Choosing the Right Neutron Spectrometer

Peter Gehring

NIST Center for Neutron Research

Main Messages of the Week

(1) Neutron scattering experiments measure the flux of neutrons scattered by a sample into a detector as a function of the change in neutron wave vector ($\vec{Q}$) and energy ($\hbar\omega$).

$$\Phi(Q,\hbar\omega) = \frac{\text{neutrons}}{\text{sec–cm}^2}$$
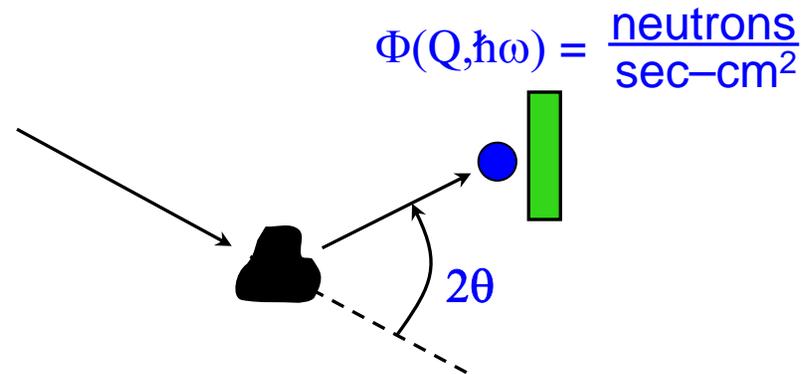
Momentum

$$\hbar k = \hbar(2\pi/\lambda)$$

$$\hbar Q = \hbar\vec{k}_i - \hbar\vec{k}_f$$

Energy

$$\hbar\omega_n = \hbar^2 k_n^2/2m$$

$$\hbar\omega = \hbar\omega_i - \hbar\omega_f$$

2θ

(2) The expressions for the scattered neutron flux Φ involve the positions and motions of atomic nuclei or unpaired electron spins.

$$\Phi = \mathbb{F}\{\vec{r}_i(t),\ \vec{r}_j(t),\ \vec{S}_i(t),\ \vec{S}_j(t)\}$$
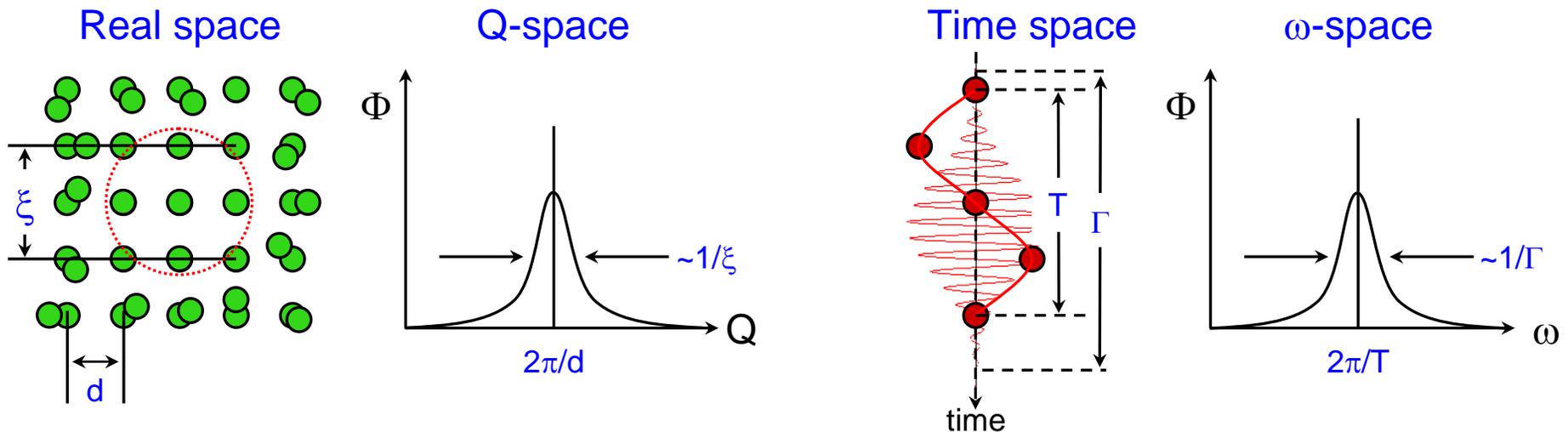
Φ provides information about __all__ of these quantities!
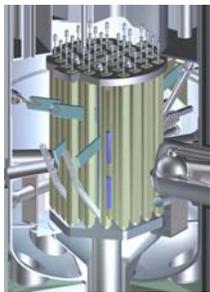
Main Messages of the Week

(3) The scattered neutron flux $\Phi(\vec{Q}, \hbar\omega)$ is proportional to the space ($\vec{r}$) and time (t) Fourier transform of the <u>probability</u> $G(\vec{r}, t)$ of finding one or two atoms separated by a particular distance at a particular time.

$$\Phi \propto \frac{\partial^2 \sigma}{\partial\Omega\partial\omega} \propto \iint e^{i(\vec{Q}\cdot\vec{r} - \omega t)} G(\vec{r}, t) d^3\vec{r} dt$$

Real space

ξ

d

Q-space

Φ

$\sim 1/\xi$

$2\pi/d$

Q

Time space

T

Γ

time

ω-space

Φ

$\sim 1/\Gamma$

$2\pi/T$

ω

What is required to do an inelastic neutron scattering experiment?

