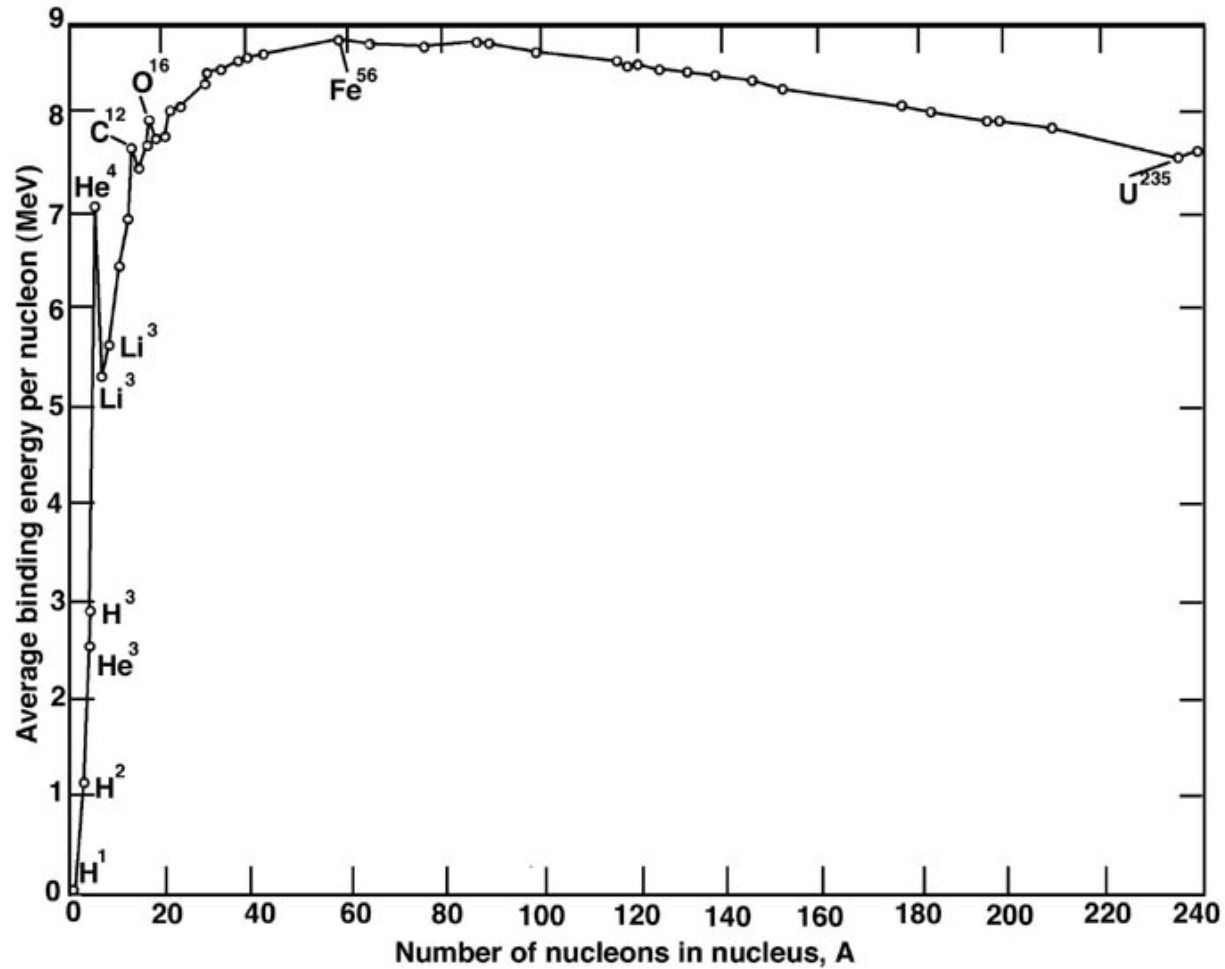


Neutron Binding Energy
Measurements for a Direct Test
of $E=mc^2$

Outline

- Framework of test
- Two crystal spectrometer
- Binding energy measurements
- Does $E=mc^2$?
- Towards 10^{-8} precision
- References
- Historical highlights of the program

Framework



Framework

$$n + {}^A X \rightarrow {}^{A+1} X + \gamma's$$

Framework

$$A_r(n) + A_r({}^A X) - A_r({}^{A+1} X) = \left\{ 10^{-3} \frac{N_A h}{c} \right\}_{\text{SI}} \left\{ \frac{1}{\lambda_{A+1}^*} \right\}_{\text{SI}}$$

Framework

Penning trap ion mass
measurement (m)

$$A_r(^{A+1}\text{X}) + A_r(\text{H}) - A_r(^A\text{X}) - A_r(\text{D}) =$$

$$\left\{ 10^{-3} \frac{N_A h}{c} \right\}_{\text{SI}} \left\{ \frac{1}{\lambda_{\text{D}}^*} - \frac{1}{\lambda_{A+1}^*} \right\}_{\text{SI}}$$

Molar Planck
constant
divided by c ; u_r
 $= 1.4 \times 10^{-9}$

Gamma-ray
measurements
(E)

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NIST Physics Laboratory home page

Physics Laboratory

NIST
National Institute of Standards and Technology

Supporting U.S. industry by providing measurement services and research for electronic, optical, and radiation technologies.

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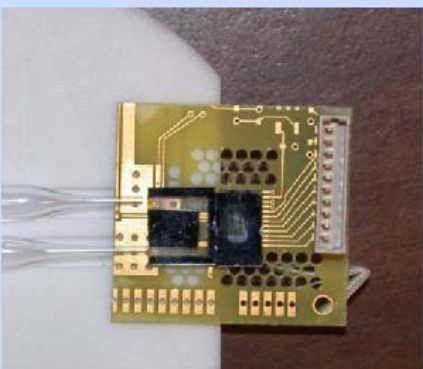
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Credit: NIST

'NMR on a Chip' Features NIST Magnetic Mini-Sensor

A super-sensitive mini-sensor developed at NIST can detect NMR in tiny samples of fluids flowing

Done

Local intranet 100%

The NIST Reference on Constants, Units, and Uncertainty

Information at the foundation of modern science and technology from the [Physics Laboratory](#) of NIST

[Detailed contents](#)

Fundamental Physical Constants

[Values of the constants](#) and related information
[Searchable bibliography](#) on the constants

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http://physics.nist.gov/cuu/Constants/index.html

Fundamental Physical Constants from NIST

The NIST Reference on Constants, Units, and Uncertainty

Information at the foundation of modern science and technology from the [Physics Laboratory of NIST](#)

CODATA Internationally recommended values of the Fundamental Physical Constants

Latest (2006) values of the constants

[Version history](#) and [disclaimer](#)

Constants Topics:

- Values
- Energy Equivalents
- Searchable Bibliography
- Background

Constants Bibliography

Constants Units & Uncertainty home page

(e.g., [electron mass](#), most misspellings okay)

Search for value by name

Display alphabetical list, table (image), or table (pdf)

by clicking a category below

Universal	Adopted values	Frequently used constants
Electromagnetic	Non-SI units	Extensive listings
Atomic and nuclear	Conversion factors for energy equivalents	All values (ascii)
Physico-chemical	X-ray values	

Find the [correlation coefficient](#) between any pair of constants
Data from the [least-squares adjustment](#) of the values of the constants

See also

[Reprint of the paper giving the details of the adjustment of the constants](#) [1.2 MB PDF]
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The NIST Reference on Constants, Units, and Uncertainty

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Uncertainty
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molar Planck constant

$$N_A h$$

Value $3.990\ 312\ 6821 \times 10^{-10} \text{ J s mol}^{-1}$

Standard uncertainty $0.000\ 000\ 0057 \times 10^{-10} \text{ J s mol}^{-1}$

Relative standard uncertainty 1.4×10^{-9}

Concise form $3.990\ 312\ 6821(57) \times 10^{-10} \text{ J s mol}^{-1}$

Click [here](#) for correlation coefficient of this constant with other constants

