrophobic core alone does not lead to stretching of these shorter chains. Rather, at least within this model, the curvature of the interface and low attachment density allows them to extend laterally even more than in bulk solution.

Experimental shell thicknesses are on average 2.4 Å thicker than the unperturbed chain dimension, \( R_F \). Although less than the length of a single ethoxy unit, this small difference is uniformly observed and is especially apparent if only spherical micelles are considered. This may arise from some chain extension or preferential orientation of ethoxy segments near the hydrophobic core. However, these surfactants are polydisperse in their polyoxyethylene chains, so that 50% of chains are longer than the average degree of ethoxylation. For example, the experimentally measured thickness of 21.2 Å for Gem\(_{20}\)E\(_{15}\) corresponds to \( R_F \) of the 75th percentile of the chain distribution and 24.1 Å to the 90th percentile. This would also be more than enough to account for the discrepancy between measured and predicted shell thickness for all of the surfactants studied.

This finally leaves us with a picture of a polyoxyethylene shell around spherical or elongated micelles consisting of chains in conformations close to their unperturbed solution dimensions. No gradient in composition is or should be needed to describe the structure of the shell.

The amount of water per ethoxy monomer unit in the shell, \( n_{D_2O}/m \), is obtained from the fitted data using eq 1. All of the values obtained are much larger than the 1.2–2.0 \( n_{D_2O}/m \) values typically obtained for conventional nonionic surfactants with smaller polyoxyethylene chains but compares well with a value of around 7 obtained for C\(_{12}\)E\(_{23}\). The results are in fact consistent with the available volume for \( D_2O \) inside a polyoxyethylene coil of \( m \) units, which may be estimated by subtracting the volume occupied by the chain monomers from the total volume of the (unstretched) coil

\[
V_{D_2O} = \frac{\pi}{6} R_F^3 - \nu_{\text{EO}} \tag{4}
\]

The number of \( D_2O \) molecules that can be accommodated per ethoxy unit within the coil is then just

\[
n_{D_2O}/m = \frac{V_{D_2O}^{1/2}}{V_{D_2O}^{1/2}} \tag{5}
\]

which increases as \( m^{0.75–0.8} \) for a polymer chain in a good solvent like polyoxyethylene in water. The values and trends in the water-to-ethoxy ratios and corresponding shell scattering length densities thus calculated agree well with the fitted data, as listed in Table 4. These values thus simply reflect the fact that shell scattering includes all of the water present, not only water of solvation, and that the amount of available volume for solvent increases with chain length.

We return briefly to the low aggregation number obtained for Gem\(_{20}\)E\(_{30}\) (Table 3). The smaller core is very likely to be an accommodation by the hydrophobic chains.
Table 4. Calculated and Fitted Parameters for Polyoxyethylene Shells of Gemini Nonionic Surfactants

<table>
<thead>
<tr>
<th>M</th>
<th>(n_{\text{D2O/m}}) calc.</th>
<th>(n_{\text{D2O/m}}) expt.</th>
<th>(\rho_{\text{shell}}) (x (10^{\text{-6}} \text{ Å}^2)) calc.</th>
<th>(\rho_{\text{shell}}) (x (10^{\text{-6}} \text{ Å}^2)) expt.</th>
</tr>
</thead>
<tbody>
<tr>
<td>100</td>
<td>3.7</td>
<td>2.5, 4.8</td>
<td>4.2</td>
<td>3.7</td>
</tr>
<tr>
<td>10a</td>
<td>5.7</td>
<td>3.3, 6.2, 6.8</td>
<td>4.2, 4.1, 4.9</td>
<td>5.0</td>
</tr>
<tr>
<td>20</td>
<td>7.6</td>
<td>8.3</td>
<td>5.1</td>
<td>5.2</td>
</tr>
<tr>
<td>30</td>
<td>11.1</td>
<td>13.7</td>
<td>5.4</td>
<td>5.6</td>
</tr>
</tbody>
</table>

* Multiple values correspond to different alkyl chain lengths with the same degree of ethoxylation, \(m\): Gem12E10, Gem14E15, Gem12E15, Gem14E125, Gem20E15.

Figure 3. SANS spectra for (a) Gem20E15, (b) Gem20E20, and (c) Gem20E30 at 1 wt % (circles), 2 wt % (squares, Gem20E15 only), 5 wt % (triangles), and 10 wt % (diamonds). Hard sphere fits are shown for Gem20E20 and Gem20E30 (see Table 5 for best fit values).

of the conformation adopted by the larger E30 chain in water, similar to effects seen in block copolymer micelles.39

Concentrated Solutions. Figure 3 shows SANS spectra for solutions of Gem20E15, Gem20E20, and Gem20E30 respectively at concentrations between 1 and 10 wt %. SANS spectra for Gem20E20 and Gem20E30, which form spherical micelles in dilute solution, were fitted using a core–shell form factor17 together with a hard sphere structure factor (using the Percus–Yevick closure).40 The fitting parameters are the same as in the dilute solution case, together with an effective hard-sphere volume fraction of micelles, which determines \(S(Q)\). Best fits are shown in Figure 3 and fitting parameter values are given in Table 5. The model used here also allows for some polydispersity in the micelle sizes. We found this to be smaller in every case than the smearing due to the 15% wavelength spread in the incident neutrons and so has been disregarded.