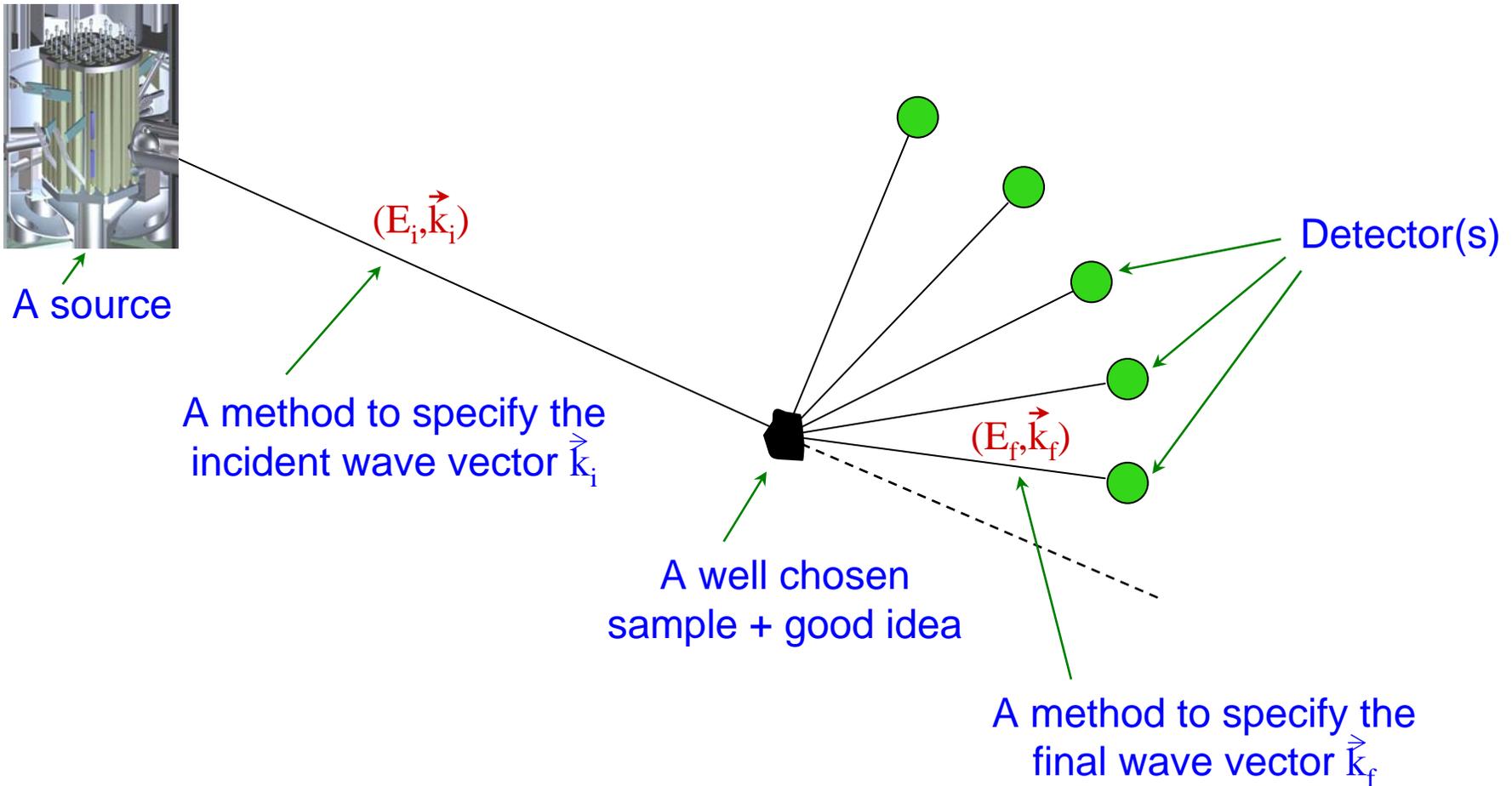A source

$(E_i, \vec{k}_i)$

A method to specify the incident wave vector $\vec{k}_i$

A well chosen sample + good idea

$(E_f, \vec{k}_f)$

Detector(s)
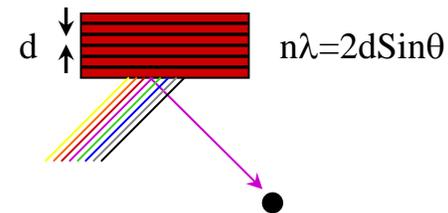
A method to specify the final wave vector $\vec{k}_f$

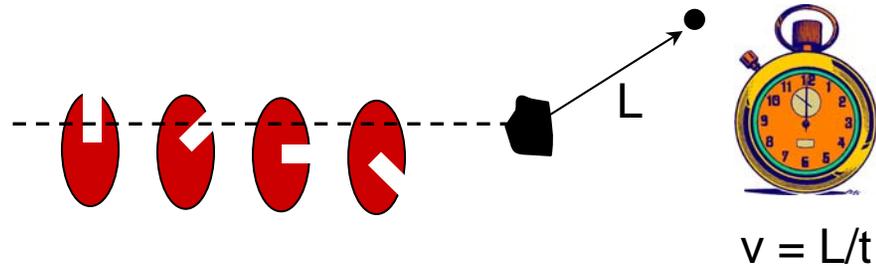# Methods of specifying and measuring $\vec{k}_i$ and $\vec{k}_f$

1. **Bragg Diffraction**
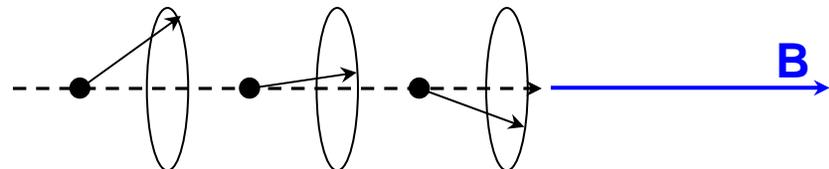
    SPINS, FANS, Backscattering

    d $n\lambda = 2d\sin\theta$

2. **Time-of-Flight (TOF)**

    DCS, Backscattering (?)

    L

    $v = L/t$

3. **Larmor Precession**

    Spin Echo

    B

Why are there so many different spectrometers?

Because neutron scattering is an intensity limited technique. Thus detector coverage and resolution MUST be tailored to the science.

Uncertainties in the neutron wavelength and direction imply that $\mathbf{Q}$ and $\hbar\omega$ can only be defined with a certain precision.

The total signal in a scattering experiment is proportional to the resolution volume → better resolution leads to lower count rates! So choose *carefully* …

$\propto$
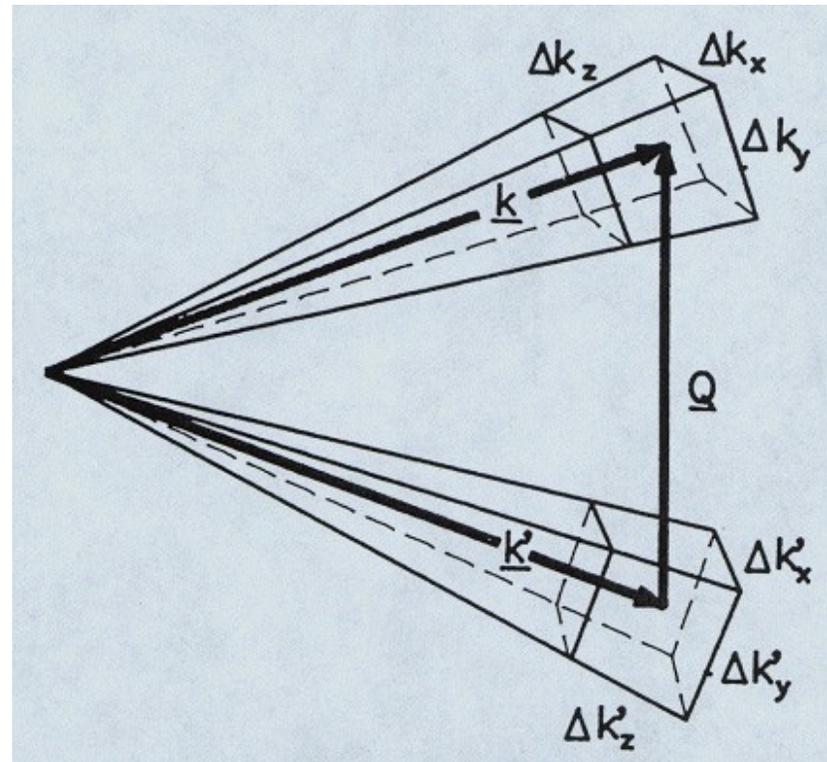
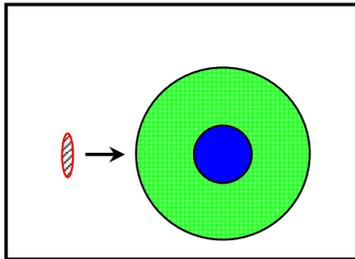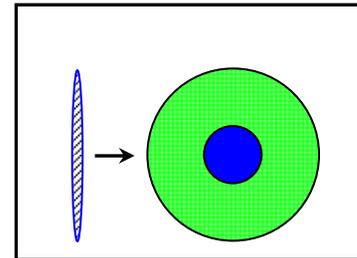Courtesy of R. Pynn

Q-Resolution Matters!
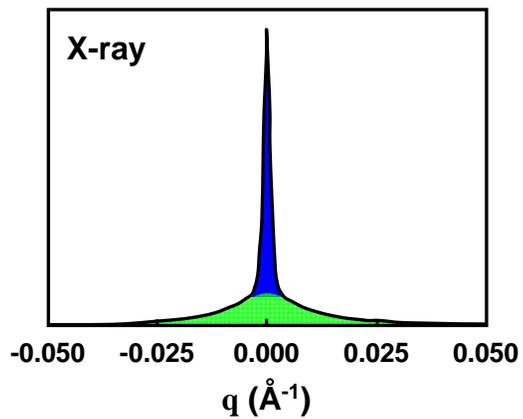
The "right" resolution depends on what you want to study.