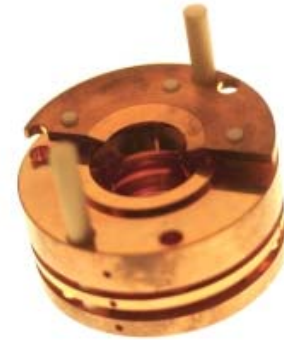
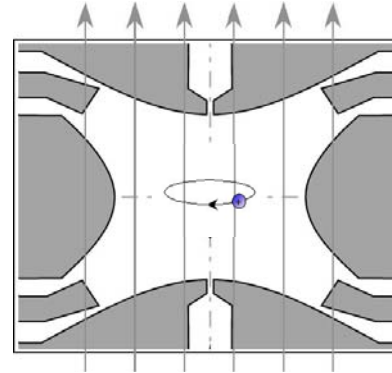
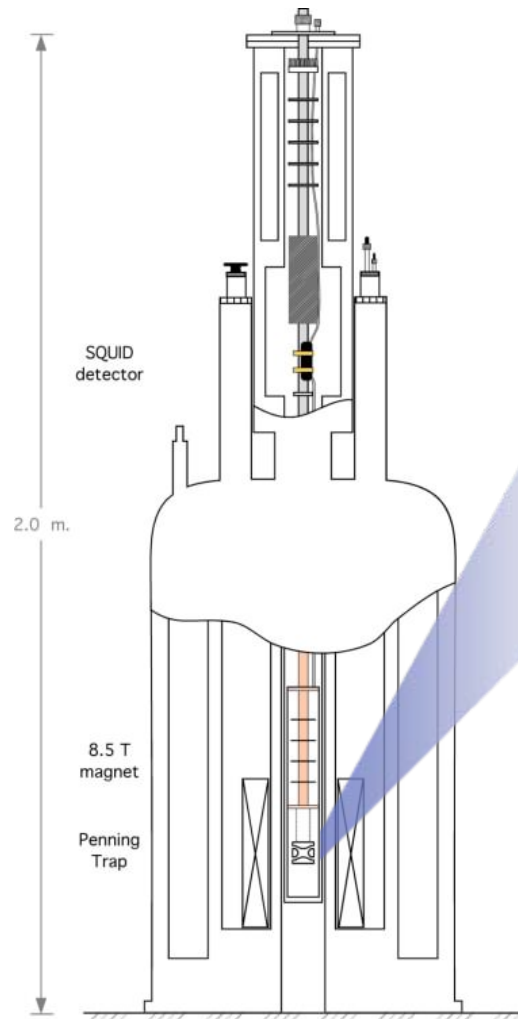
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recommended values](#)

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uncertainty](#)

[Correlation coefficient with
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Piège de Penning



Fréquence cyclotron $\omega_c = \frac{qB}{m}$
(5 MHz)

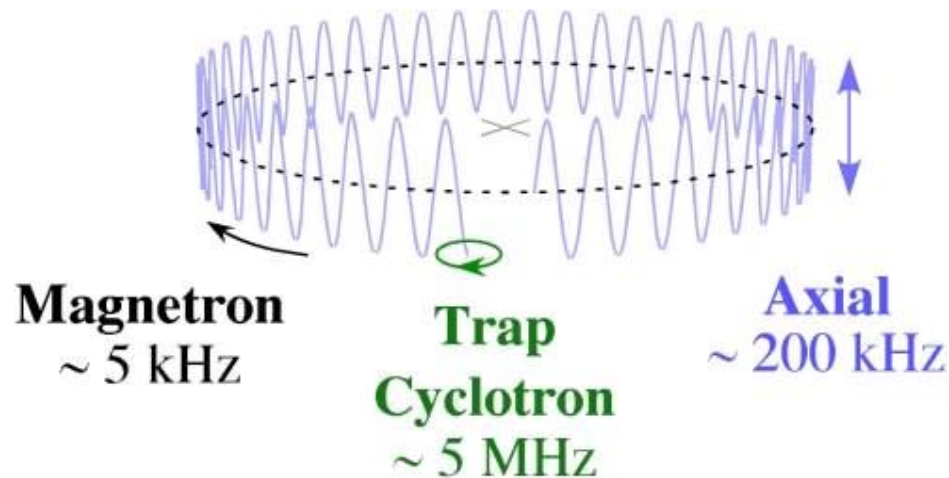


$$\frac{\omega_{c1}}{\omega_{c2}} = \frac{q_1}{q_2} \frac{m_2}{m_1}$$

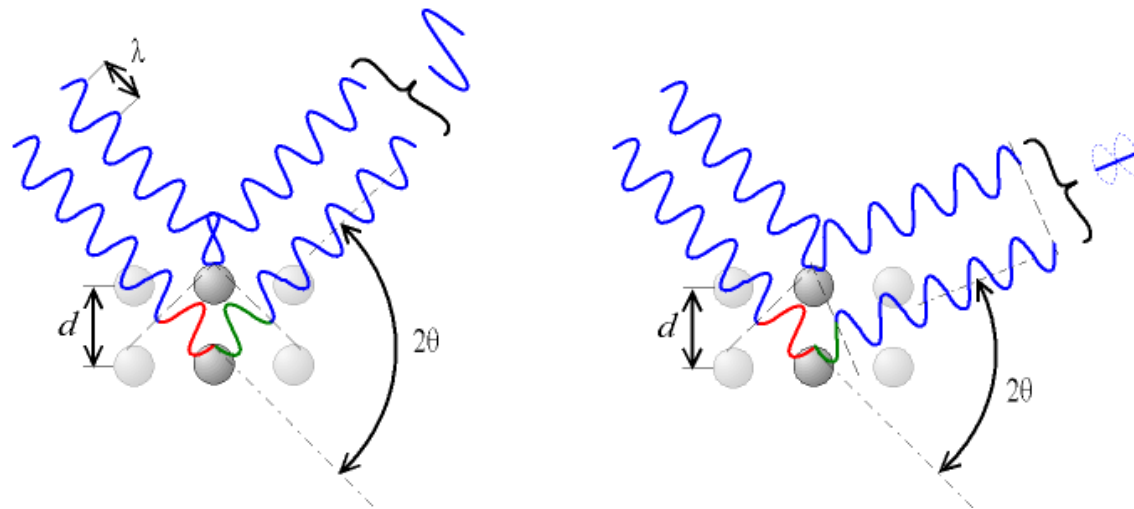
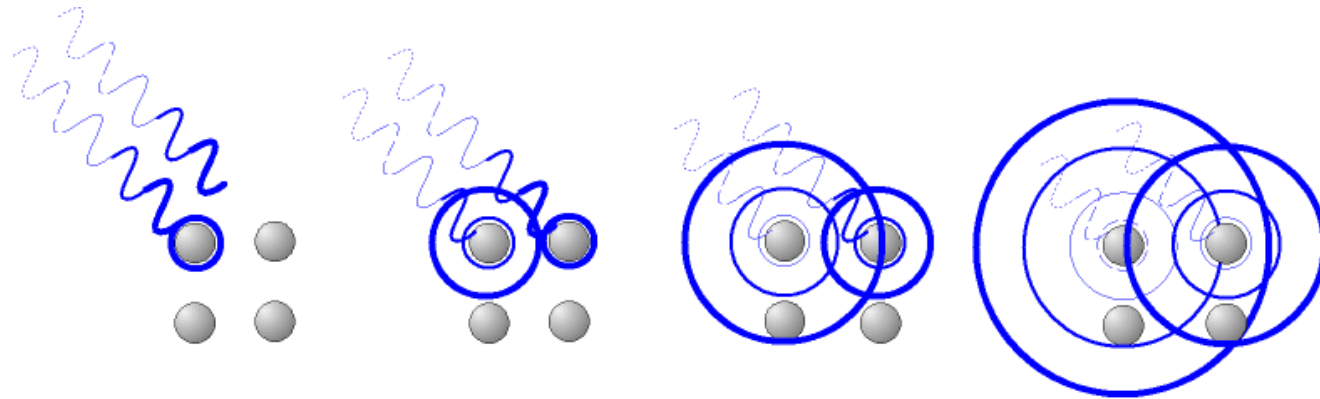
Exemples de résultat

$$\frac{m[{}^{33}\text{S}^+]}{m[\text{H}{}^{32}\text{S}^+]} = 0.999\,744\,164\,347\,(16) \quad (1.6 \times 10^{-11})$$

$$\frac{m[{}^{29}\text{Si}^+]}{m[\text{H}{}^{28}\text{Si}^+]} = 0.999\,715\,124\,181\,3\,(67) \quad (6.7 \times 10^{-12})$$