This model fits the experimental data well at low \(Q\) and near the peak for both Gem20E20 and Gem20E30, as expected for interacting spherical micelles. The fits are poorer at higher \(Q\), where they fall away from the peak too sharply. This is probably because the micelles do not interact as hard spheres but via a soft steric repulsion between ethylene oxide headgroups. For further details, see ref 24.

This is also evident from the effective hard sphere volume fractions of the micelles, which are roughly double the real volume fractions. True volume and weight fractions should be approximately the same in these systems because the densities of the surfactant and the solvent are almost the same. This artifact arises from the large volume of water in the polyoxyethylene shell, discussed above, which increases the effective volume fraction of the micelles and in turn produces the steeper falloff in intensity at high \(Q\) in the hard-sphere model. The volume fraction of micelles including all water in the shell is expected to be 3.3–3.6 times greater than the dry volume fraction, whereas the best fit data yields only about 2. Micelle structural parameters, \(R_c\), \(t_{\text{shell}}\), and especially \(\rho_{\text{shell}}\), do not vary systematically with surfactant concentration, so we conclude that the micelle sizes do not change very much in the range examined. The observed variations probably arise simply from inconsistencies in modeling the polyoxyethylene shell in the form and structure factors, and should not be over interpreted.

The nearest neighbor center-to-center distance (\(D\)) estimated from the peak position using13 \(D = 2\pi Q_{\text{peak}}\) yields \(D \sim 140 \text{ Å}\) for Gem20E20 and \(D \sim 150 \text{ Å}\) for Gem20E30 at 10 wt %. These values are comparable with the fitted micelle diameters of 105–110 and 110–120 Å, respectively, again underscoring the problems associated with a hard-sphere interaction in these systems.

Effects of Temperature. Figure 4 shows SANS spectra for 1 wt % solutions of Gem12E10, Gem14E10, and Gem20E15 as a function of temperature from 20 °C up toward their respective cloud points. All three show an increase in the scattering at low \(Q\) indicating the formation and growth of cylindrical micelles. Both Gem12E10 and Gem20E15 already form elongated micelles at 20 °C. Only Gem12E10 shows the complete evolution from near-spherical or short rodlike micelles at 20 °C into the \(Q^{-1}\) dependence expected for long, rigid rods.19 For each of these surfactants, the

Table 5. Best Fit Values for Gem20E20 and Gem20E30 at 1, 5, and 10 wt %

<table>
<thead>
<tr>
<th>surfactant</th>
<th>(R_c) (Å)</th>
<th>(t_{\text{shell}}) (Å)</th>
<th>(p)</th>
<th>(\rho_{\text{shell}}) (x (10^{\text{-6}} \text{ Å}^2))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gem20E20</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1 wt %</td>
<td>26.0</td>
<td>26.1</td>
<td>5.2</td>
<td></td>
</tr>
<tr>
<td>5 wt %</td>
<td>0.11</td>
<td>25.4</td>
<td>23.2</td>
<td>0.09</td>
</tr>
<tr>
<td>10 wt %</td>
<td>0.21</td>
<td>31.3</td>
<td>24.0</td>
<td>0.07</td>
</tr>
<tr>
<td>Gem20E30</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1 wt %</td>
<td>22.8</td>
<td>29.9</td>
<td>5.6</td>
<td></td>
</tr>
<tr>
<td>5 wt %</td>
<td>0.116</td>
<td>21.1</td>
<td>26.5</td>
<td>0.12</td>
</tr>
<tr>
<td>10 wt %</td>
<td>0.084</td>
<td>32.0</td>
<td>28.1</td>
<td>0.00</td>
</tr>
</tbody>
</table>

* \(\phi_{\text{HS}}\) is the effective hard sphere volume fraction of interacting micelles, \(R_c\) is the core radius, \(t_{\text{shell}}\) is the shell thickness, \(p\) is the polydispersity (the variance divided by the mean radius), \(\rho_{\text{shell}}\) is the scattering length density of the shell.

SANS data indicates elongation at low temperatures before approaching a $Q^{-1}$ dependence several degrees below the cloud temperature, i.e., short rigid rodlike micelles\(^\text{19}\) that grow as the cloud temperature is approached.

The shape of nonionic micelles as a function of temperature has long been studied using SANS. Zulauf et al.\(^\text{41}\) found increased scattering by C\(_8\)E\(_4\), C\(_8\)E\(_5\),\(^\text{16,17,41}\) and C\(_{12}\)E\(_8\) solutions at low $Q$ with increasing temperature, which they interpreted as attractions between spherical micelles. They proposed that the micelles form loose “clouds” due to a short-range attraction that became stronger as the temperature approached the cloud point. Triolo et al.,\(^\text{7}\) studying C\(_{12}\)E\(_6\),\(^\text{7}\) found a similar scattering behavior and attributed it to critical concentration fluctuations between spherical micelles. However, Lum Wan et al.\(^\text{5}\) have shown (for C\(_{12}\)E\(_6\) at least) that these data could also be interpreted as polydisperse, rodlike micelles, and that SANS, in isolation of other techniques, is not capable of distinguishing between the two models.