ħω-Resolution Matters!
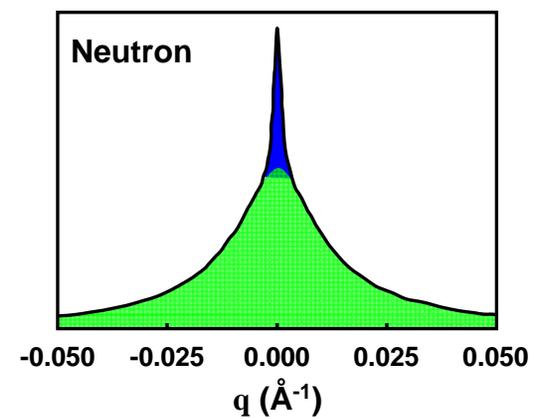
"Elastic" Bragg Peak Intensity

Consider $YBa_2Cu_3O_{6.35}$
$T_c = 18K$

Magnetic order occurs
at $Q = (1/2, 1/2, 2)$.

What is T_N?

☐ C5	$\Delta E = 1500\ \mu eV$
◆ C5	$\Delta E = 100\ \mu eV$
● SPINS	$\Delta E = 80\ \mu eV$
● HFBS	$\Delta E = 0.8\ \mu eV$
? Spin Echo	

Intensity (Arb Units)

1000
800
600
400
200
0

T (K)
0   10   20   30   40   50   60

A "fatter" energy resolution integrates
over low-energy fluctuations …
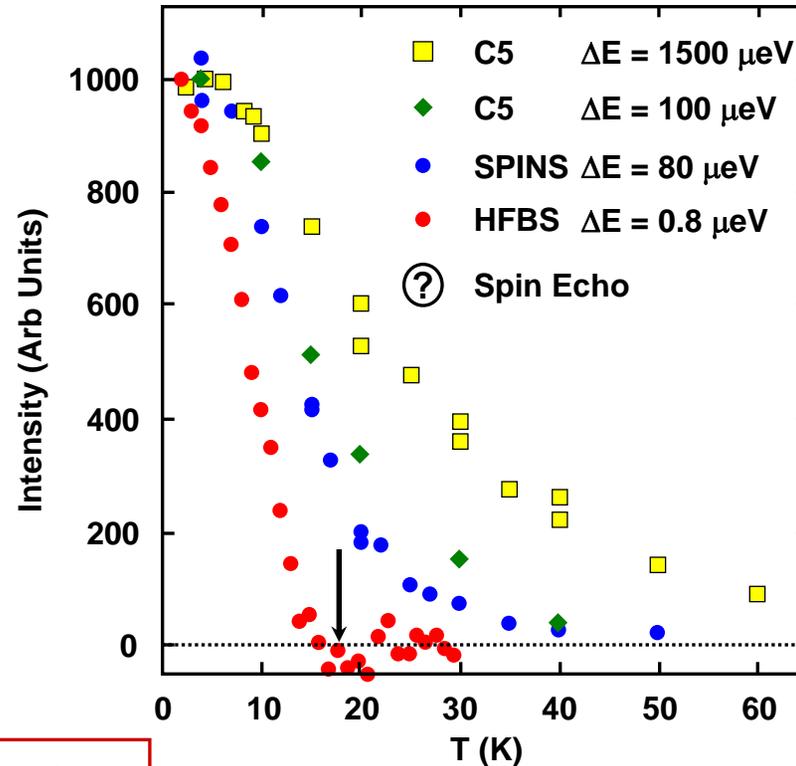
ℏω-Resolution Matters!

Another example …

SPINS

$\vec{Q} = (0,K,0.5)$
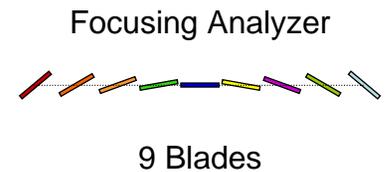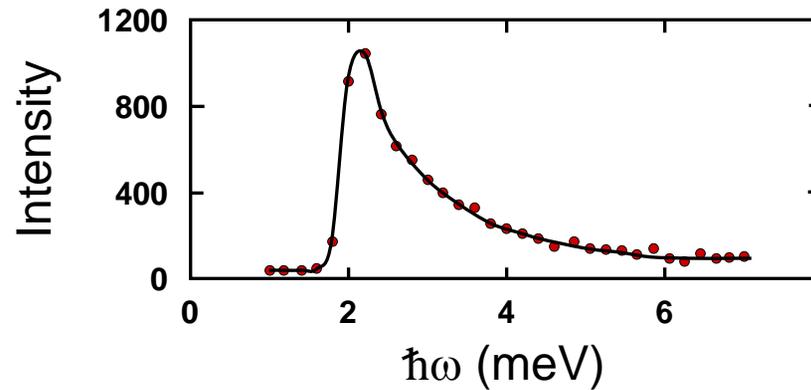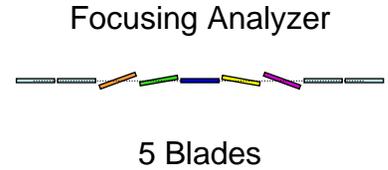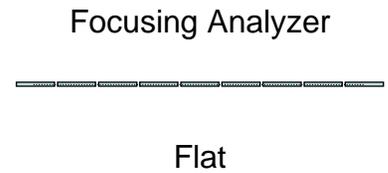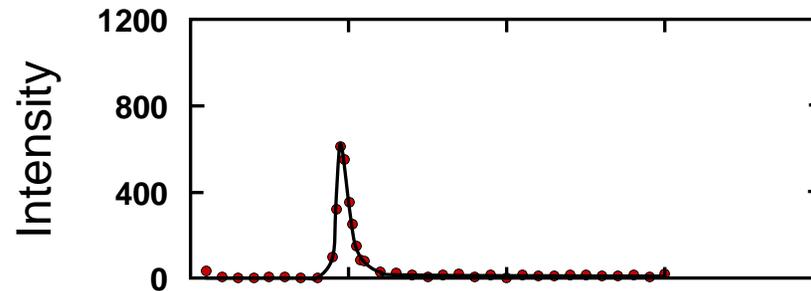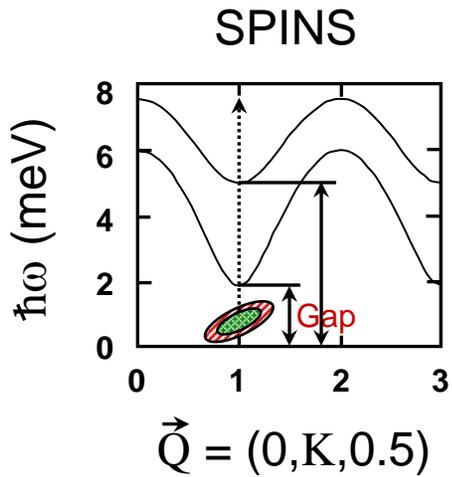
So, how do I choose the right spectrometer?