Wavelength Determination Principle



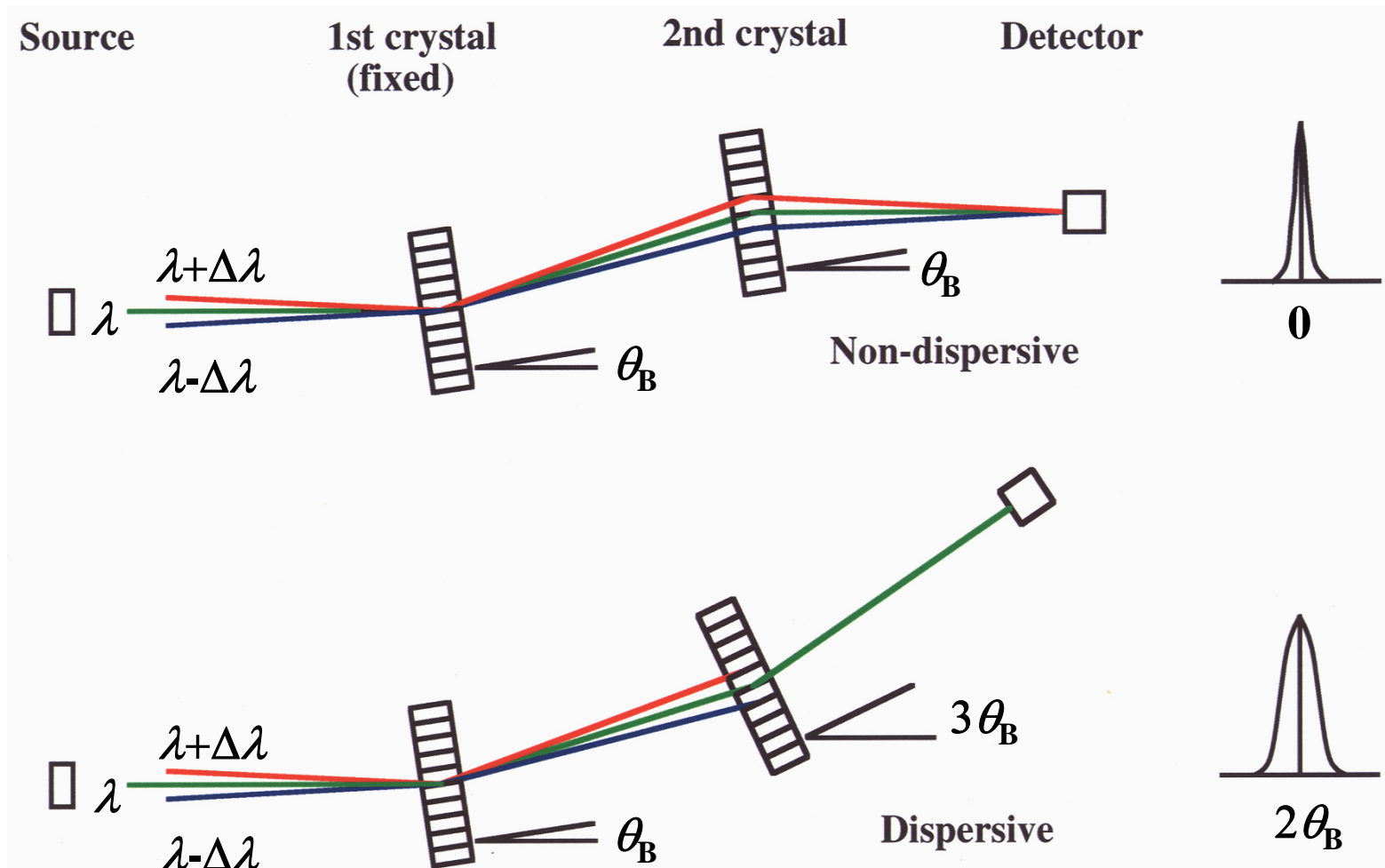
Wavelength Determination Principle

$$n\lambda = 2d \sin \theta_n$$

$$\frac{\Delta\lambda}{\lambda} \approx \sqrt{\left(\frac{\Delta d}{d}\right)^2 + \left(\frac{\Delta\theta_n}{\theta_n}\right)^2}$$

$$\frac{\Delta d}{d} \approx 5 \times 10^{-8} \quad \frac{\Delta\theta_n}{\theta_n} \approx ?$$

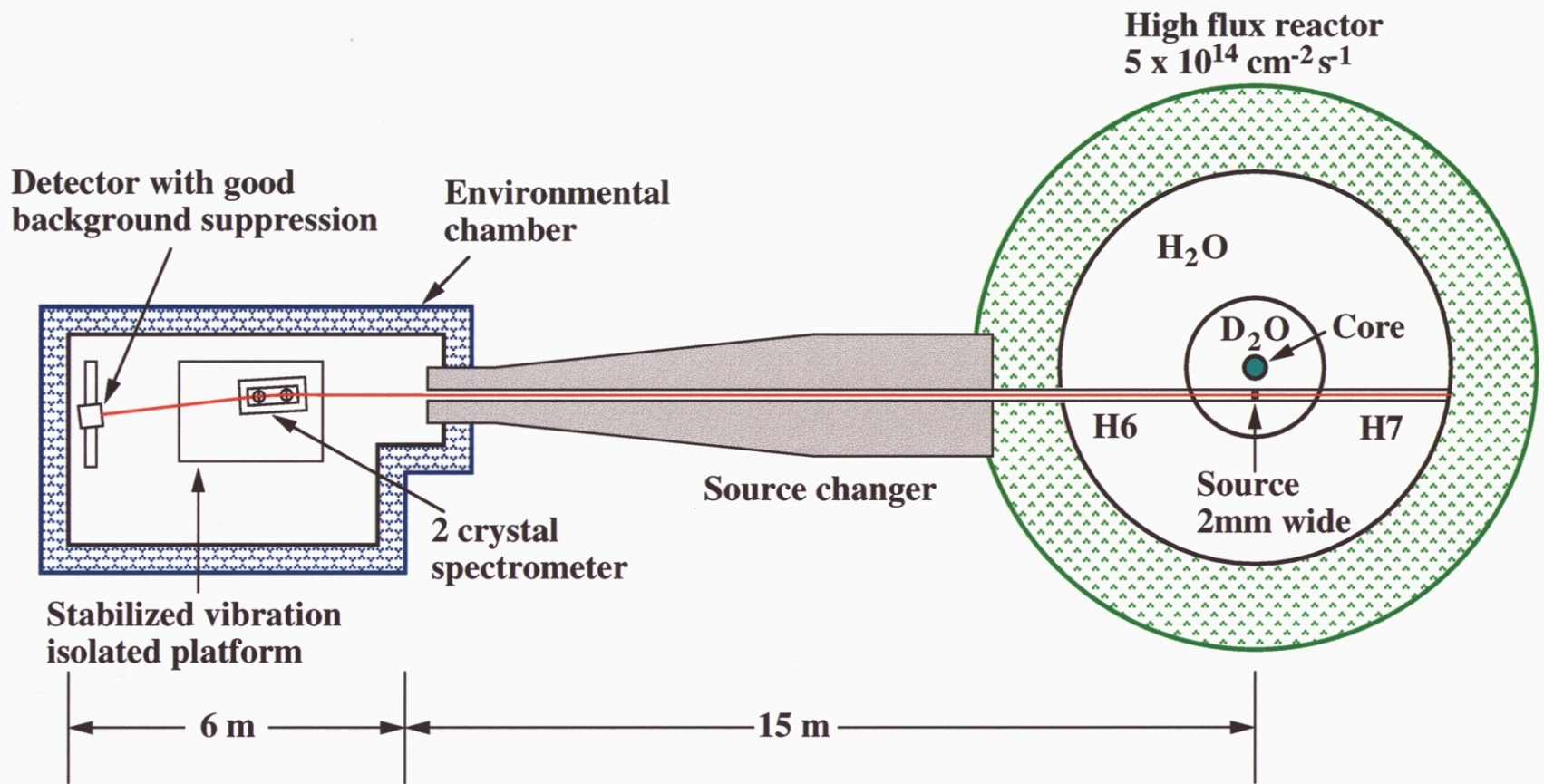
Two Crystal Geometry



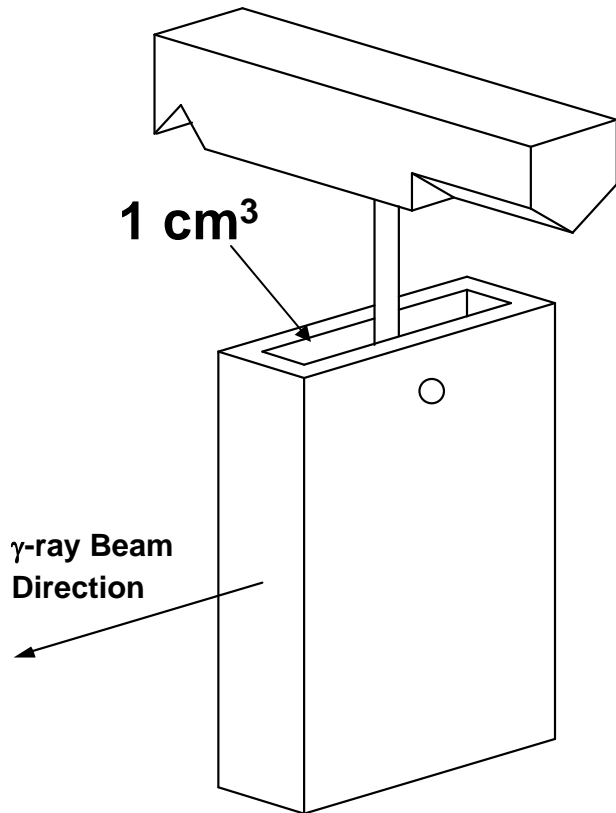
Grenoble - the scientific centers, ILL, and ESRF, together with Belledonne