More recently, Glatter et al.\(^\text{31}\) have studied C\(_{6}\)E\(_4\),\(^\text{16,17,41}\) C\(_{10}\)E\(_4\), and C\(_{12}\)E\(_5\),\(^\text{16,17,41}\) from 3 °C up to their cloud temperatures with a combination of SANS and viscosity measurements. Using a more complex method\(^\text{42,43}\) than previous studies, they interpreted the solution structure as interacting, rodlike micelles, finding a sphere-to-rod transition with increasing temperature. Further, surfactants with small headgroups, such as C\(_6\)E\(_4\) (\(T_c\sim37 \text{ °C}\)) and C\(_{12}\)E\(_5\) (\(T_c\sim30 \text{ °C}\)), formed rodlike micelles even at low temperatures.

The general trends obtained here for the gemini surfactants compare well with the study by Glatter et al.\(^\text{31}\) Surfactants with small headgroups form rodlike micelles at low temperatures, whereas larger headgroups produce spherical micelles. As the cloud temperature is approached, the micelles undergo a sphere-to-rod transition and micellar growth.

The viscosity of Gem\(_{20}\)E\(_{15}\) also strongly suggests a sphere-to-rod transition on warming. Figure 5 shows the temperature dependence of the relative viscosity of Gem\(_{20}\)E\(_{15}\) aqueous solutions. Below about 40 °C, the solutions are Newtonian and have low viscosities, but on warming, the viscosity increases rapidly at all concentrations studied. At 1 wt %, \(\eta_r\) increases by a factor of about 10 between 40 and 70 °C. At 10 wt %, the sample was visually observed to become viscoelastic at approximately 50 °C and then gelled near 60 °C so that no flow was observed in the viscometer. The massive increase in viscosity above 40 °C corresponds well with the large increase in low angle scattering and supports the growth of rigid rodlike micelles and formation of an entangled network.

No such effects of temperature on viscosity increases were observed for the shorter tailed Gem\(_{12}\)E\(_{10}\), and only a slight increase in viscosity occurred for Gem\(_{14}\)E\(_{10}\) just below the cloud temperature, despite both approaching a $Q^{-1}$ scattering dependence. We conclude therefore that the high viscosity is a consequence of the higher energies required for scission of rodlike micelles with two C\(_{20}\) alkyl chains (\(R_c\sim19 \text{ Å}\)) compared with C\(_{12}\) or C\(_{14}\) (\(R_c\sim13 \text{ or } 15 \text{ Å}\)). A similar dependence of viscosity (and viscoelasticity) on alkyl chain length has been observed for elongated micelles of the well-known alkyltrimethylammonium salicylate surfactants.\(^\text{32}\) For 1 mM solutions, the viscosity was found to increase by a factor of 10 when the alkyl chain was increased from C\(_{12}\) to C\(_{14}\) but by a factor of 100 when further increased to C\(_{16}\).

Conclusions

The structure of aqueous Gem\(_m\)E\(_n\) micelles is similar to that of conventional, or monomeric nonionic surfactants.

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The presence of two alkyl chains and a hexamethylene spacer decreases their solubility, so that longer polyoxyethylene chains are needed on each alkyl tail to confer solubility, but after this the trends on behavior are familiar. At room-temperature Gem$_{12}$E$_{15}$, Gem$_{14}$E$_{15}$, Gem$_{20}$E$_{20}$, and Gem$_{20}$E$_{30}$ all form spherical micelles; Gem$_{20}$E$_{15}$ and Gem$_{12}$E$_{10}$ form slightly anisotropic (short rod) micelles, whereas Gem$_{14}$E$_{10}$ (which has the largest packing parameter value among the surfactants examined) forms long rodlike micelles. Increasing the temperature of the Gem$_{12}$E$_{10}$, Gem$_{14}$E$_{15}$, and Gem$_{20}$E$_{15}$ from 20 °C toward their cloud temperature results in the growth of long rodlike micelles. In Gem$_{20}$E$_{15}$, this is accompanied by a marked increase in viscosity, the onset of viscoelasticity at low concentrations, and gelation of the solution at higher concentrations. Such an effect has not previously been reported for nonionic surfactants to our knowledge.

The polyoxyethylene chains in the micelle corona are well-described by a random coil chain in a good solvent having an approximately constant composition and scattering length density, with no significant chain stretching as occurs for longer chains and for star polymers.

Acknowledgment. This work was supported by the Australian Research Council Industry Linkage Program, Orica Australia, and Huntsman Chemicals. P.A.F. acknowledges receipt of an ARC postgraduate scholarship, and T.W.D. acknowledges receipt of a Henry Bertie and Florence Mabel Gritton Postdoctoral Fellowship from the University of Sydney. This work utilized facilities supported in part by the National Science Foundation under Agreement No. DMR-9986442. We acknowledge the support of the National Institute of Standards and Technology, U.S. Department of Commerce, in providing the neutron research facilities used in this work.