Two basic considerations:

1. What are the time scales ($\hbar\omega$) of interest?

2. What are the length scales (Q) of interest?

(Some spectrometers overlap → the choice may boil down to one of resolution)
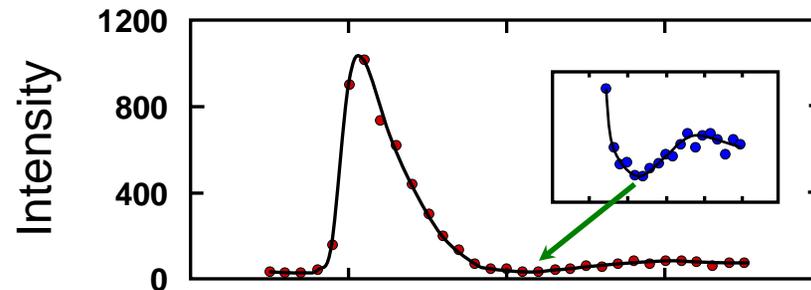
Two additional considerations:

1. What energy resolution ($\Delta\hbar\omega$) is required?

2. What momentum resolution (ΔQ) is required?

Different spectrometers cover different regions of phase space

Rules of Thumb

1. What are the energies ($\hbar\omega$), i.e. time scales ($\Delta t \sim 1/\omega$), of interest?

$\hbar\omega > $ 10-20 meV - use FANS (or another spectrometer designed for vibrational spectroscopy)

$\hbar\omega < $ 20-30 μeV - use HFBS
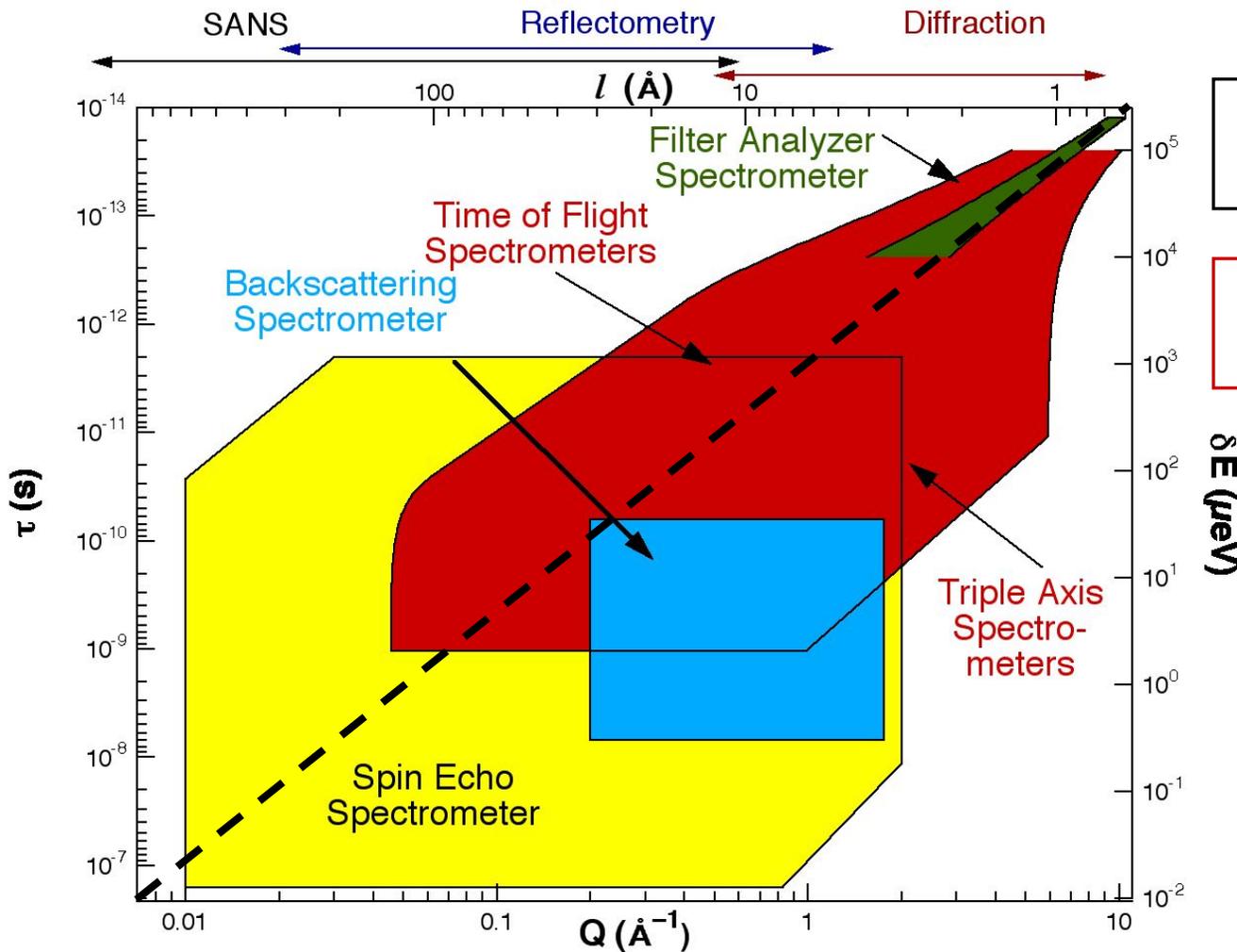
In between - use DCS (or another cold neutron TOF spectrometer)

2. Be certain that the length scales of the relevant motions lie within the range of the spectrometer.

As a simple example, consider the HFBS instrument. ($Q \sim 2\pi/L$)

$Q_{min} = 0.25$ Å^{-1} → $L_{max} \sim 25$ Å

$Q_{max} = 1.75$ Å^{-1} → $L_{min} \sim 3.5$ Å

REMEMBER - Q_{min} and Q_{max} are inversely proportional to the incident neutron wavelength

DCS versus SPINS

DCS   – incoherent scattering,
         broad surveys in $\mathbf{Q}$-ω

SPINS – coherent scattering,
         limited regions in $\mathbf{Q}$-ω

Rules of Thumb: (think carefully before violating)

DCS – systems requiring resolution < 100 μeV

SPINS – single crystals

Things to consider when choosing SPINS

Triple axis spectrometers are typically used when either the *direction* of **Q** is important or the interesting region of **Q-ω** space is of *limited extent*.