NIST-ILL Gamma-ray Facility



Gamma-ray Sources



Activity depends upon:

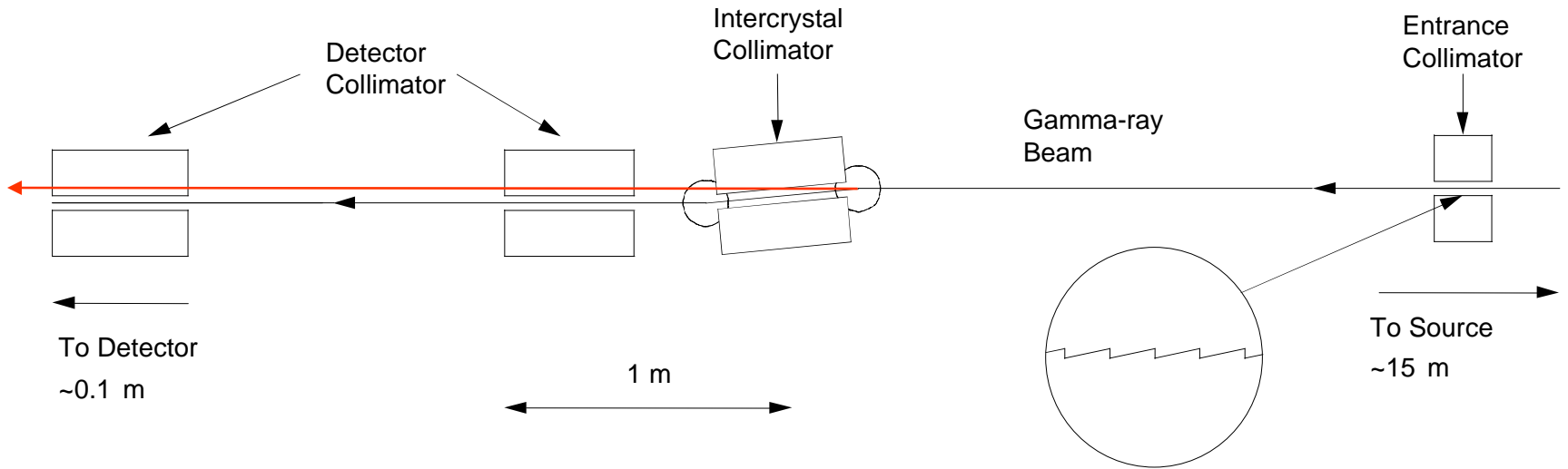
- Neutron flux
- Capture cross section
- Density of source material

Typical total activities:

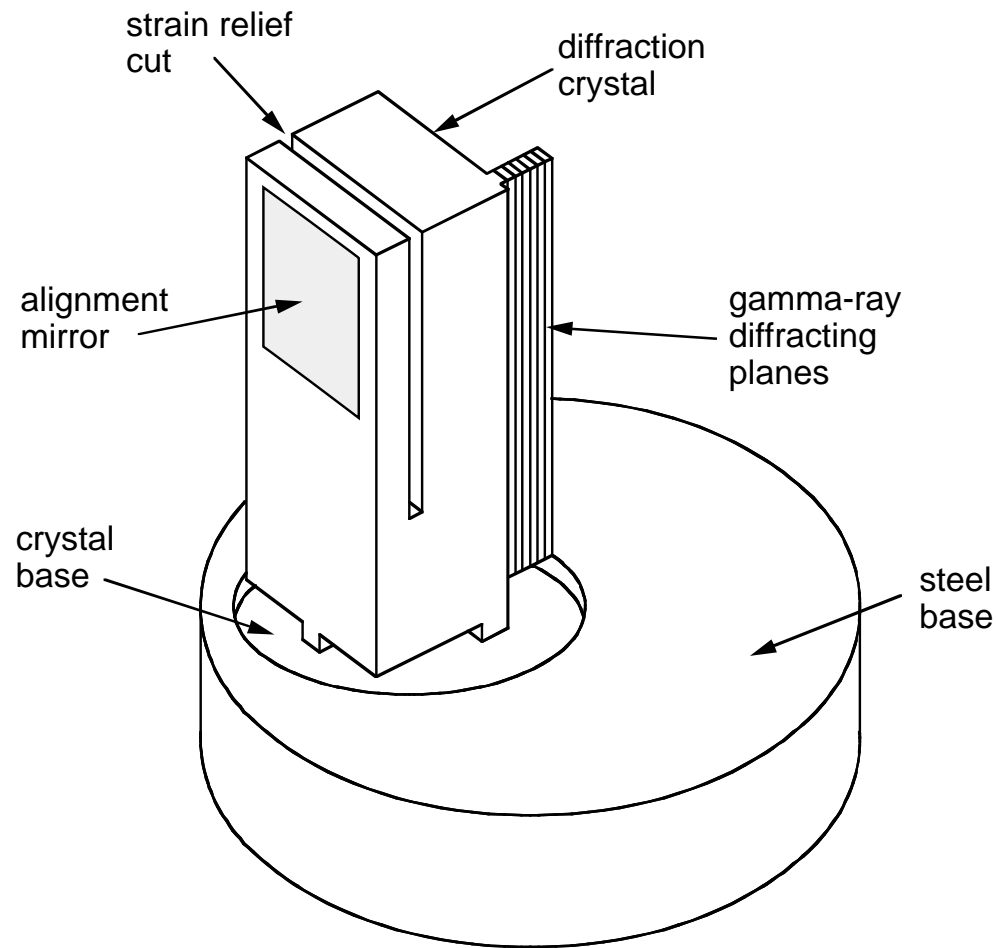
10^{13} - 10^{15} Bq (s^{-1})