k_i k_f

One data point at a time …

Remember – Intensity ↓

Resolution ↑

Collimation(')	λ	rel. signal	FWHM .
55-80-80-80	4 Å	1.00	0.28 meV
55-40-40-40	4 Å	0.24	0.17 meV
69-80-80-80	5 Å	0.26	0.13 meV
84-80-80-80	6.1 Å	0.03	0.05 meV
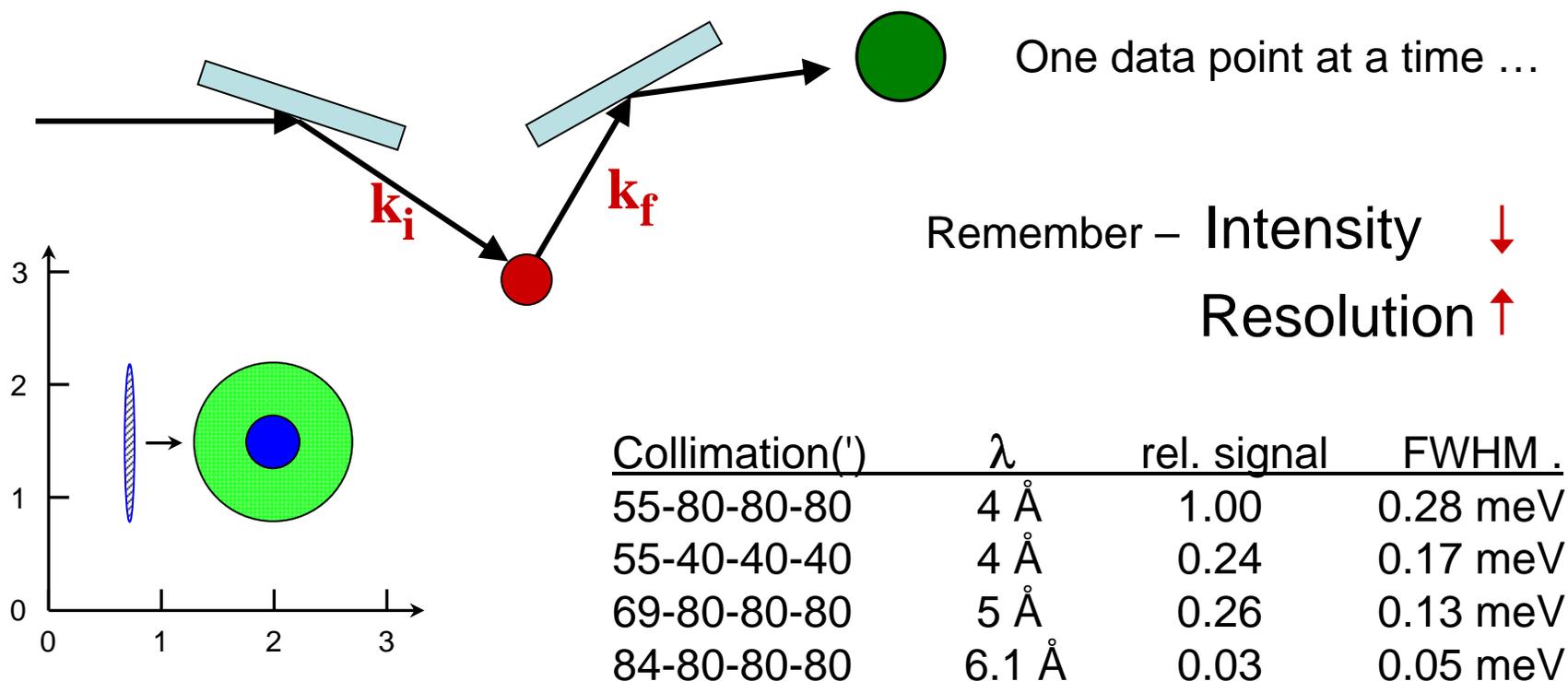
Things to consider when choosing DCS

ΔE

I(E)
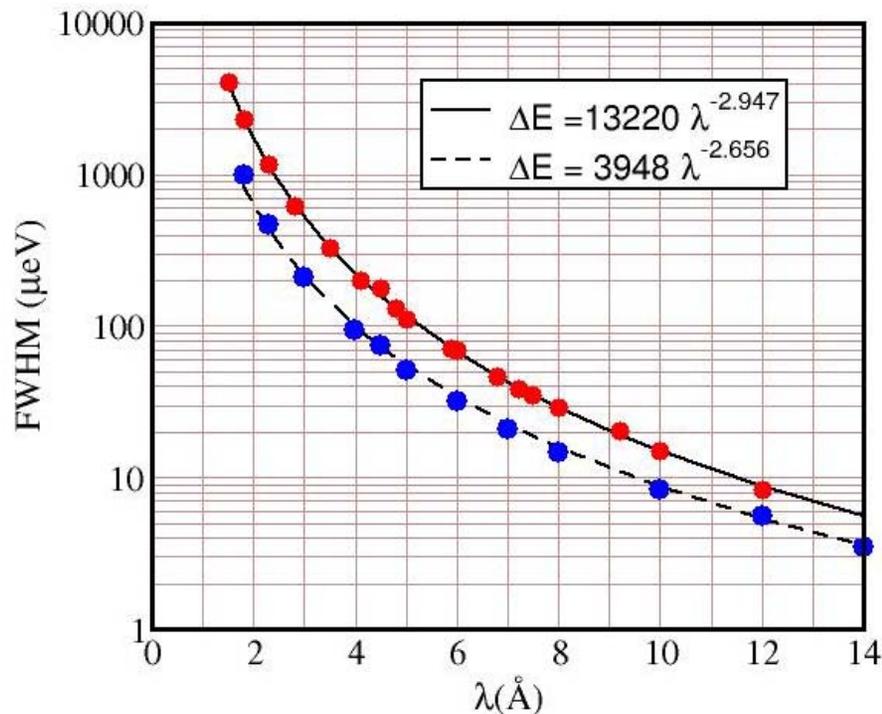
Quantities varied

• wavelength λ

• chopper slot widths W

Remember – **Intensity** ↓

Resolution ↑

Things to consider when choosing HFBS

$0.25\ \text{Å}^{-1} < Q < 1.75\ \text{Å}^{-1}$ Do the length scales of interest lie within this range?
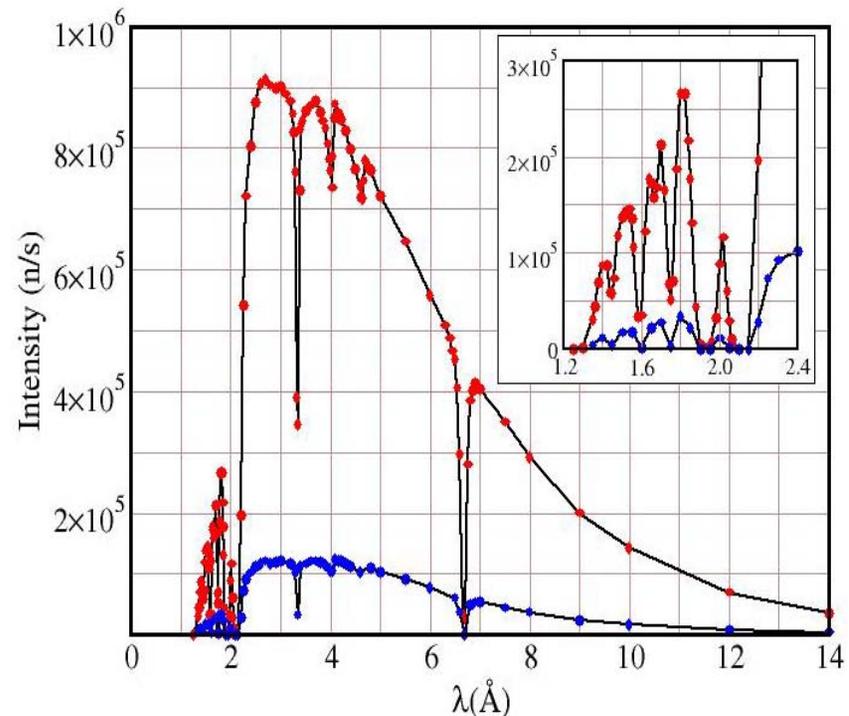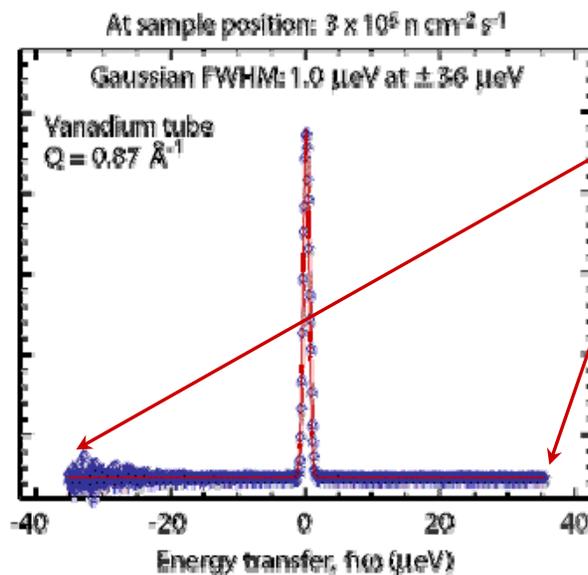
$\delta Q < 0.1 - 0.2\ \text{Å}^{-1}$ Can you live with such coarse Q-resolution?

At sample position: 3×10^5 n cm^{-2} s^{-1}

Gaussian FWHM: 1.0 μeV at ± 36 μeV

Vanadium tube
Q = 0.87 Å^{-1}

-40   -20   0   20   40

Energy transfer, ℏω (μeV)

Do the features that interest you lie within this range?

Do you really require such good energy resolution $\delta E \sim 1\ \mu eV$ (or perhaps even better resolution)?

Things to consider when choosing NSE

If the resolution of backscattering is "not good enough" or if you are only interested in a "limited" region of $\mathbf{Q}$ space (typically small $\mathbf{Q}$) …

… use NSE (low $\mathbf{Q}$, long times)
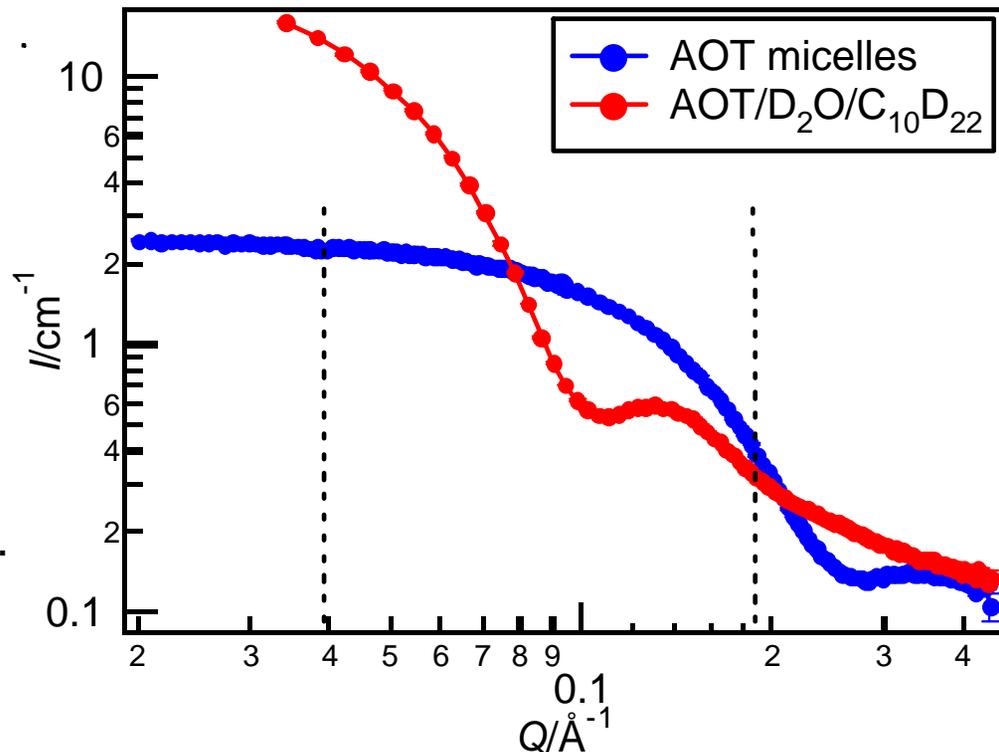
These cases typically involve coherent scattering, which tends to peak around

$$Q \sim \frac{2\pi}{\text{Relevant length scale of sample}}$$

Remember – slower motions usually imply larger length scales.

Many atoms moving together => Coherent scattering

Legend: AOT micelles; AOT/D_2O/$C_{10}D_{22}$

Axes: I/cm^{-1} (vertical); Q/Å^{-1} (horizontal)

Things to consider about your sample
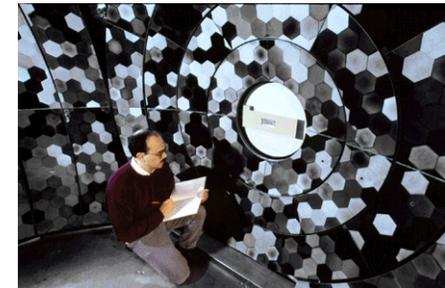
Is your sample polycrystalline or amorphous?

Does ONLY the magnitude (not the direction) of Q matter?

Is the expected Q-dependence of the scattering weak?

This often means that you want to look at a large region of Q-$\hbar\omega$ space or that you can sum the data over a large region of Q-$\hbar\omega$ space

If YES, consider instruments with large analyzer areas

FANS, DCS, Backscattering

General sample "design"

The most important thing is:

Know as much about your sample as possible (Beamtime costs ~ $4000/day!!)

The types of things that you might want to know include:

What's the structure (in a general sense)?
Are there any phase transitions (or a glass transition)?
What isotopes are present?
Supplementary data from other measurements …

Magnetization vs T   Muon spin relaxation   X-ray data

Specific heat vs T   Raman spectroscopy

General sample "design"

Try to avoid isotopes that are strongly absorbing

^{6}Li ^{10}B ^{113}Cd ^{157}Gd

For a complete listing go to

http://www.ncnr.nist.gov/resources/n-lengths

Sample "design" for triple-axis spectrometers
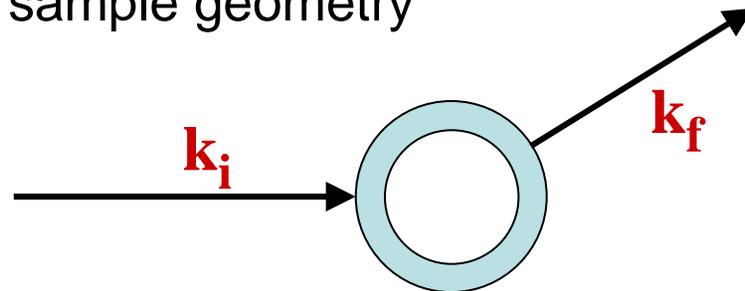
NCNR