kilo-curies

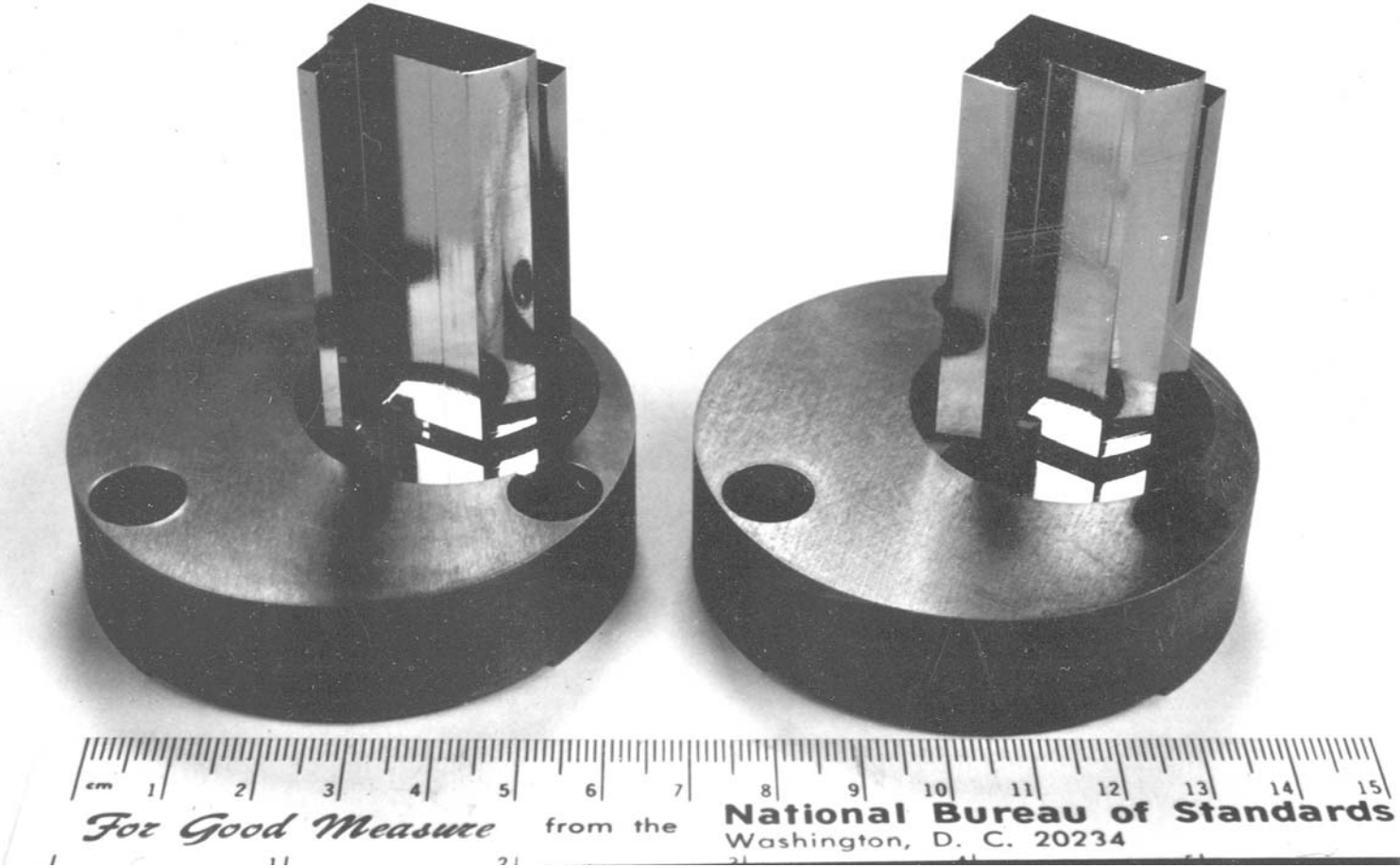
Collimation



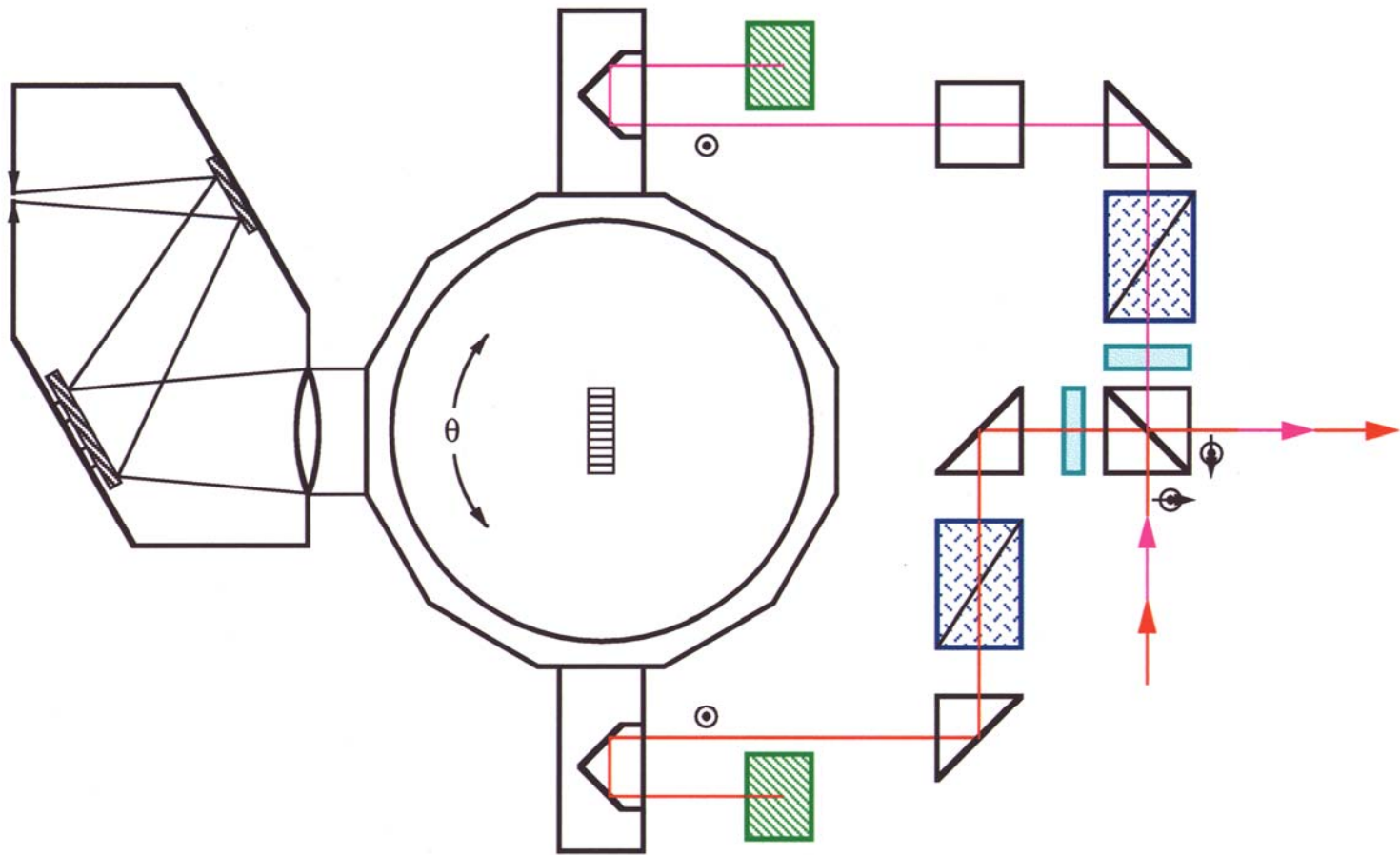
GAMS4 Diffraction Crystal



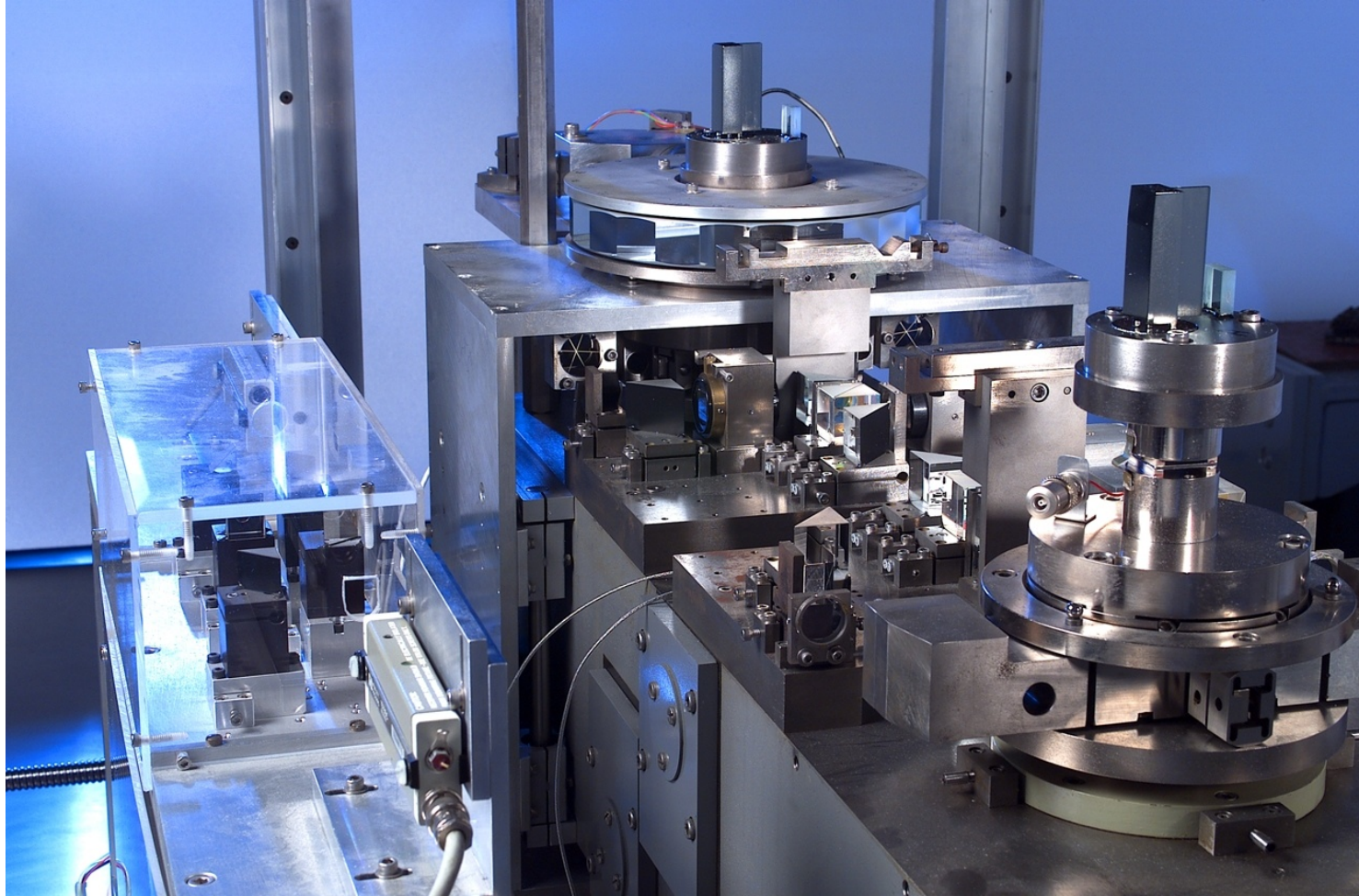
GAMS4 Diffraction Crystals



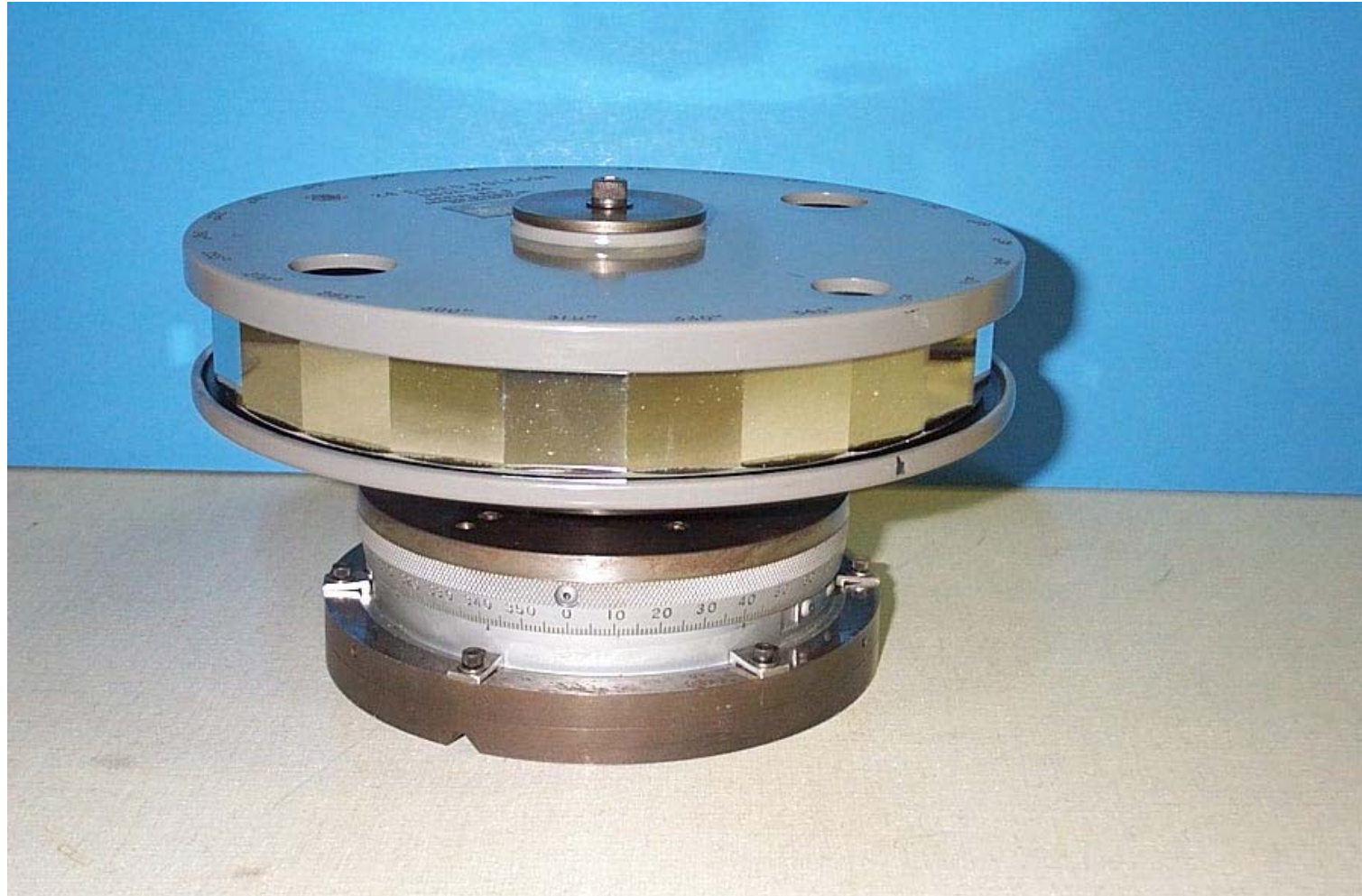
Angle Interferometer And Polygon



GAMS4 Spectrometer



Interferometer Calibration