Single Crystals yield the most information

Increase the intensity by increasing the amount of sample

If you have a powder, use a cylindrical container (rather than flat plate)

Annular may be the best sample geometry

k_i

k_f

Almost all experiments on triple-axis spectrometers involve coherent scattering
→ sample should be deuterated (if it contains H at all)

Sample "design" for DCS and HFBS

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Increase the intensity by increasing the amount of sample

→ Fill the beam with sample

maximum beam size is usually given in the instrument description
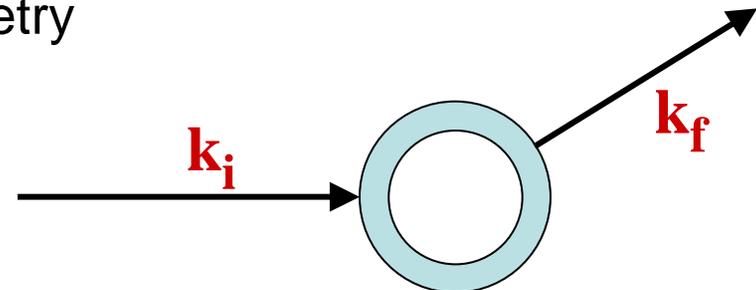
3 cm X 10 cm for DCS (or 1.5 cm X 10cm)   3 cm X 3 cm for Backscattering

If possible, use cylindrical samples (rather than flat plate)

Remember - For incoherent, quasielastic
scattering the transmission of the
beam should be ~90%

$$I/I_O = \exp-(n\sigma_T D)$$
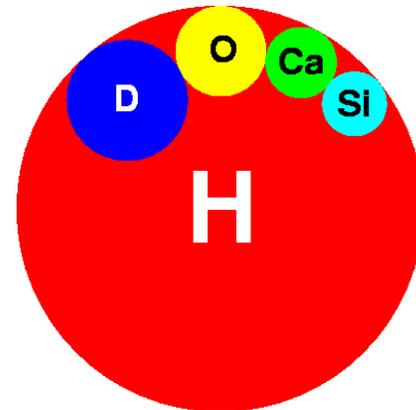
Often annular is the best sample geometry

k_i

k_f

Sample "design" for DCS and HFBS

Does the sample contain H?

Remember: Neutrons LOVE H!!

Create a sample where the "interesting" portions of the sample are hydrogenated and the "uninteresting" portions are deuterated.
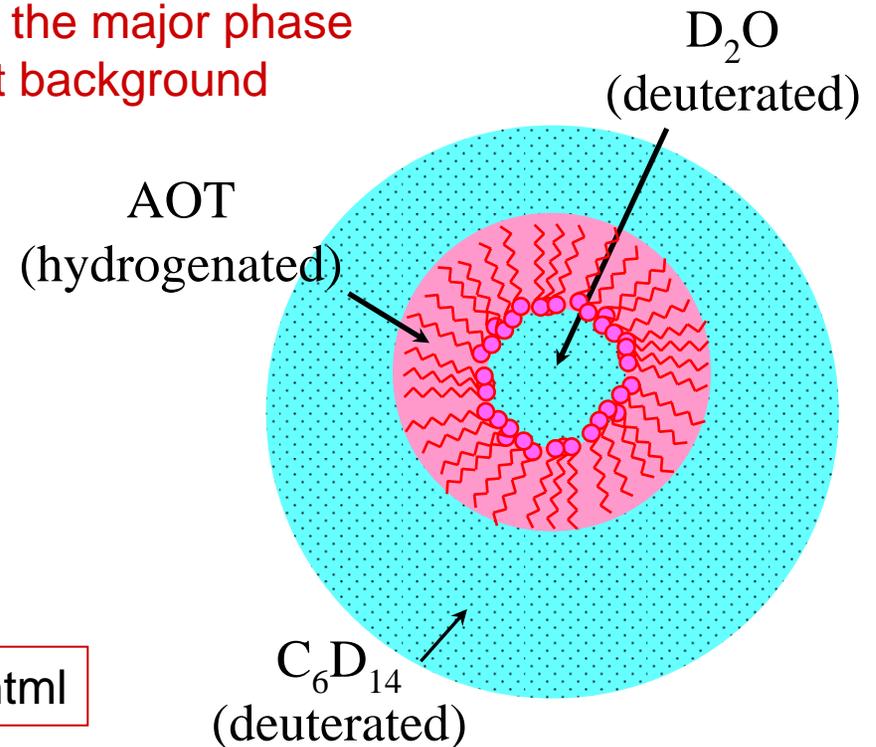
Sample "design" for NSE

Create a sample where the "interesting" portions
of the sample have a different SLD than the
"uninteresting" portions

Typically this means deuterating the major phase
in order to reduce the incoherent background

SLD core 6.4×10^{-6} Å^{-2}

SLD shell 1.0×10^{-6} Å^{-2}

SLD solvent 6.5×10^{-6} Å^{-2}

D_2O
(deuterated)

AOT
(hydrogenated)

C_6D_{14}
(deuterated)

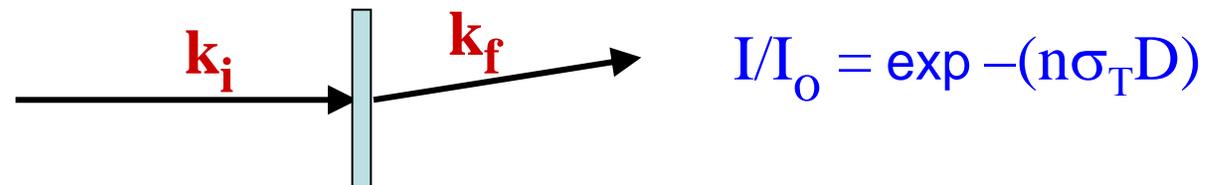http://www.ncnr.nist.gov/resources/sldcalc.html

Sample "design" for NSE

Increase the intensity by increasing the amount of sample
→ Fill the beam with sample
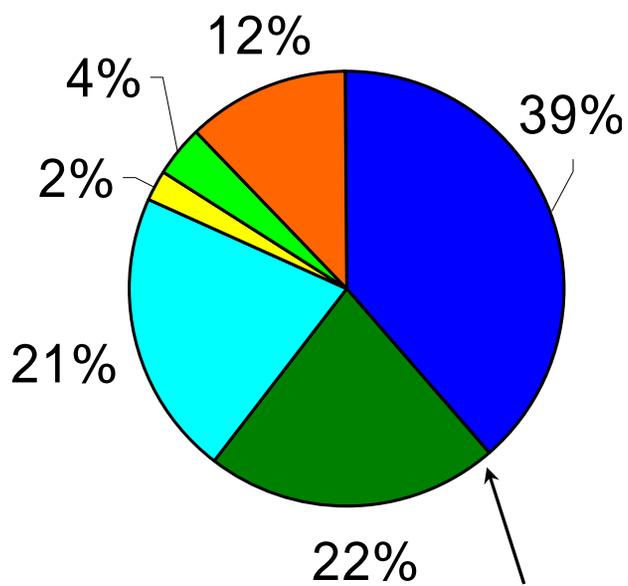
Typically use flat plate samples (at small angles)