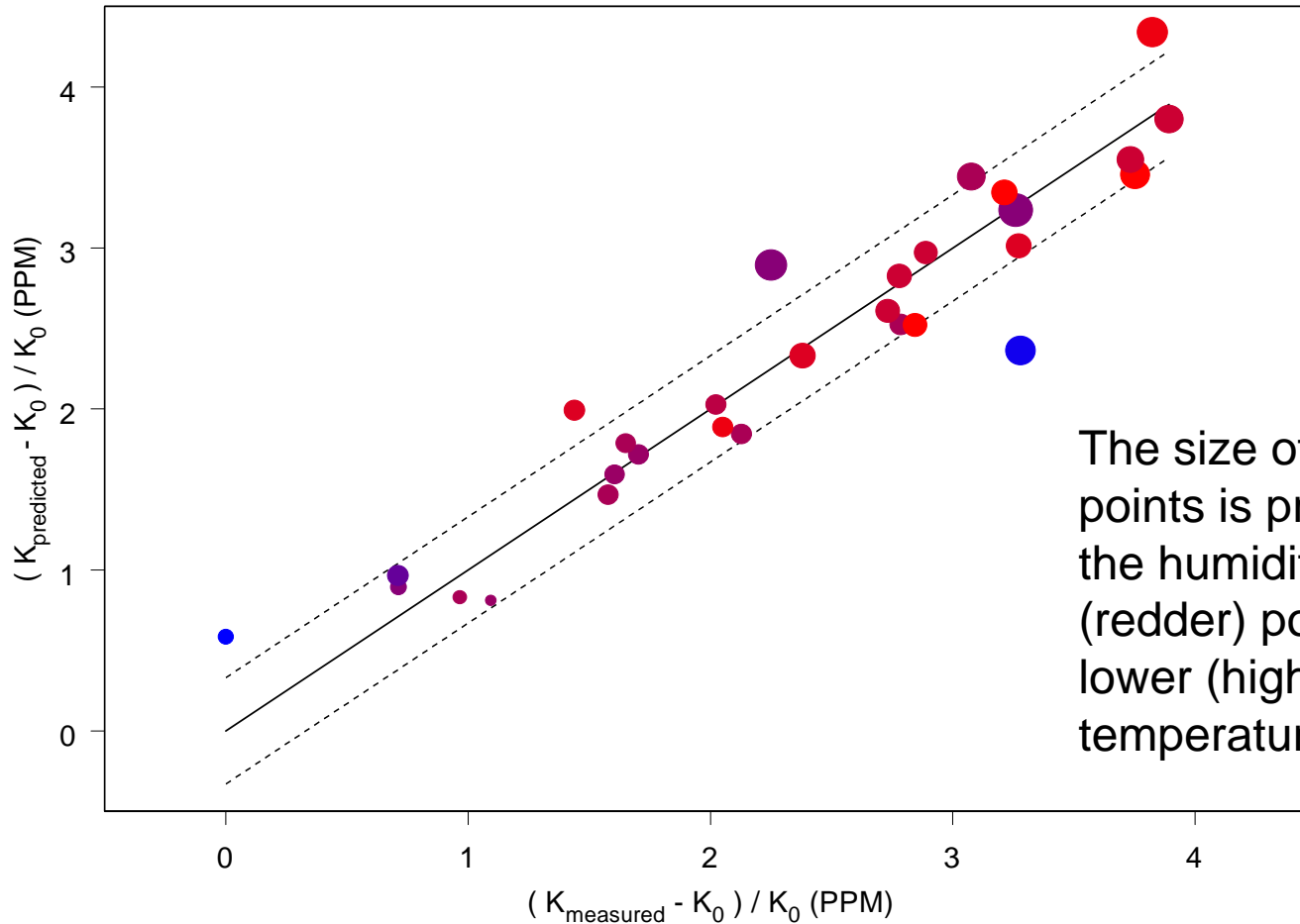


Interferometer Calibration

$$f = K \sin \theta + f_0$$

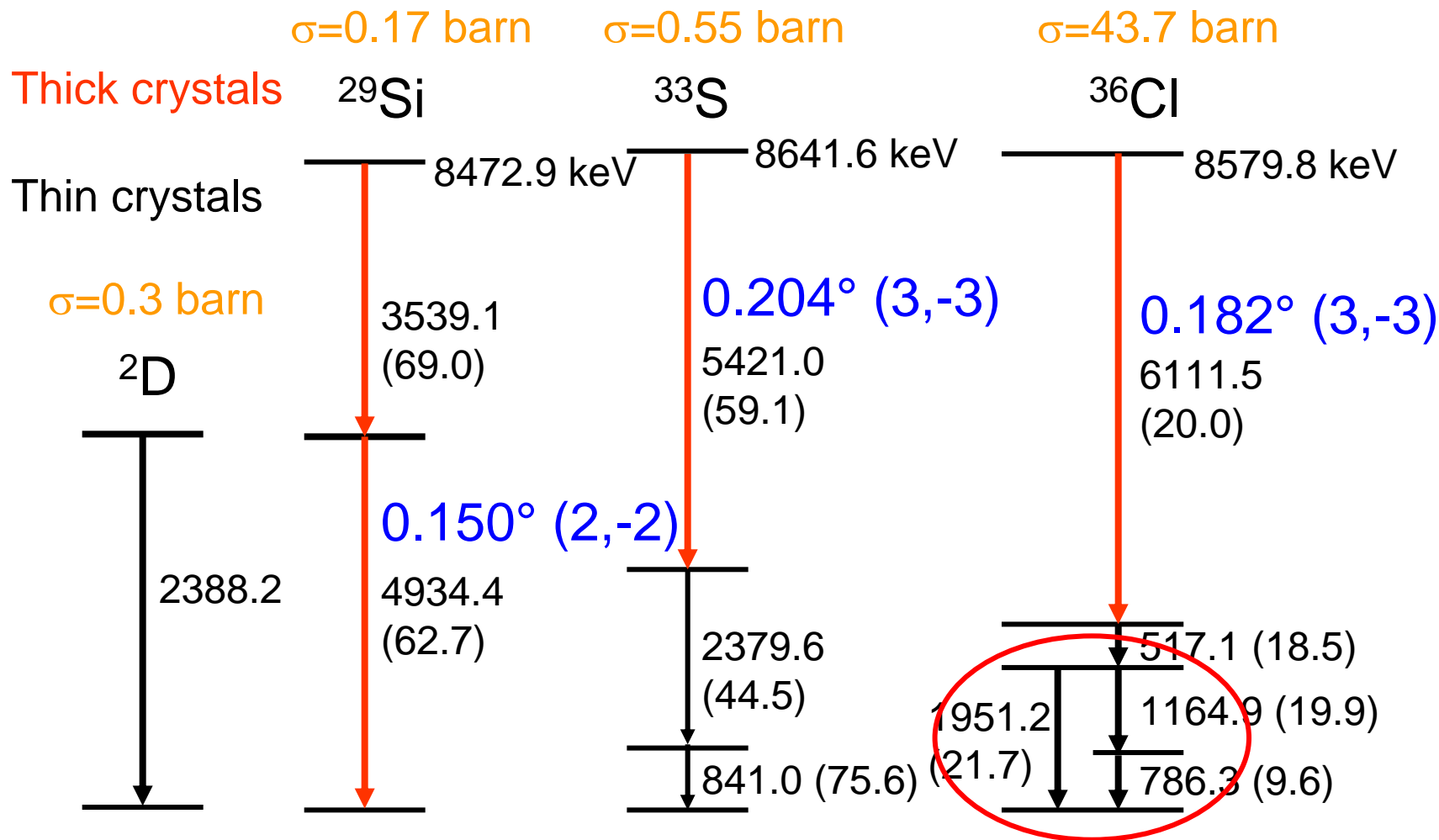
$$360^\circ = \sum_{i=1}^{24} \arcsin \left\{ \frac{f_{i+1} - f_0}{K} \right\} - \arcsin \left\{ \frac{f_i - f_0}{K} \right\}$$

GAMS4 Calibration Fit

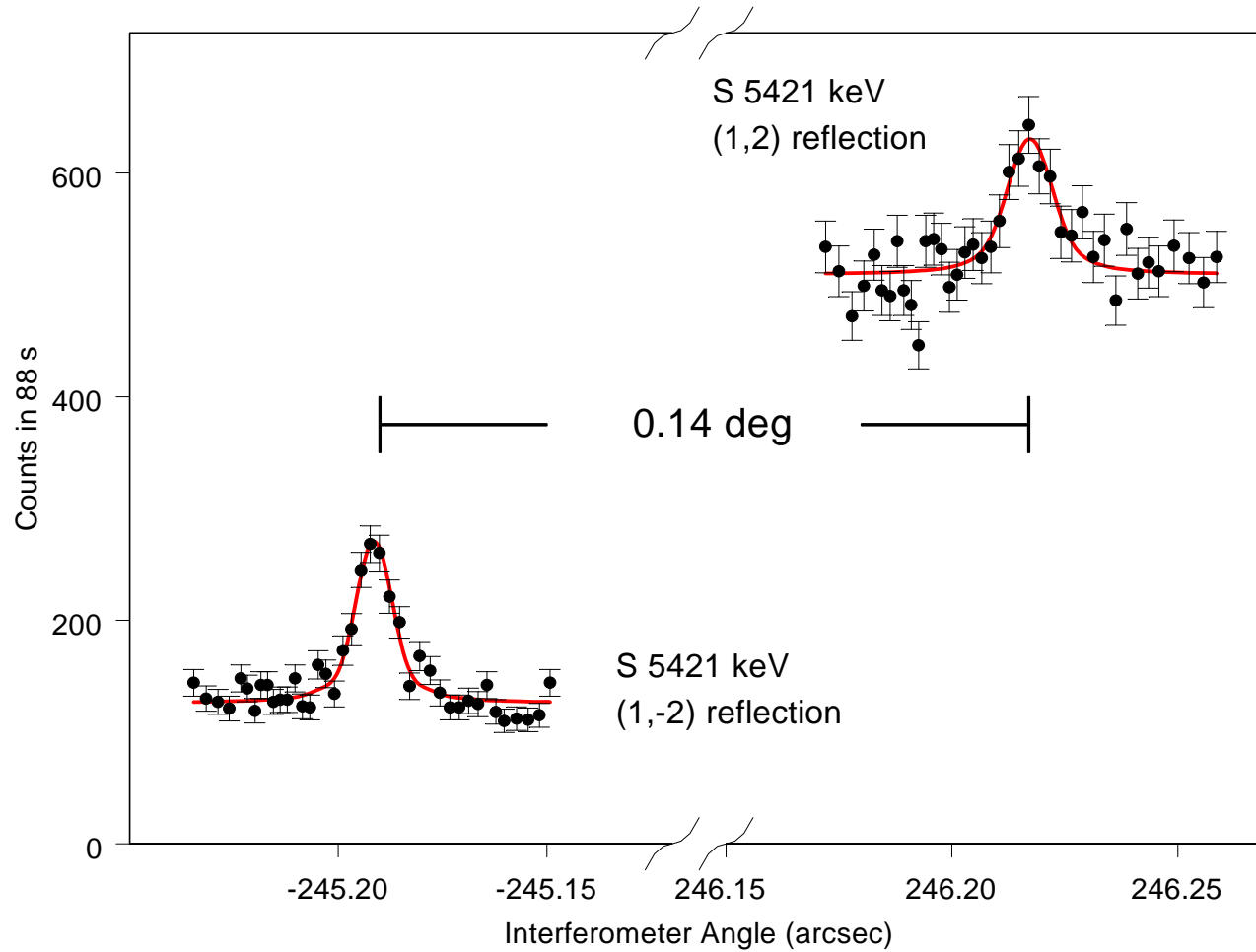




Binding Energy Measurements



Representative ^{33}S Profiles



Binding Energy Results

<i>Nuclide</i>	$\lambda_{be} \text{ £ } 10^{12} (m)$	$S_n \text{ £ } 10^3 (u)$	$u_r \text{ £ } 10^6$ <i>total</i>
^{29}Si	0.146318275(86)	9.0967793(53)	0.59
^{33}S	0.143472991(54)	9.2771820(35)	0.38
^{36}Cl	0.144507180(80)	9.2107883(51)	0.55
^2H	0.557341007(98)	2.38816996(42)	0.18