$$\mathbf{k_i} \qquad \mathbf{k_f} \qquad I/I_O = \exp -(n\sigma_T D)$$

Rule of thumb - the transmission should be ~70%

Samples from this Summer School
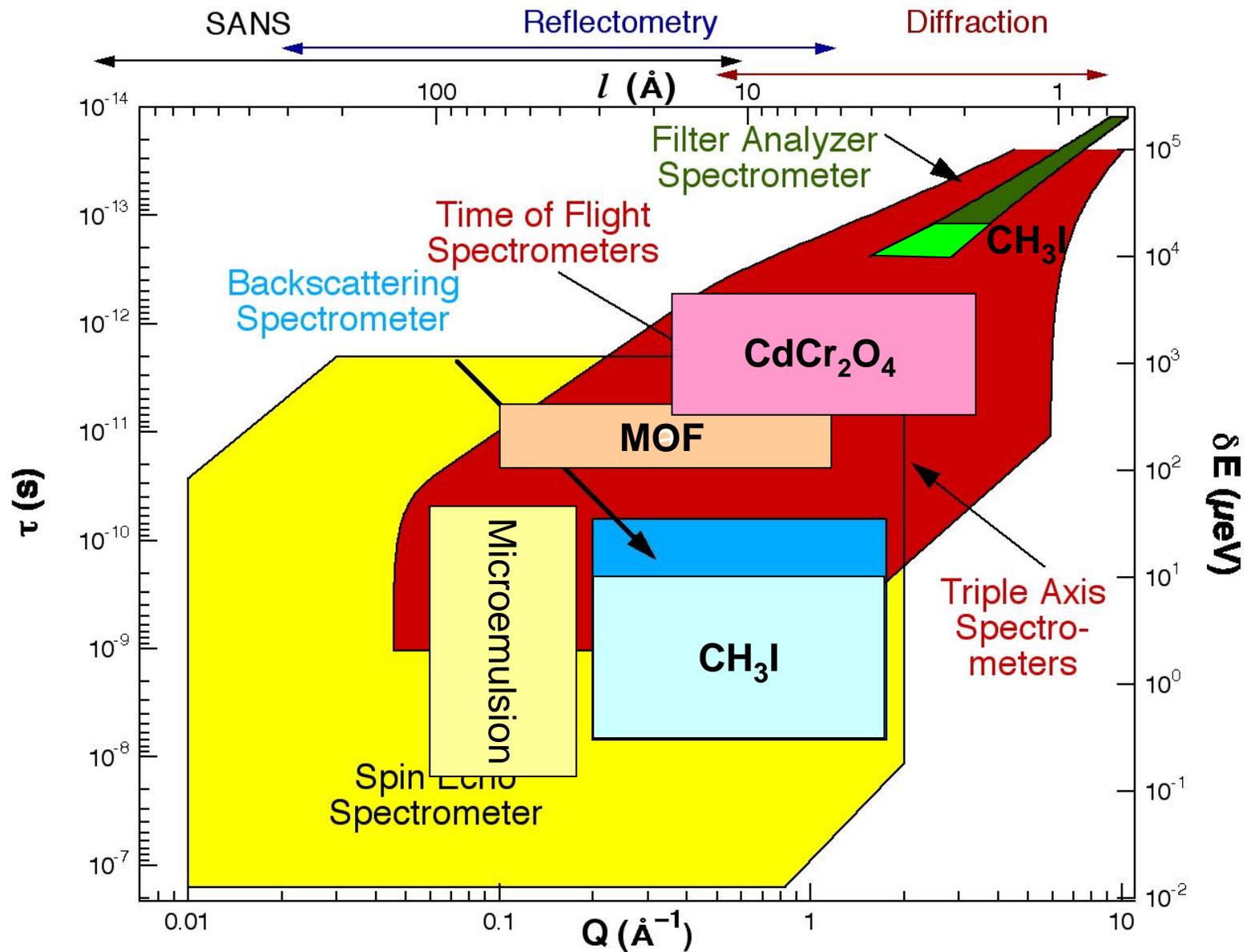
Types of Science
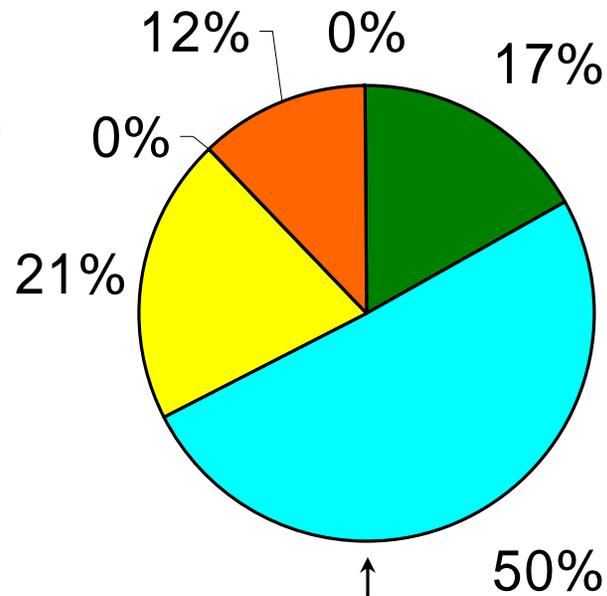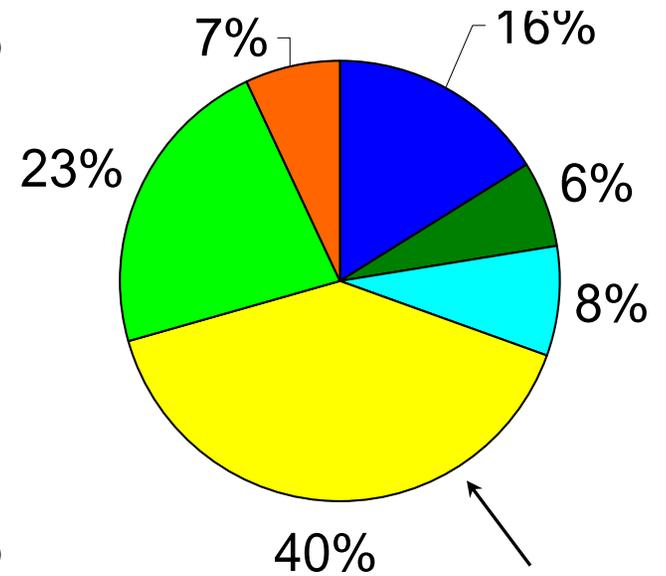
Applying for beam time

The use of the neutron scattering instrumentation that you've used over the past week is open to all qualified users based on peer-reviewed proposals. Calls for proposals are issued about twice per year.

The **next deadline** for **new proposals** will be **~October of 2008**.

Further information on submitting proposals can be found at:

http://www.ncnr.nist.gov/programs/CHRNS/CHRNS_prop.html

Some Summer School Success Stories

2001

Jae-Ho Chung
University Prof.

2003

Vicky Garcia-Sakai
ISIS Staff Scientist

1999

William Ratcliff
NCNR Staff Physicist

1997

Rob Dimeo
NCNR Deputy Director

Ok, so you can't win them all …

Acknowledgements

Organizers - Antonio Faraone and Yamali Hernandez

Our administrative staff - Julie Keyser

All of the experiment teams

Invited speakers - C.L. Broholm and M.C. Rheinstädter

Thanks for coming!