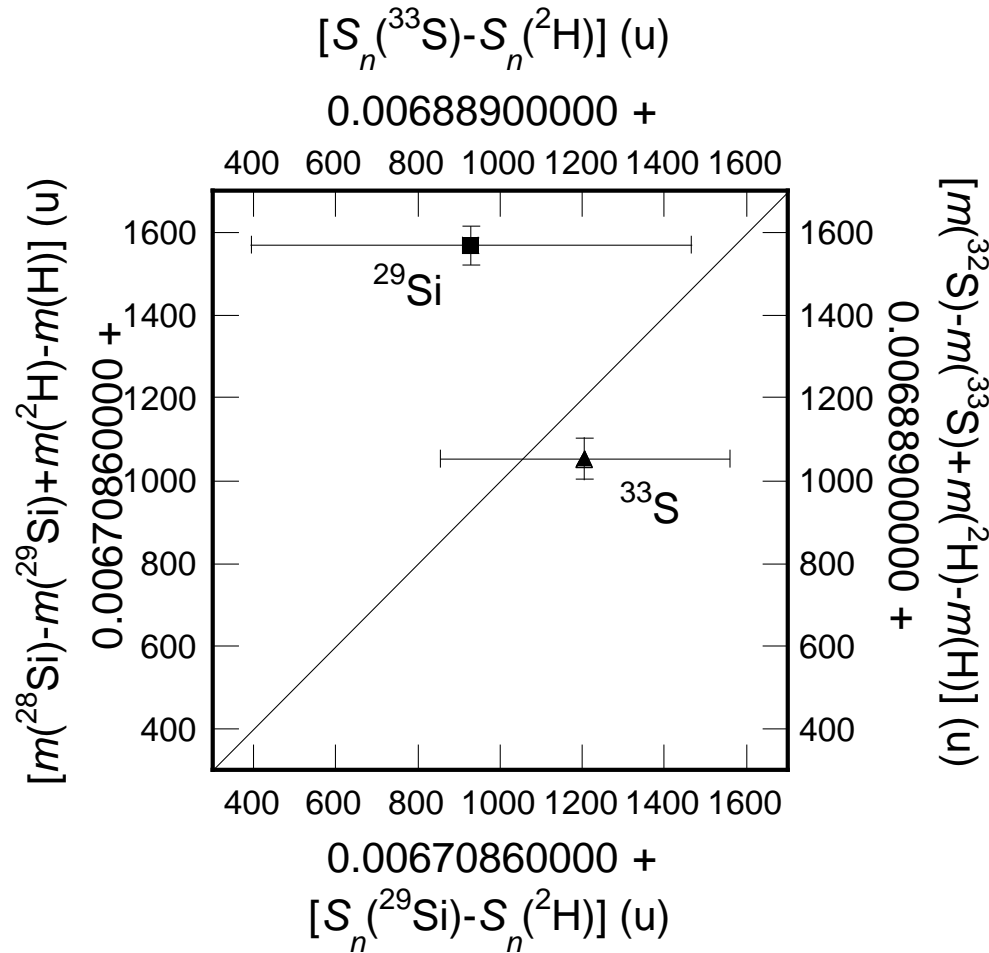
Uncertainty Sources

<i>Source</i>	<i>Relative σ $\times 10^6$</i>	<i>Comments</i>
statistics	~0.4	two weeks measuring time
calibration	0.4	interferometer instability
crystal temperature	0.1	$\Delta T_{\text{crystal}} = 0.05^\circ \text{K}$
vertical divergence	0.06	§5 mm over 15 m; γ -beam vs. plane of dispersion
crystal lattice spacing	0.05	conservative figure

Mass-Energy Comparison

$A+1X$	Δm from Penning trap (u)	Δm from GAMS4 (u)	Rel. Diff. $\times 10^7$
^{29}Si	0.00670861569(47)	0.00670860929(536)	-9.5(8.0)
^{33}S	0.00688901053(50)	0.00688901206(351)	2.2(5.1)
weighted average relative difference			-1.2(4.3)

Mass Difference Comparison





Special Relativity Test

$$\frac{E - \Delta mc^2}{E} = (-1.2 \pm 4.3) \times 10^{-7}$$

- The most precise direct test of $E = mc^2$
- This result is 55 times more accurate than the previous best direct test performed by comparing the electron and positron masses to the energy released in their annihilation
- Doesn't require the assumption of the existence of a preferred frame of reference in order to place constraints on proposed Lorentz-violating parameters



Towards 10^{-8} precision

- **Statistics:** longer measuring times, greater source density, reduce spectrometer drift, concentrate on sulfur and chlorine and radioactive isotopes
- **Calibration:** redesign interferometer, remove non-linearities, reduce sensitivity to environment
- **Crystal temperature:** more sensors on crystal, 3-4 mK absolute accuracy required
- **Vertical divergence:** need to rethink the way the beam and spectrometer are aligned with respect to each other
- **Crystal lattice spacing:** 10^{-8} precision possible

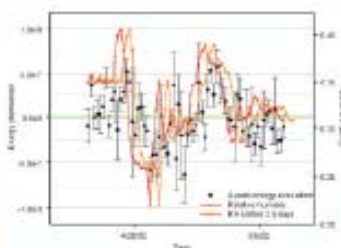
J. Krempel^{1,2}, M. Jentschel¹, P. Mutti¹, G. Mana³, B. Lauss⁴, P. Becker²

¹Institut Laue-Langevin, Grenoble (F), ²Physikalisch-Technische Bundesanstalt, Braunschweig (D), ³Istituto Nazionale di Ricerca Metrologica, Torino (I), ⁴Paul Scherrer Institut, 5232 Villigen (CH)

Performance

		Radian	Degree	ArcSec	Fringes
Interferometer properties	1 Fringe	633×10^6	36×10^6	0.13	1
	360°	6.3	360	1.3×10^6	9.9×10^7
	1"	4.8×10^5	0.3×10^3	1	7.7
Smallest Angle (interesting energy)	0.2°	3.5×10^3	0.2	720	5500
Accuracy	1/14000 F	45×10^{12}	2.6×10^6	9.3×10^6	7.1×10^5
Resolution limit (by electronics)	1/36000 F	18×10^6	1×10^6	3.6×10^6	2.8×10^5

Drift



Drift of the old GAMS4 interferometer at ILL due to a humidity sensitive glue

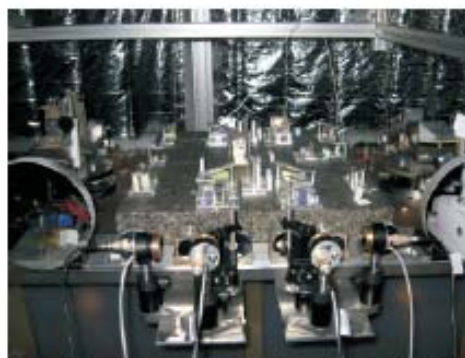
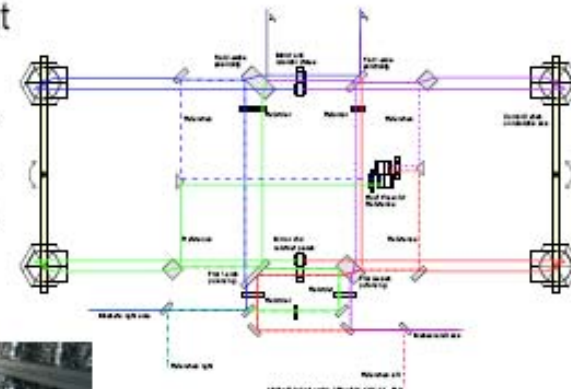


Drift of the old GAMS4 interferometer. Here the interferometer arm was fixed to 7.5° by the calibration unit. Despite the large drift of 10° it is possible to obtain a calibration constant with an uncertainty of 10° as only the drift over 30 minutes (one calibration step) is important. Thus, reducing the interferometer instability, as well as reducing the calibration/acquisition time will improve the result.

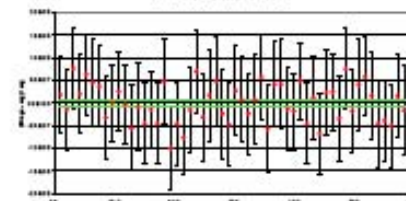
New Interferometer Layout

Main features:

- 2 axes in 1 interferometer: no longer drifts between two interferometers
- Compensating effects: elements are used twice. If they drift, the overall result stays constant.
- Spatial separation of beams, no frequency mixing – avoids non-linearity



The working prototype of the interferometer on GAMS5 at ILL



Stability test of the new interferometer: A 182keV was measured in (1,1) and (1,-1) Crystal order the angle difference varies not much over time, although there is no correction for temperature, pressure or humidity at all. The fit error for each point is about 4.6×10^{-5} . The standard deviation of all points is 4.2×10^{-5} . Thus the 54 points yield a total relative uncertainty of 5×10^{-6} .



Historical Highlights

- **1969** the first combined x-ray and optical interferometer (XROI) is realized at the NBS by Deslattes and collaborators
- **1973** “*X-Ray to Visible Wavelength Ratios*” links the optical “standard” to x-ray transition wavelengths for the first time
- **1978** a double crystal spectrometer is used at NBS to measure reactor-produced, non-prompt Au and Ir gamma-ray reference lines (675 keV maximum energy)



Historical Highlights

- **1982** spectrometer moves to ILL in search of prompt lines having higher energies
- **1984** instrument “aiming” difficulties lead to a major upgrade that includes a new platform, position and vibration stabilization, and new collimators
- **1986-present** GAMS4 becomes a scheduled ILL instrument used to measure binding energies, reference lines, lifetimes of nuclear excited states in the sub-picosecond range, and interatomic potentials in the 10 eV to 100 eV range
- **1998** GAMS5 becomes operational



Useful References

- The deuteron binding energy and the neutron mass
 - Kessler, E. G. *et al. Phys. Lett. A* **255**, 221-229 (1999).
- Precision measurement of fundamental constants using GAMS4
 - Dewey, M. S. *et al. J. Res. Natl. Inst. Stand. Technol.* **105**, 11-23 (2000).
- The GAMS4 flat crystal facility
 - Kessler, E. G. *et al. Nucl. Instrum. Meth. Phys. Res. A* **457**, 187-202 (2001).
- Precision measurement of the ^{29}Si , ^{33}S , and ^{36}Cl binding energies
 - Dewey, M. S. *et al. Phys. Rev. C* **73**, 044303-1 - 044303-11 (2006).
- A direct test of $E=mc^2$
 - Thompson, J. K. *et al. Nature* **430**, 58-61 (2005).